

VBM FUSION REACTOR D-D CYCLE

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Verdict :-

1. Formation of compound nucleus :-

Various charged particles fuse to form a homogeneous compound nucleus. The homogeneous compound nucleus is unstable. So, the central group of quarks [that which with gluons and other groups of quarks compose the homogeneous compound nucleus] with its surrounding gluons to become a stable and the just lower nucleus [a nucleus having lesser number of groups of quarks and lesser mass (or gluons) than the homogeneous nucleus] than the homogeneous one, includes the other nearby located groups of quarks with their surrounding gluons and rearrange to form the 'A' lobe of the heterogeneous compound nucleus. While the remaining groups of quarks [the groups of quarks that are not involved in the formation of the lobe 'A'] to become a stable nucleus includes their surrounding gluons (or mass) [out of the available mass (or gluons) that is not involved in the formation of the lobe 'A'] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus. The remaining gluons [the gluons (or the mass) that are not involved in the formation of any lobe] keeps both the lobes joined them together. Thus , due to formation of two lobes within into the homogeneous compound nucleus, the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

2. Splitting of the compound nucleus :-

The heterogeneous compound nucleus, due to its instability, splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into three lobes. Where the each separated lobe represent a separated particle. So, the two particles that represent the lobes 'A' and 'B' are stable while the third particle that represent the remaining gluons (or the reduced mass) is unstable . each particle that is produced due to splitting of the compound nucleus has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}) .

3. Propulsion of the produced particles :- The reduced mass converts into energy and propell both the particles with equal and opposite momentum .

Verdict :-

Various charged particles with different momentum by charge ratio when injected to a point 'F' where two uniform magnetic fields perpendicular the charged particles follow the confined circular paths of different radii passing through the common tangential magnetic field point 'F' (point of injection) by time and again.

Where ,

$$r \propto \frac{mv}{q}$$

Where , radius of the circular path followed by the charged particle is directly proportional to the momentum by charge .

Or

$$r = \frac{2E_k}{F_r}$$

Where ,

E_k = Kinetic energy of the confined particle.

F_r = Resultant force (net force) acting on the charged particle due to the magnetic fields.

By how we can apply the principle :-

Injection of bunches of charged particle :-

if the bunches of charged particles of same species (deuterons) are injected to a point 'F' where the two magnetic fields are applied , the charged particles (deuterons) of the first bunch will undergo to a confined circular path and will pass through this point 'F' [point of injection] by time and again and thus will be available for the deuterons of the later bunch(es) to be fused with at point 'F' .

2 Occurrence of fusion at point 'F' :-

As the deuterons of the n^{th} injected bunch reaches at point 'F' , it fuses with the deuterons of the first injected bunch passing through the point 'F' .

3. Confinement of the injected deuteron and Exhaustment of the produced charged and uncharged nuclei :-

1. confinement of injected deuteron

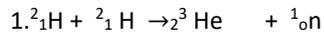
Conclusion :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the deuteron are along $+x$, $-y$ and $-z$ axes respectively . So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the deuteron lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the deuteron to undergo to a circular orbit of radius of 0.7160 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.1092 \text{ m}, -0.6403 \text{ m}, -0.6406 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak. And uninterruptedly goes on completing its circle until it fuses with the deuteron of later injected bunch (that reaches at point "F") at point "F"

2. Fusion reactions and the confinement or exhaustment of the produced charged and uncharged particles :-



[injected] [confined] [not confined]

€ Conclusion for the produced helium -3 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **-x, +y and +z** axes respectively .So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

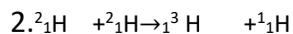
The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 0.4842 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.7501 \text{ m}, 0.4329 \text{ m}, 0.4331 \text{ m})$ where the magnetic fields are not applied.

So, It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the helium-3 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so, inspite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

Hence the helium-3 nucleus is not confined.

€ Conclusion for the produced neutron :- The produced neutron strike to the wall of the tokamak.



[injected] [confined] [not confined] [not confined]

Conclusion for the produced proton :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the proton are along **+x, -y and -z** axes respectively .So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular

orbit to be followed by the proton lies in the plane made up of positive x- axis, negative y-axis and negative z- axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 2.5977 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(4.0238 \text{ m}, -2.3233 \text{ m}, -2.3239 \text{ m})$. In trying to complete its circle, due to lack of space, it strikes to the base wall of the tokamak.

Hence the proton is not confined.

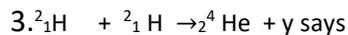
Conclusion for the produced triton :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the triton are along **-x, +y and +z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the triton lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the triton to undergo to a circular orbit of radius 1.1918 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.8463 \text{ m}, 1.0659 \text{ m}, 1.0661 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the triton gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. So, in spite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

Hence the triton is not confined.



[injected] [confined] [confined]

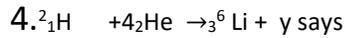
€ Conclusion for the produced helium -4 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the helium-4 nucleus are along **+x, -y and -z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-4 nucleus lies in the plane made up of positive x- axis, negative y- axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the helium-4 nucleus to undergo to a circular orbit of radius of 0.6997 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.0838 \text{ m}, -0.6258 \text{ m}, -0.6259 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

€ Conclusion for the produced gamma rays :- The gamma rays strike to the wall of the tokamak.



[injected] [confined] [confined]

€ Conclusion for the produced lithium -6 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-6 nucleus are along **+x, -y and -z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-6 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the lithium-6 nucleus to undergo to a circular orbit of radius of 0.6557 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.0158 \text{ m}, -0.5863 \text{ m}, -0.5865 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

€ Conclusion for the produced gamma rays :- The produced gamma rays strike to the wall of the tokamak.



[injected] [confined] [not confined] [not confined]

€ Conclusion for the produced lithium -7 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-7 nucleus are along **-x, +y and +z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-7 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the lithium-7 nucleus to undergo to a circular orbit of radius 0.2645 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.4098 \text{ m}, 0.2364 \text{ m}, 0.2365 \text{ m})$ where the magnetic fields are not applied.

So, It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the lithium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. so, inspite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

So the lithium-7 nucleus is not confined.

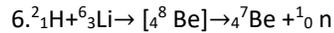
€ Conclusion for the produced proton :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x, -y and -z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 2.9812m.

It starts its circular motion from point P₁(0,0,0) and tries to reach at point P₂(4.6178 m, -2.6657 m, -2.6669 m). in trying to complete its circle, due to lack of space ,it strike to the base wall of the tokamak.

Hence the proton is not confined.



[injected] [confined] [not confined]

€ Conclusion for the produced beryllium -7 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the beryllium-7 nucleus are along **-x, +y and +z** axes respectively .So ,by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the beryllium-7 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

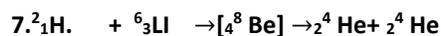
The resultant force (\vec{F}_r) tends the beryllium-7 nucleus to undergo to a circular orbit of radius 0.0773 m.

It starts its circular motion from point P₁(0,0,0) and tries to reach at point P₂(-0.1198 m, 0.0690 m, 0.0690m) where the magnetic fields are not applied.

So , It starts its circular motion from point P₁(0,0,0) and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the beryllium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , in spite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

Hence the beryllium-7 nucleus is not confined.

€ Conclusion for the produced neutron :-The produced neutron strike to the wall of the tokamak.



[injected] [confined] [not confined] [not confined]

€ Conclusion for the produced right hand side propelled helium -4 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the right hand side propelled helium-4 are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the right hand side propelled helium-4 lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the right hand side propelled helium-4 to undergo to a circular orbit of radius 4.8509 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(7.5140 \text{ m}, -4.3376 \text{ m}, -4.3396 \text{ m})$. in trying to complete its circle, due to lack of space, it strikes the base wall of the tokamak.

Hence the right hand side propelled helium-4 is not confined.

€ Conclusion for the produced left hand side propelled helium -4 nucleus :-

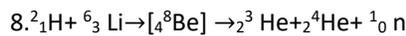
The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the left hand side propelled helium-4 nucleus are along **-x, +y and +z** axes respectively. So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the left hand side propelled helium-4 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the left hand side propelled helium-4 nucleus to undergo to a circular orbit of radius 3.7601m

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-5.8243 \text{ m}, 3.3630 \text{ m}, 3.3637 \text{ m})$ where the magnetic fields are not applied.

So, It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the left hand side propelled helium-4 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. so, in spite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

So the left hand side propelled helium-4 nucleus is not confined



[injected] [confined] [not confined] [not confined]

€ Conclusion for the produced helium -3 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **-x, +y and +z** axes respectively. So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 0.3899 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.6039 \text{ m}, 0.3487 \text{ m}, 0.3488 \text{ m})$ where the magnetic fields are not applied

So, It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the helium-3 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. so, in spite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

Hence the helium-3 nucleus is not confined.

€ Conclusion for the produced helium -4 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-4 nucleus are along **+x, -y and -z** axes respectively .

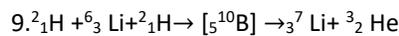
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-4 nucleus lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the helium-4 nucleus to undergo to a circular orbit of radius of 0.7980 m.

It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.2362 \text{ m}, -0.7135 \text{ m}, -0.7137 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuterium or deuterium of later injected bunch (that reaches at point "F") at point "F"

€ Conclusion for the produced neutron :- The neutron strike to the wall of the tokamak.



[injected] [confined] [confined] [not confined] [not confined]

Conclusion for the produced lithium -7 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-7 nucleus are along **-x, +y and +z** axes respectively . So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-7 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the lithium-7 nucleus to undergo to a circular orbit of radius 1.4805 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-2.2935 \text{ m}, 1.3238 \text{ m}, 1.3241 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the lithium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , in spite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

The lithium-7 nucleus is not confined within into the tokamak.

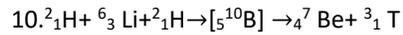
Conclusion for the produced helium -3 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **+x, -y and -z** axes respectively . So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-3 nucleus lies in the plane made up of positive x- axis, negative y-axis and negative z-axis

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 3.3766 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(5.2303 \text{ m}, -3.0200 \text{ m}, -3.0207 \text{ m})$. in trying to complete its circle, due to lack of space, it strikes to the base wall of the tokamak.

Hence the helium-3 nucleus is not confined.



[injected] [confined] [confined] [not confined] [not confined]

Conclusion for the produced beryllium -7 nucleus :-

The direction components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the beryllium-7 nucleus are along **-x, +y and +z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the beryllium-7 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-7 nucleus to undergo to a circular orbit of radius 1.0458 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.6201 \text{ m}, 0.9351 \text{ m}, 0.9353 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travels along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the beryllium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. So, in spite of completing its circle, it travels upward and strikes to the roof wall of the tokamak.

The beryllium-7 nucleus is not confined within into the tokamak.

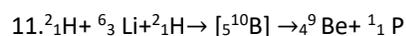
Conclusion for the produced triton :-

The direction components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the triton are along **+x, -y and -z** axes respectively. So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the triton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the triton to undergo to a circular orbit of radius 6.4952 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(10.0610 \text{ m}, -5.8093 \text{ m}, -5.8106 \text{ m})$. in trying to complete its circle, due to lack of space, it strikes to the base wall of the tokamak.

Hence the triton is not confined.



[injected] [confined] [confined] [not confined] [not confined]

Conclusion for the produced beryllium -9 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the beryllium-9 nucleus are along **-x , +y and +z** axes respectively .So, by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-9 nucleus to undergo to a circular orbit of radius 0.9078 m . It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.4061 \text{ m}, 0.8117 \text{ m}, 0.8121 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the beryllium-9 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

The beryllium-9 nucleus is not confined within into the tokamak.

Conclusion for the produced proton :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x , -y and -z** axes respectively .So ,by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x- axis, negative y-axis and negative z-axis .

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 5.9402 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(9.2013 \text{ m}, - 5.3117 \text{ m} , - 5.3141 \text{ m})$. in trying to complete its circle , due to lack of space ,it strike to the base wall of the tokamak.

Hence the proton is not confined.

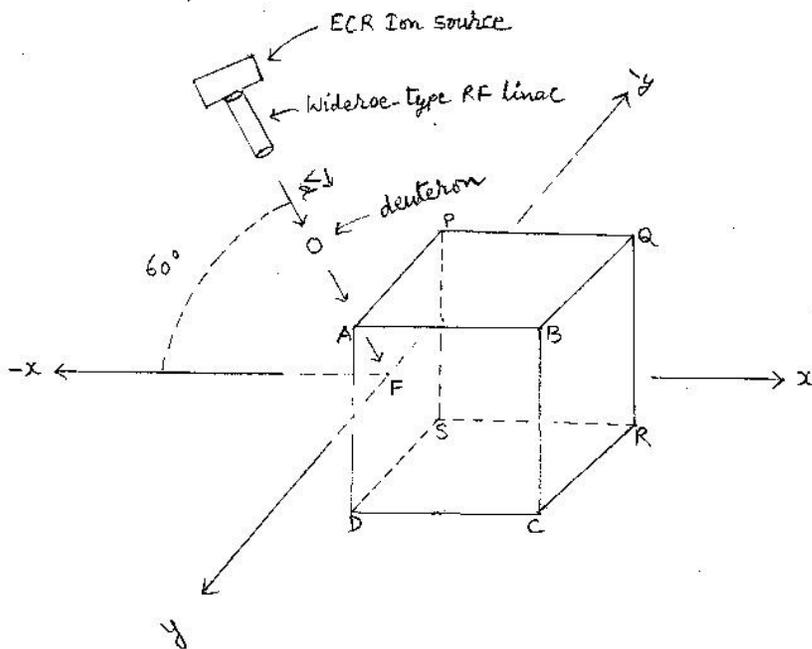
4. production of power:-

- (i) The non-useful charged nuclei (He-4) produced due to fusion reactions [D-T and D- ^3_2He] also undergo to a confined circular path but in trying to complete one round, the He-4 nucleus strike to the wall of the tokamak and thus be exhausted out of the tokamak with the help of vacuum pumps.
- (ii) The produced uncharged nuclei (neutrons) have no effects of magnetic fields and so follow an irregular straight path and strike to the wall of the tokamak and thus the neutrons are absorbed by the boron (the inner liner) of the tokamak.
- (iii) The produced are absorbed by the inner liner (graphite) of the tokamak.

The heat is transferred by a water – cooling loop from the tokamak to a heat exchanger to make steam.
 The steam will drive electrical turbines to produce electricity .
 The steam will be condensed back into water to absorb more heat from tokamak.

Thus, we get a steady state VBM fusion reactor based on D-D cycle.

Ion Source : Electron cyclotron resonance Ion source produce the 6×10^{19} deuterons per second. The produced bunches of deuterons enters into a wideroe-type RF linac



Where, the point's 'F' is a point of injection . The RF linac accelerate the deuterons. The accelerated deuterons enters into the main tokamak at point 'F' (or the point of injection) where the two magnetic fields perpendicular to each other are applied.

Minimum kinetic energy (E_m) required for fusion :

Tunneling – tunneling is a consequence of the Heisenberg uncertainty principle which states that the greater certainty we know the particle the less we know about its position in the space and vice versa

The uncertainty in the position is such that

when a proton collides with another proton , it may find itself on the other side of the coulomb barrier and in the attractive potential well of the strong force .

Work done to overcome the coulomb barriers

$$U = k z_1 z_2 q^2 / r_0$$

So, the kinetic energy of the particle should be equal to

$$E_m = \frac{1}{2} m v^2 = k z_1 z_2 q^2 / r_0$$

Rewriting the kinetic energy of the particle in terms of momentum

$$\frac{1}{2} m v^2 = p^2 / 2m = (h/\lambda)^2 / 2m$$

If we require that the nuclei must be closer than the de-broglie wavelength for tunneling to take over nuclei to fuse . ($r_0 = \lambda$)

$$k z_1 z_2 q^2 / r_0 = k z_1 z_2 q^2 / \lambda$$

where ,

$$\frac{1}{2} m v^2 = (h/\lambda)^2 / 2m = k z_1 z_2 q^2 / \lambda$$

$$\text{So, } h^2 / \lambda^2 2m = k z_1 z_2 q^2 / \lambda$$

$$\text{Or } \lambda = h^2 / k z_1 z_2 q^2 m$$

If we use this wavelength as the distance of closest approach , the kinetic energy required for fusion is –

$$E_m = \frac{1}{2} m v^2 = k z_1 z_2 q^2 / r_0 = k z_1 z_2 q^2 / \lambda = k z_1 z_2 q^2 \times 2k z_1 z_2 q^2 m / h^2$$

$$E_m = 2k^2 z_1^2 z_2^2 q^4 m / h^2$$

Where m is the mass of the penetrating (injected) nucleus .

Fusion velocity :- A particle having charge q and mass m should have a minimum velocity () to overcome the electrostatic repulsive force exerted by the other charge to reach into a fusion well where the distance of closest approach r =

$$E_m = \frac{1}{2} m v_{\text{fusion}}^2 = 2k^2 z_1^2 z_2^2 q^4 m / h^2$$

$$v_{\text{fusion}}^2 = 2 \times 2k^2 z_1^2 z_2^2 q^4 / h^2$$

$$v_{\text{fusion}} = 2k z_1 z_2 q^2 / h$$

Minimum kinetic energy required for D – D fusion :

$$E_m = \frac{1}{2} m v_{\text{fusion}}^2 = \frac{1}{2} m_d (2k z_1 z_2 q^2 / h)^2$$

$$E_m = \frac{2 K^2 Z_1^2 Z_2^2 q^4 m}{h^2}$$

For D-D fusion

$$Z_1 = Z_2 = 1$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$m = 3.3434 \times 10^{-27} \text{ kg}$$

$$h = 6.62 \times 10^{-34} \text{ J-S}$$

$$k = 9 \times 10^9 \text{ Nm/C}^2$$

$$E_{D-D} = \frac{2 \times (9 \times 10^9)^2 \times 1^2 \times 1^2 \times (1.6 \times 10^{-19})^4 \times 3.3434 \times 10^{-27}}{(6.62 \times 10^{-34})^2} \text{ J}$$

$$= \frac{3549.63161088 \times 10^{18} \times 10^{-76} \times 10^{-27}}{43.8244 \times 10^{-68}} \text{ J}$$

$$43.8244 \times 10^{-68}$$

$$= 80.9966961528 \times 10^{-17} \text{ J}$$

$$= 50.6229350955 \times 10^2 \text{ eV}$$

$$E_{D-D} = 5.0622 \text{ keV}$$

$$= 0.0050622 \text{ MeV}$$

Minimum kinetic energy required by a deuteron for D-Helium -4 fusion :

$$E_m = E_{D-D} \times Z_2^2 \quad [Z_2 = 1]$$

$$= 0.0050622 \times 4 \text{ MeV}$$

$$= 0.0202488 \text{ MeV}$$

$$= 20.2488 \text{ MeV}$$

Minimum kinetic energy required by a helium -4 nucleus to take part in D – He-4 fusion :

$$E_m = \frac{1}{2} m v_{\text{fusion}}^2 = \frac{1}{2} m_{\text{He-4}} \left(\frac{2k z_1 z_2 q^2}{h} \right)^2$$

$$E_m = \frac{2 K^2 Z_1^2 Z_2^2 q^4 m_{\text{He-4}}}{h^2}$$

$$E_m = \frac{2 K^2 Z_1^2 Z_2^2 q^4 m}{h^2}$$

$$Z_1 = 2, Z_2 = 1$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$m = 6.64449 \times 10^{-27} \text{ kg}$$

$$h = 6.62 \times 10^{-34} \text{ J-S}$$

$$k = 9 \times 10^9 \text{ Nm/C}^2$$

$$E_{\text{He-D}} = \frac{2 \times (9 \times 10^9)^2 \times 2^2 \times 1^2 \times (1.6 \times 10^{-19})^4 \times 6.64449 \times 10^{-27}}{(6.62 \times 10^{-34})^2} \text{ J}$$

$$= \frac{28217.3736222 \times 10^{18} \times 10^{-76} \times 10^{-27}}{43.8244 \times 10^{-68}} \text{ J}$$

$$= 643.87358691 \times 10^{-17} \text{ J}$$

$$= 402.420991818 \times 10^2 \text{ eV}$$

$$E_{\text{he-D}} = 40.242 \text{ keV}$$

$$= 0.040242 \text{ MeV}$$

Minimum kinetic energy required by lithium-6 nucleus for D–lithium-6 fusion :

$$E_m = \frac{1}{2} m v_{\text{fusion}}^2 = \frac{1}{2} m_{\text{Li-6}} (2k z_1 z_2 q^2 / h)^2$$

$$E_m = \frac{2 K^2 Z_1^2 Z_2^2 q^4 m_{\text{Li-6}}}{h^2}$$

$$h^2$$

$$Z_1 = 3, Z_2 = 1$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$m = 9.9853 \times 10^{-27} \text{ kg}$$

$$h = 6.62 \times 10^{-34} \text{ J-S}$$

$$k = 9 \times 10^9 \text{ Nm/C}^2$$

$$E_{\text{Li-D}} = \frac{2 \times (9 \times 10^9)^2 \times 3^2 \times 1^2 \times (1.6 \times 10^{-19})^4 \times 9.9853 \times 10^{-27}}{(6.62 \times 10^{-34})^2} \text{ J}$$

$$(6.62 \times 10^{-34})^2$$

$$= \frac{95411.0273126 \times 10^{18} \times 10^{-76} \times 10^{-27}}{43.8244 \times 10^{-68}} \text{ J}$$

$$43.8244 \times 10^{-68}$$

$$= 2177.12113143 \times 10^{-17} \text{ J}$$

$$= 1360.70070714 \times 10^2 \text{ eV}$$

$$E_{\text{Li-D}} = 136.0700 \text{ keV}$$

$$= 0.13607 \text{ MeV}$$

Particle accelerator :

with the help of a wideroe- type linac we accelerate the deuterons up to 102.4 Kev .

A wideroe type linear accelerator

$$K_n = n q v_o T_{tr}$$

where, $v_o = v_{max} = 40$ KV and $n=6$

$$\sin \psi_o = T_{tr} = 0.64 \text{ and } q = 1.6 \times 10^{-19} \text{ C}$$

$$K_2 = 6 \times 1.6 \times 10^{-19} \times 40 \times 0.64 \text{ KJ}$$

$$= 245.76 \times 10^{-19} \text{ KJ}$$

$$= 153.6 \text{ Kev} [1.6 \times 10^{-19} \text{ J} = 1 \text{ ev}]$$

1. length of the first drift tube

$$L_1 = \frac{n}{2} \times \frac{\sqrt{q v_{max} \sin \psi_o}}{\sqrt{2m}}$$

f_{rf}

Where , $f_{rf} = 7 \times 10^6 \text{ Hz}$, $m = 3.3434 \times 10^{-27} \text{ kg}$

$$L_1 = \frac{\sqrt{1}}{7 \times 10^6} \times \frac{\sqrt{1.6 \times 10^{-19} \times 40 \times 10^3 \times 0.64}}{\sqrt{2 \times 3.3434 \times 10^{-27}}} \text{ m}$$

$$= \frac{\sqrt{1}}{7 \times 10^6} \times \frac{\sqrt{409.6 \times 10^{10}}}{\sqrt{6.6868}} \text{ m}$$

$$= \frac{1}{7 \times 10^6} \times \sqrt{61.2550098701 \times 10^{10}} \text{ m}$$

$$= \frac{1}{7 \times 10^6} \times 7.8265 \times 10^5 \text{ m}$$

$$= 1.11807 \times 10^{-1} \text{ m}$$

$$= 11.1807 \times 10^{-2} \text{ m}$$

$$l_2 = \sqrt{2} \times l_1$$

$$= 1.4142 \times 11.1807 \times 10^{-2} \text{ m}$$

$$= 15.8117 \times 10^{-2} \text{ m}$$

$$l_3 = \sqrt{3} \times l_1$$

$$= 1.732 \times 11.1807 \times 10^{-2} \text{ m}$$

$$= 19.3649 \times 10^{-2} \text{ m}$$

$$L_4 = \sqrt{4} \times l_1$$

$$= 2 \times 11.1807 \times 10^{-2} \text{ m}$$

$$= 22.3614 \times 10^{-2} \text{ m}$$

$$l_5 = 2.2360 \times 11.1807 \times 10^{-2} \text{ m}$$

$$= 25.0000 \times 10^{-2} \text{ m}$$

$$l_6 = 2.4494 \times 11.1807 \times 10^{-2} \text{ m}$$

$$= 27.3860 \times 10^{-2} \text{ m}$$

Total length of the wideroe –type linac is -

$$L = l_1 + l_2 + l_3 + l_4 + l_5 + l_6$$

$$= [11.1807 + 15.8117 + 19.3649 + 22.3614 + 25.0000 + 27.3860] \times 10^{-2} \text{ m}$$

$$= 121.1047 \times 10^{-2} \text{ m}$$

The tokamak

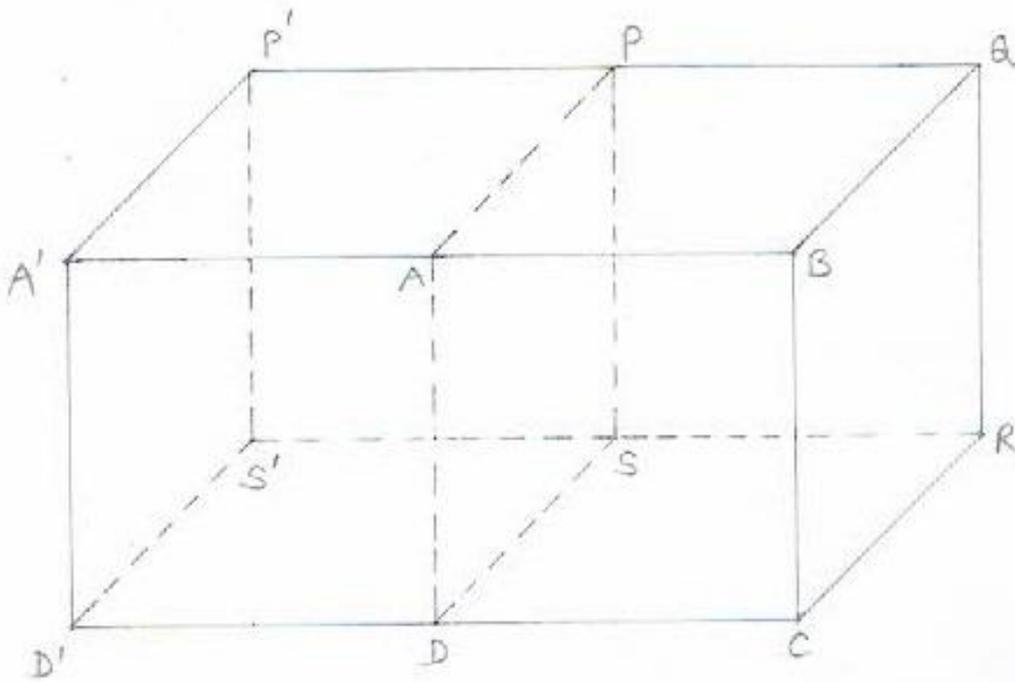
The tokamak has two parts – one is the main tokamak and the other is the extended tokamak .

The points A, B, C, D, P, Q, R, and S represents the corners of the walls of the main tokamak while all the other remaining points represents the corners of the walls of the extended tokamak .

The tokamak is made up of steel .

The graphite or the boron is used as the inner liner of the tokamak to absorb the thermal neutrons .

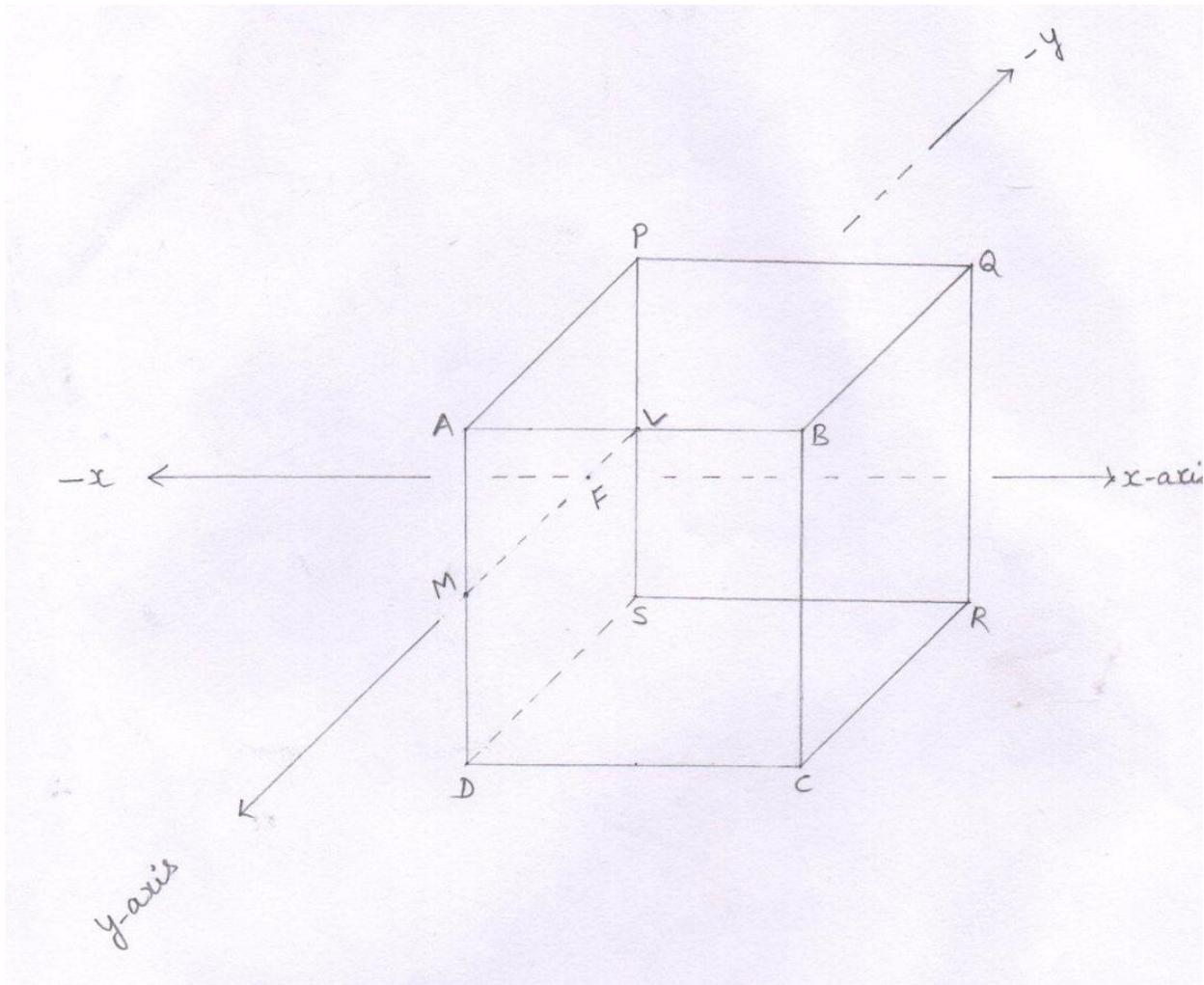
The main tokamak with its extensions



The location of the point of injection (F) of the charged particles (deuterons) or the location of the center of fusion (F) within - into the tokamak is -

Or

The location of the point ' F ' [or the point of injection or the center of fusion]



where, $MF=0.1\text{m}$ and $LF=1.40\text{ m}$

$AM = 0.1\text{ m}$ $MD = 1.40\text{ m}$

$PL = 0.1\text{ m}$ $LS = 1.40\text{ m}$

$AP = AD=DS= PS= ML = 1.5\text{ m}$ $AB=DC= PQ=SR =2\text{ m}$

$$BQ=CR=BC= RQ =1.5 \text{ m}$$

Total surface area of the tokamak

Surface area of the walls of the main tokamak

$$I \quad ABCD = \text{length} \times \text{breadth} = 2 \text{ m} \times 1.5 \text{ m} = 3 \text{ m}^2$$

$$ii \quad PQRS = 2 \text{ m} \times 1.5 \text{ m} = 3 \text{ m}^2$$

$$iii \quad APQB = 2 \text{ m} \times 1.5 \text{ m} = 3 \text{ m}^2$$

$$IV \quad DSRC = 2 \text{ m} \times 1.5 \text{ m} = 3 \text{ m}^2$$

$$V \quad BQRC = 1.5 \text{ m} \times 1.5 \text{ m} = 2.25 \text{ m}^2$$

So , the total surface area of the main tokamak = 14.25 m² eq.(9)

The points APSD do not represent a wall . it is a blank place that allows the injected protons to enter into the main tokamak . (or the region where the magnetic fields are applied .)

iiTotal Surface area of of the tokamak : -

$$\text{surface area} = 2(lxb + bxh + hxl)$$

$$\text{where, } l = 4 \text{ m}$$

$$b = 1.5 \text{ m}$$

$$h = 1.5 \text{ m}$$

$$S = 2(4 \times 1.5 + 1.5 \times 1.5 + 1.5 \times 4) \text{ m} = 2 \times 14.25 \text{ m} = 28.50 \text{ m}$$

Magnetic field coils

VBM fusion reactor has two pairs of semicircular magnetic field coils . out of them , one pair of semicircular magnetic field coils is vertically erected while another pair of semicircular magnetic field coils is horizontally lying .

1 Vertically erected magnetic field coils :

In a VBM fusion reactor , there are two vertically erected semicircular magnetic field coils that act as a helmholtz coil.

The distance between the two vertically erected semicircular coils is equal to the radius of any one of the semicircular magnetic field coil .

$$\text{i.e. } d = r = 2.5 \text{ m}$$

The vertically erected semicircular magnetic field coils acting as a helmholtz coil produce a uniform magnetic field (\vec{B}_y) parallel to y – axis .

horizontally lying magnetic field coils :

in a VBM fusion reactor , there are two horizontally lying semicircular magnetic field coils that acts as a helmholtz coil .

the distance between the two horizontally lying semicircular magnetic field coils is equal to the radius of any one of the semicircular magnetic field coil .

$$\text{i.e. } d = r = 2.2 \text{ m}$$

The horizontally lying semicircular magnetic field coils acting as a helmholtz coil produce a uniform magnetic field (\vec{B}_z) parallel to z –axis .

Magnetic field due to a semicircular coil at point x is –

$$B_1 = \mu_o / 4\pi \times \pi R^2 ni / (R^2 + x^2)^{3/2}$$

Magnetic fields due to a semicircular coil at the x , If $x = R/2$

$$B_1 = \mu_o / 4\pi \times \pi R^2 ni / (R^2 + R^2 / 4)^{3/2} \quad [\because x = R / 2]$$

$$= 8 / 5\sqrt{5} \times \mu_o \text{ ni} / 4R$$

So, the magnetic field in the mid plane of the two semicircular coils acting as a helmholtz coil is

$$B_T = B_1 + B_2$$

$$= 2 B$$

$$[\because B_1 = B_2 = B]$$

$$= \frac{16}{5\sqrt{5}} \times \mu_o ni / 4R$$

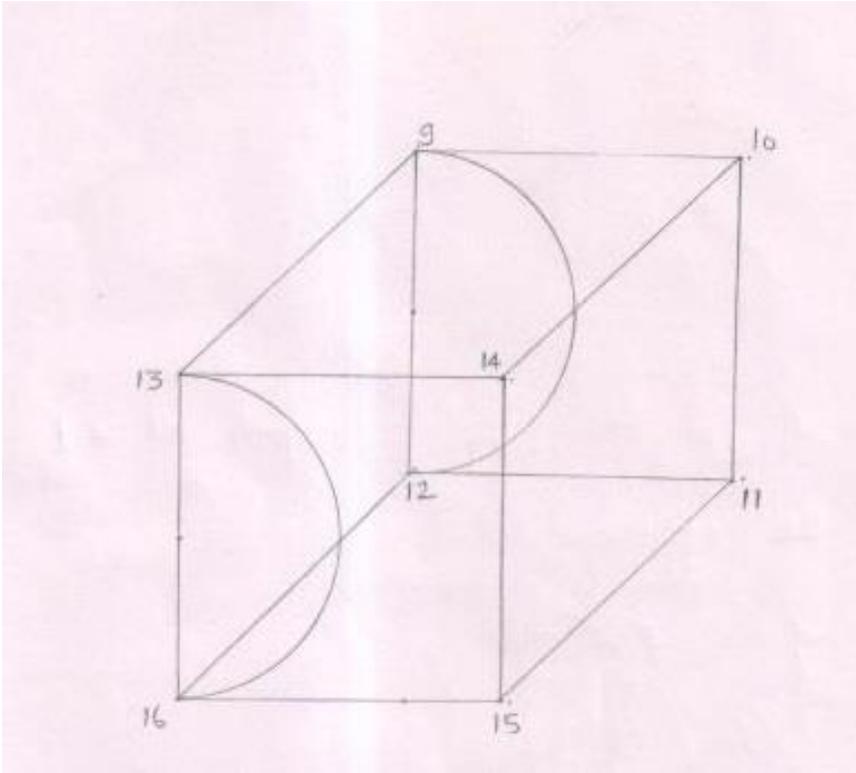
from eq. (11)

$$= 1.43 \times \mu_o ni / 4R$$

$$= 1.43 B_{center}$$

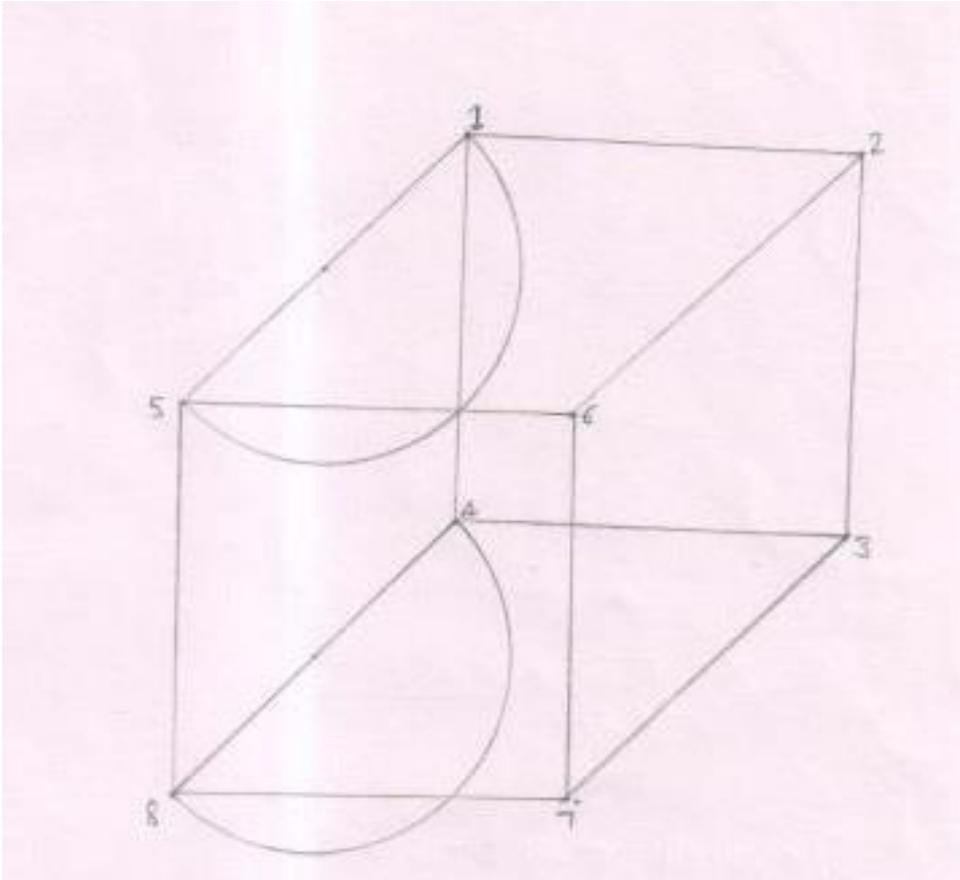
$$[B_{center} = \mu_o ni / 4R] \text{ eq.(12)}$$

The vertically erected magnetic field coils .



The vertically erected magnetic field coils are exterior to the horizontally lying magnetic field coils which in turn are exterior to the the main tokamak. so, the area covered up by the points 9,10,11,12,13,14,15,16, is greater than the area covered up by the points 1, 2, 3, 4, 5, 6, 7 and 8. The area covered up by the points 1,2,3,4,5,6,7,8 is greater than the area covered up by the points P, Q, R, S, A, B, C, D of the main tokamak .

The horizontally lying semicircular magnetic field coils



The vertically erected semicircular coils are exterior to the main tokamak and also exterior to the horizontally lying magnetic field coils. so, the area covered up by points 9, 10, 11, 12, 13, 14, 15, 16 is more than the area covered up by the points 1, 2, 3, 4, 5, 6, 7, 8. The area covered up by the points A, B, C, D, P, Q, R, S is less than the area covered up by the points 1, 2, 3, 4, 5, 6, 7 and 8.

Magnetic field (B_y) in the mid plane of the two vertically erected semicircular coils acting as a helmholtz coil is -

$$B_y = 1.43 B_{\text{centre}}$$

$$B_{\text{centre}} = \frac{\mu_0 n i}{4 R}$$

Where ,

$n = 5570$ turns

$i = 100$ Amperes

$R = 2.5$ m

$$\text{so, } B_{\text{centre}} = \frac{4 \times 22 \times 10^{-7} \times 5570 \times 100}{7 \times 4 \times 2.5} \quad \text{Tesla}$$

$$12254 \times 10^{-3} / 175 \quad \text{Tesla}$$

$$B_{\text{centre}} = 70.02285 \times 10^{-3} \quad \text{Tesla}$$

$$= 7.002285 \times 10^{-2} \text{Tesla}$$

$$B_y = 1.43 B_{\text{centre}}$$

$$B_y = 1.43 \times 7.002285 \times 10^{-2} \text{Tesla}$$

$$= 10.0132 \times 10^{-2} \text{Tesla}$$

$$= 1.0013 \times 10^{-1} \quad \text{Tesla}$$

Magnetic field (B_z) in the mid plane of the two horizontally lying semicircular coils acting as a helmholtz coil is -

$$B_y = 1.43 B_{\text{centre}}$$

$$B_{\text{centre}} = \frac{\mu_0 n i}{4 R}$$

4 R

Where ,

$n = 4900$ turns

$i = 100$ Amperes

$R = 2.2$

$$\text{so, } B_{\text{centre}} = \frac{4 \times 22 \times 10^{-7} \times 4900 \times 100}{7 \times 4 \times 2.2} \quad \text{Tesla}$$

$$B_{\text{centre}} = 0.07 \text{Tesla}$$

$$B_z = 1.43 \times 0.07 \text{Tesla}$$

$$= 0.1001 \quad \text{Tesla}$$

$$= 1.001 \times 10^{-1} \text{Tesla}$$

The directions of magnetic fields

The direction of flow of current in the horizontally lying semicircular coils is clockwise so that the direction of the produced magnetic field is according to negative z – axis (i. e. downward)

$$\text{As } B_z = 1.001 \times 10^{-1} \text{Tesla}$$

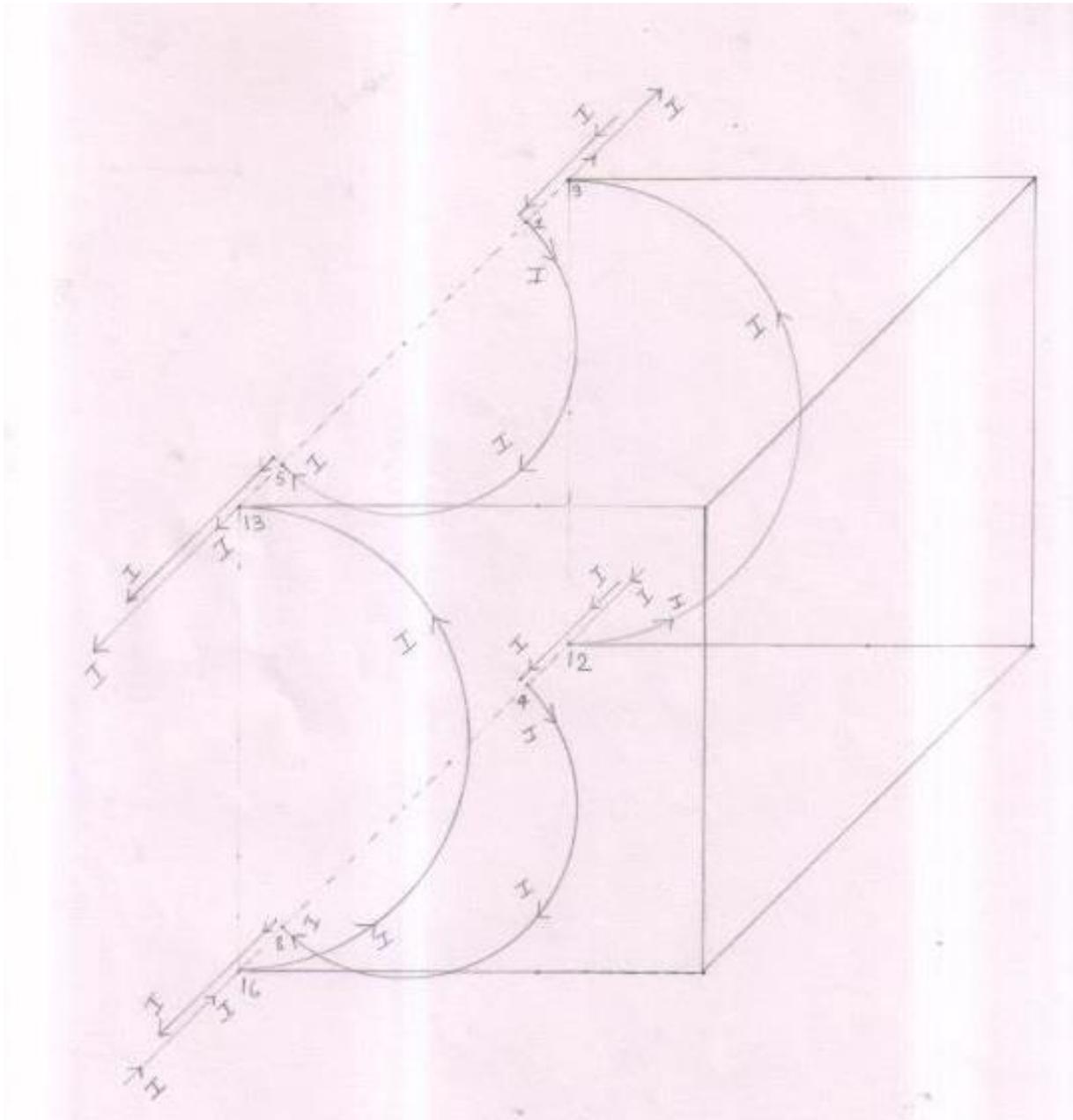
$$\text{So } \vec{B_z} = - 1.001 \times 10^{-1} \text{Tesla}$$

The direction of flow of current in the vertically erected magnetic coils is anticlockwise so that the direction of the produced magnetic field is according to positive y – axis .

$$\text{As } B_y = 1.0013 \times 10^{-1} \text{Tesla}$$

So $\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$

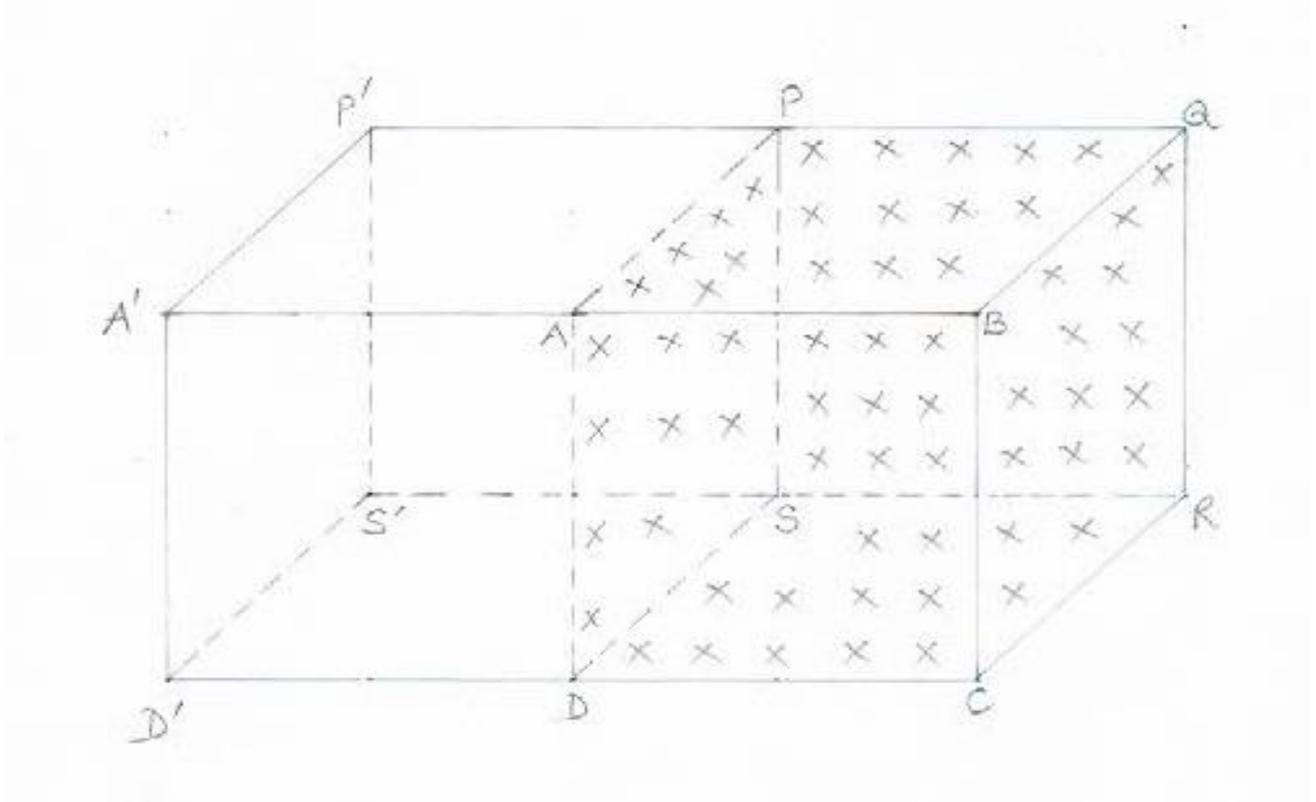
The direction of flow of current in the magnetic field coils.



In the horizontally lying semicircular coils the current (I) flows in the clockwise direction while in the vertically erected semicircular coils the current (I) flows in the anticlockwise direction.

The wire that supply the current (I) in the horizontally lying coils is above to the wire (&) that supply the current in vertically erected coils.

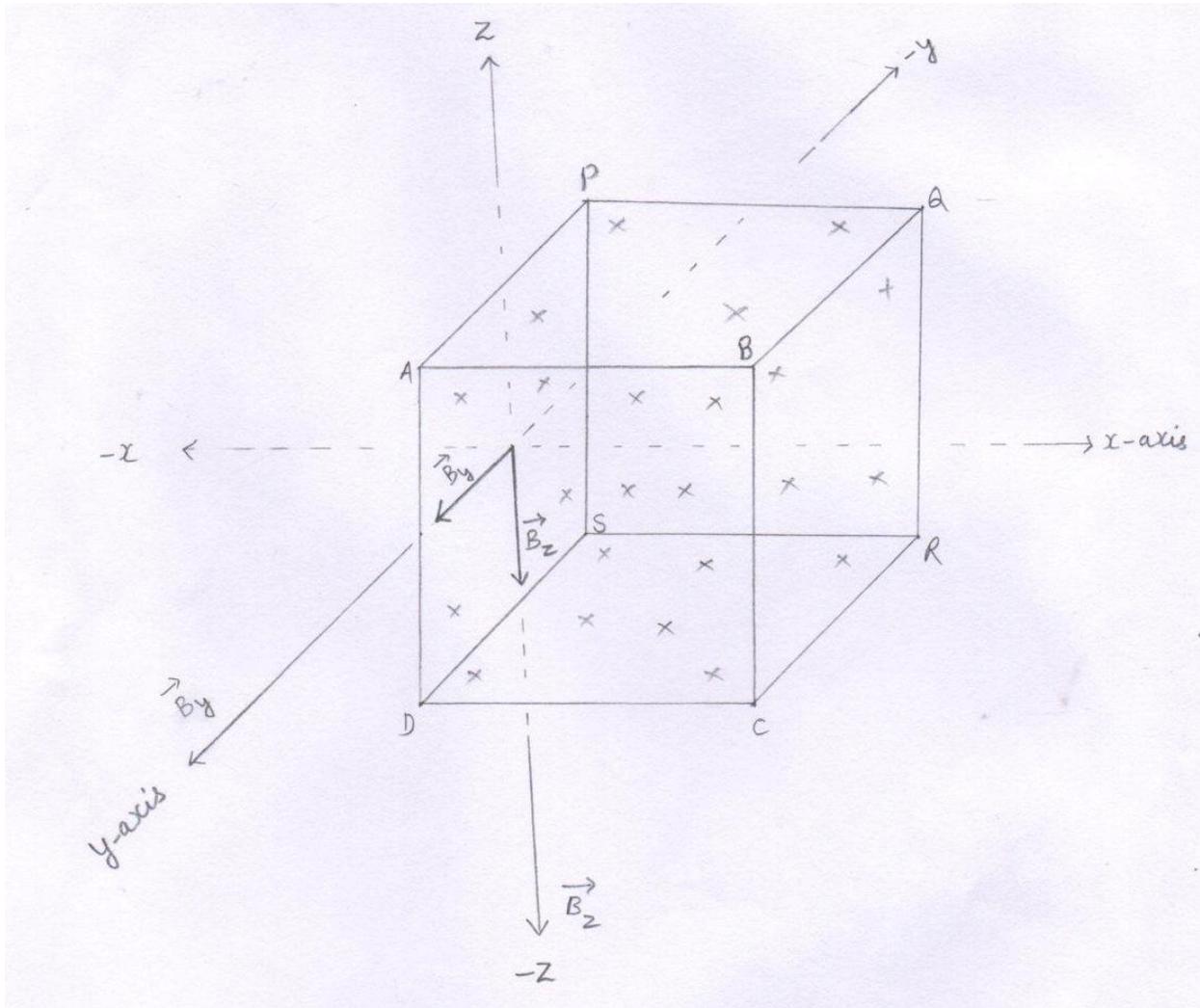
The uniform magnetic fields [B_y and B_z] are applied within into the main tokamak only.



we have denoted the presence of two uniform magnetic fields by the [x] sign.

Two uniform magnetic field are applied within into the main tokamak.

The direction of the uniform magnetic fields applied within into the main tokamak.



where

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

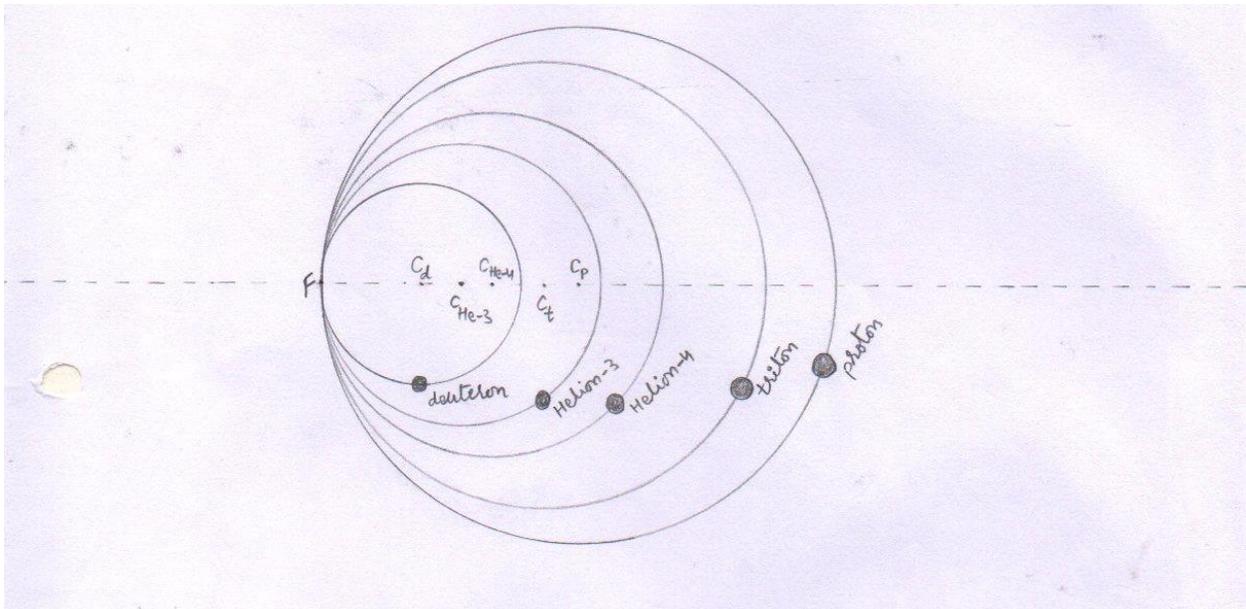
Center of fusion (F) : -center of fusion is actually a point where two charged particles fuse .

For the VBM fusion reactor –The center of fusion is a point from where a charged particle (either it is injected or produced) undergoes to a confined circular path and passes from this point by time and again and thus available for another injected particle (reaching at this point ' F ') for fusion

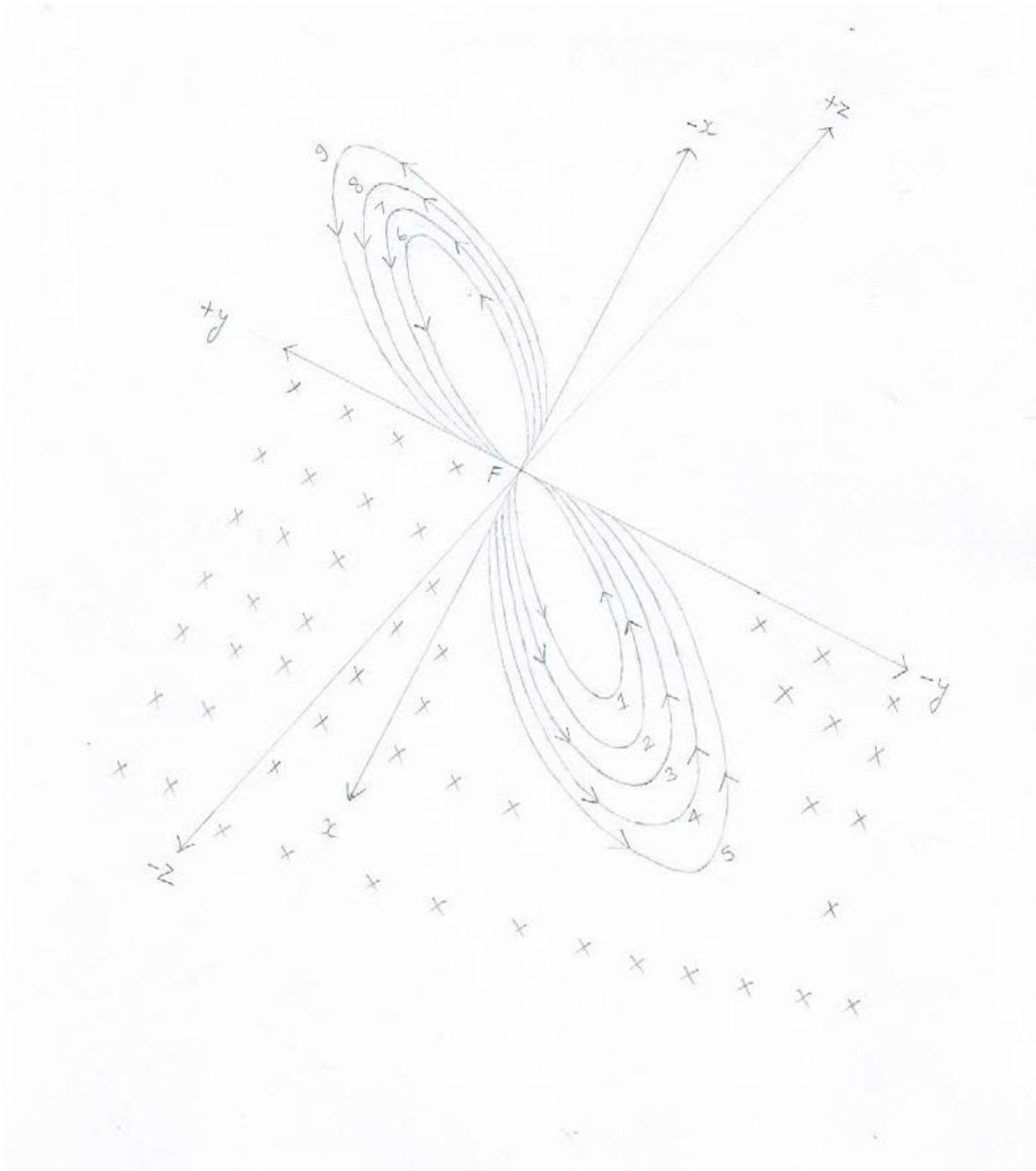
3. Number of centers of fusion (F) : As the point 'F' is acting as a center of fusion , the total no.of centers of fusion are equal to number of deuterons that an injected bunch contains.

4. Nature of center of fusion : As the magnetic field is tangential in nature so the point F (the center of fusion) that is located within into the magnetic fields is a tangential point of a number of circular orbits (followed or to be followed by the charged particles of different radii.

The center of fusion (The point 'F') is the tangential point of all the circular orbits of different radii followed by the various charged particles.



If we denote the positive x, y and z -axes as shown below then path of the confined and not confined particles will lie in the planes as shown below.



For +x, -y, -z axes

The denoted numbers represents the circular orbit of the particles described as below.

1st orbit represents the circular orbit of Li-6 (produced due to 4th fusion reaction) .

2nd orbit represents the circular orbit of Helium-4 (a by product of 3rd fusion reaction)

3rd orbit represents the circular orbit of injected deuteron.

4th orbit represents the circular orbit of Helium-4 (a by product of 8th fusion reaction) .

5th orbit represents the circular orbit of proton (a by product of 2nd fusion reaction).

Whereas, for -x, +y and -z axes

6th orbit represents the circular orbit of helion -3(a by product of first fusion reaction).

7th orbit represents the circular orbit of be-9 (a by product of 11th fusion reaction).

8th orbit represents the circular orbit of be -7(a by product of 10th fusion reaction).

9th orbit represents the circular orbit of triton (a by product of 2nd fusion reaction).

Here,

The radius of the circular orbit to be followed by the triton is more than the radius of the circular orbit to be followed by the helion -3.

'F' is the centre of fusion or the point of injection of deuteron (s).

Center of fusion (F) is a platform where the fusion is a certainty : -

From the point ' F ' [The center of fusion] the deuteron of earlier bunch will undergo to confined circular path and will pass through this point by time and again until it fuses with the deuteron of later injected bunch .

Similarly , the point ' F ' also governs the produced charged particle to go through it and tends them to be fused with the injected deuterons thus available as a platform where the fusion is a certainty .

Or , within into the tokamak , the point ' F ' [the center of fusion] is the only and only point where the fusion reactions occur .

Center of fusion in the view of magnetic fields :-

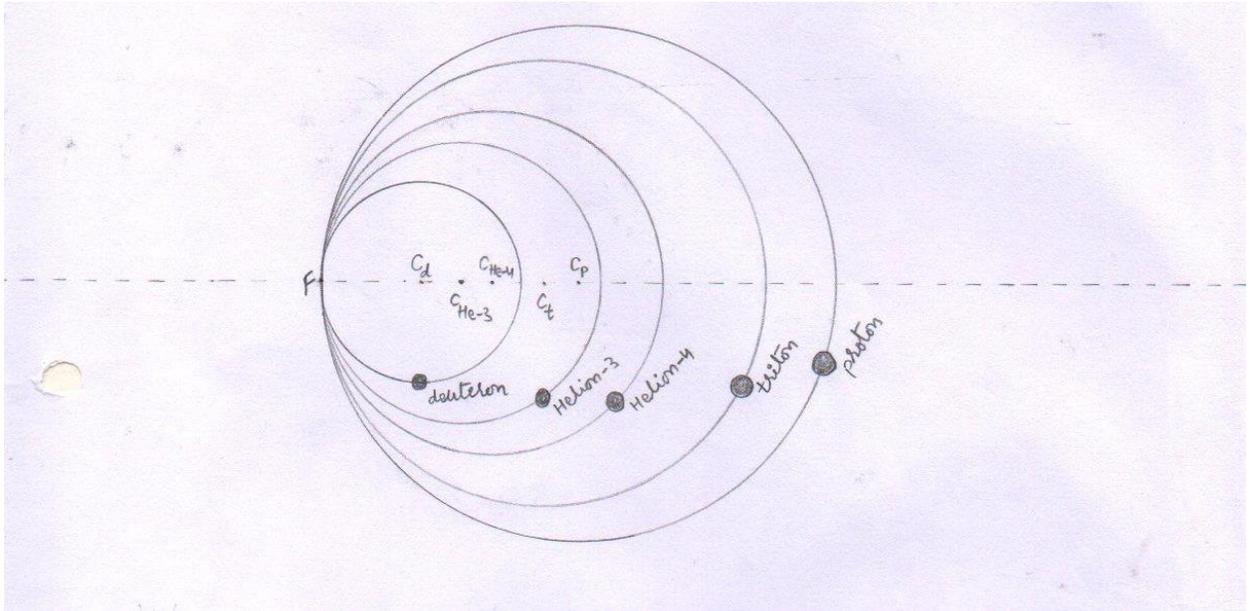
By the view of magnetic fields the center of fusion is a point where the two uniform magnetic fields are perpendicular . But within into the region covered – up by the main tokamak , at each and every point the ratio of two perpendicular magnetic fields [\vec{B}_x and \vec{B}_z] is constant . so , the each and every point within into the region covered – up by the main tokamak can act as a center of fusion .

Note : that is why. if we use the lithium blanket as an inner liner of the main tokamak then the triton produced due to lithium an neutron reaction will also undergo to a confined circular path and may interrupt the confined path (s) followed by the useful plasma and thus the produced triton may be an obstacle to the steady state VBM-fusion reactor.

7. Center of plasma :-

center of plasma is the center of the circular orbit followed by the charged particles.

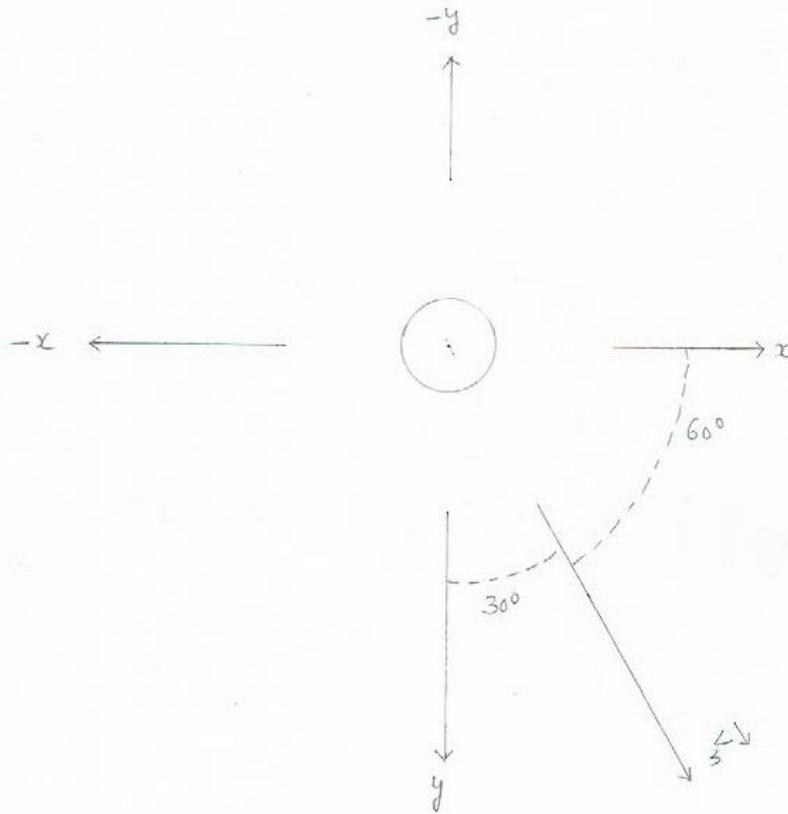
Thus the center of plasma [C_{pm}] differs particle by particles but each particle will have a common center of fusion (the point ' F ').



VBM plasma : RF linac injects the bunches of deuterons into the tokamak at point F . such that each deuterons makes angle 30° with the x -axis , 60° angle with the y-axis and the 90° angle with the z-axis . RF linac injects each proton with 153.6keV energy .

Confinement of protons of 1st bunch of deuterons : -

As the deuterons (s) of first bunch reaches at point F into the tokamak , it experiences a centripetal force due to magnetic fields and hence it follows a confined circular orbit passing through the point of injection (F) by time and again.



v_d = velocity of the deuteron

velocity of the injected deuteron

$$K.E = \frac{1}{2} m_d v^2 = 0.1536 \text{ Mev}$$

$$\begin{aligned}
 &= \left(\frac{2 \times 0.1536 \times 1.6 \times 10^{-13}}{3.3434 \times 10^{-27}} \right)^{1/2} \text{m/s} \\
 &= \left(\frac{0.49152 \times 10^{14}}{3.3434} \right)^{1/2} \text{m/s} \\
 &= [0.14701202368 \times 10^{14}]^{1/2} \text{m/s} \\
 &= 0.3834 \times 10^7 \text{m/s}
 \end{aligned}$$

Components of the velocity of deuteron at point F :-

As the deuteron is injected at point F making angle 30° with x-axis, 60° angle with y-axis and 90° angle with z-axis.

so

$$v_y = V \cos 30^\circ = v \times \frac{\sqrt{3}}{2} = 0.3834 \times 0.866$$

$$= 0.3320 \times 10^7 \text{m/s}$$

$$v_x = V \cos 60^\circ = v \times 0.5 = 0.3834 \times 10^7 \times 0.5 = 0.1917 \times 10^7 \text{m/s}$$

$$v_z = V \cos 90^\circ = v \times 0 = 0 \text{m/s}$$

Components of momentum of deuteron at point F :-

$$p_y = mv \cos 30^\circ = 3.3434 \times 10^{-27} \times 0.3320 \times 10^7 \text{kg m/s}$$

$$= 1.1100 \times 10^{-20} \text{kg m/s}$$

$$\vec{p}_x = mv \cos 60^\circ = 3.3434 \times 10^{-27} \times 0.1917 \times 10^7 \text{ kg m/s}$$

$$= 0.6409 \times 10^{-20} \text{ kg m/s}$$

$$\vec{p}_z = mv \cos 90^\circ = m \times 0 = 0 \text{ kgm/s}$$

The forces acting on the deuteron

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$1.001 \times 10^{-1} \text{ Tesla} \quad \vec{v}_x = 0.1917 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 1.6 \times 10^{-19} \times 0.1917 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 0.3070 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to - y-axis,

so,

$$\vec{F}_y = -0.3070 \times 10^{-13} \text{ N}$$

$$2 F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 1.6 \times 10^{-19} \times 0.1917 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N}$$

$$= 0.3071 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_z is according to -Z- axis,

so,

$$\vec{F}_z = -0.3071 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = 0.3320 \times 10^7$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_x = 1.6 \times 10^{-19} \times 0.3320 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

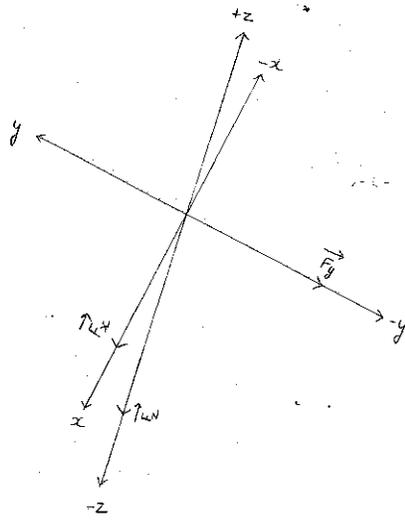
$$= 0.5317 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x axis,

so,

$$\vec{F}_x = 0.5317 \times 10^{-13} \text{ N}$$

The forces acting on the deuteron



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 0.5317 \times 10^{-13} \text{ N}$$

$$F_y = 0.3070 \times 10^{-13}$$

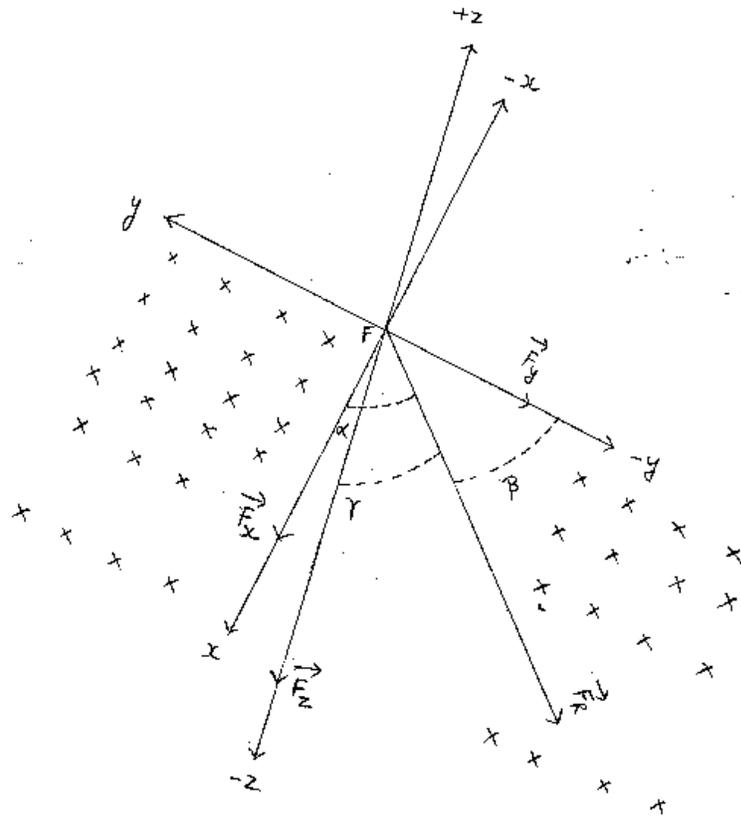
$$= F_z = 0.3071 \times 10^{-13} \text{ N}$$

$$F_R^2 = (0.5317 \times 10^{-13})^2 + (0.3070 \times 10^{-13})^2 + (0.3071 \times 10^{-13})^2 \quad \text{N}^2$$

$$= (0.28270489 \times 10^{-26}) + (0.094249 \times 10^{-26}) + (0.09431041 \times 10^{-26})^2 \quad \text{N}^2$$

$$F_R^2 = 0.4712643 \times 10^{-26} \text{ N}^2$$

$$F_R = 0.6864 \times 10^{-13} \text{ N}$$



Radius of the circular path :

Resultant force acts as a centripetal force on the deuteron . so, the deuteron follows a confined circular path.

The radius of the circular orbit obtained by the deuteron is –

$$r = mv^2 / F_R$$

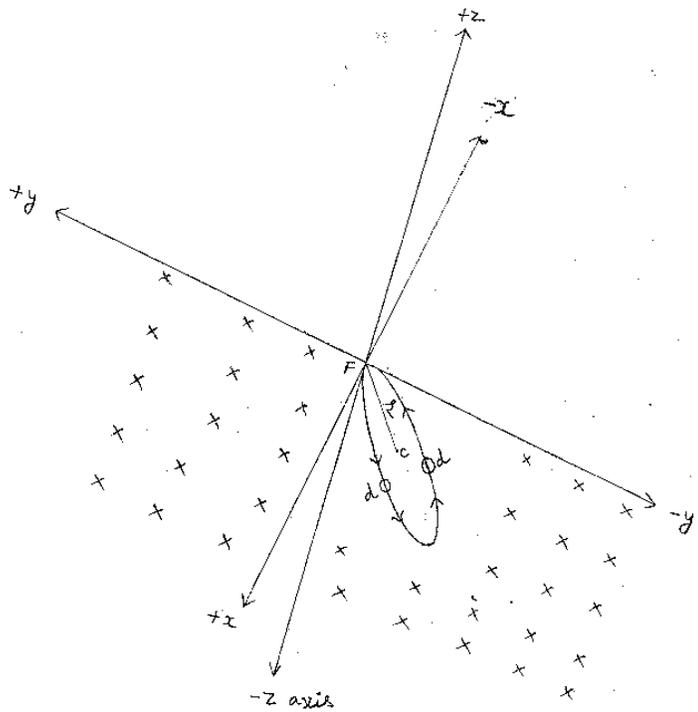
$$mv^2 = 2 \times 153.6 \text{ Kev} = 2 \times 0.1536 \text{ Mev} = 2 \times 0.1536 \times 1.6 \times 10^{-13} \text{ J}$$

$$mv^2 = 0.4915 \times 10^{-13} \text{ J}$$

$$r = \frac{0.4915 \times 10^{-13} \text{ J}}{0.6864 \times 10^{-13} \text{ N}}$$

$$= 0.7160 \text{ m}$$

The confined deuteron follows the circular orbit as shown below :-



The circular orbit followed by the confined deuteron lies in the IV (down) quadrant or in the plane made up of positive x -axis, negative y -axis and the negative z -axis.

\vec{F}_r = The resultant force acting on the deuteron when the deuteron is at point ' F '.

C_d = center of the circular orbit followed by the deuteron.

The plane of the circular orbit followed by the confined deuteron makes angles with positive x , y and z -axes as follows :-

1 with x - axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = 0.5317 \times 10^{-13} \text{ N}$$

$$F_r = 0.6864 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7746$$

$$\alpha = 39.23 \text{ degree } [\because \cos(39.23) = 0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r}$$

$$= \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = -0.3070 \times 10^{-13} \text{ N}$$

$$F_r = 0.6864 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4472$$

$$\beta = 243.43 \text{ degree } [\because \cos(243.43) = -0.4472]$$

3 with y- axis

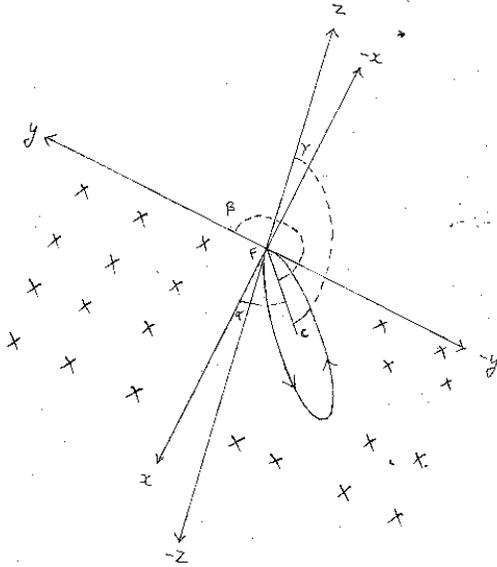
$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{F_z}{F_r}$$

$$\frac{F_z}{F_r} = -0.3071 \times 10^{-13} \text{ N}$$

$$F_r = 0.6864 \times 10^{-13} \text{ N}$$

$$\cos \gamma = -0.4474$$

$$\gamma = 243.42 \text{ degree}$$



The plane of the circular orbit followed by the confined deuteron makes angles with positive x, y and z axes as follows :-

Where,

$\alpha = 39.23$ degree

$\beta = 243.43$ degree

$\gamma = 243.42$ degree

All the angles are in degree.

The direction cosines of the line P_1P_2

The line P_1P_2 is the diameter of the circle followed (or to be followed) by the particle .

The points $P_1 (x_1 y_1 z_1)$ and $P_2 (x_2 y_2 z_2)$ make the line P_1P_2 .

The particle starts its circular motion from the point 'F' (- the center of fusion where the particle is either injected or produced).

So, we have denoted the Cartesian coordinates for the

Point 'F' as $(0, 0, 0)$.

Here the point F $(0,0,0)$ and the point $P_1 (x_1 y_1 z_1)$ are the same .

So , the direction cosines of the line P_1P_2 are : -

$$l = \cos \alpha = x_2 - x_1 / d$$

where ,

$$d = 2 \times \text{radius of the circle}$$

$\cos \alpha$ = cos component of the angle that make the resultant force (\vec{F}_r) [acting on the particle when the particle is at point F] with the positive x - axis .

$$2. \quad m = \cos \beta = y_2 - y_1 / d$$

Where ,

$\cos \beta$ = cos component of the angle that make the resultant force (\vec{F}_r) [acting on the particle when the particle is at point F] with the positive y - axis .

$$3. \quad n = \cos \gamma = z_2 - z_1 / d$$

Where ,

$\cos \gamma$ = cos component of the angle that make the resultant force (\vec{F}_r) [acting on the particle when the particle is at point F] with the positive z - axis .

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the deuteron

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$d = 2 \times r$$

$$= 2 \times 0.7160 \text{ m}$$

$$= 1.432 \text{ m}$$

$$\cos \alpha = 0.7746$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 1.432 \times 0.7746 \text{ m}$$

$$x_2 - x_1 = 1.1092 \text{ m}$$

$$x_2 = 1.1092 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

d

$$\cos \beta = -0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 1.432 \times (-0.4472) \text{ m}$$

$$y_2 - y_1 = -0.6403 \text{ m}$$

$$y_2 = -0.6403 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = -0.4474$$

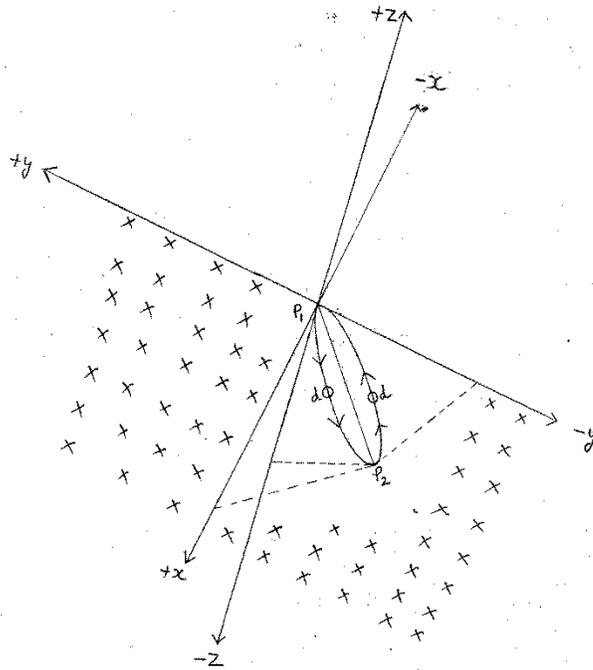
$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 1.432 \times (-0.4474) \text{ m}$$

$$z_2 - z_1 = -0.6406 \text{ m}$$

$$z_2 = -0.6406 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1(x_1, y_1, z_1)$ and $p_2(x_2, y_2, z_2)$



The cartesian coordinates of the points $P_1 (0,0,0)$ and $P_2 (3.66 \times 10^{-2}, 6.43 \times 10^{-2}, -6.43 \times 10^{-2})$ where the points $P_1(x_1, y_1, z_1)$ and $P_2(x_2, y_2, z_2)$ are located on the circumference of the circle obtained by the deuteron.

The line ____ is the diameter of the circle .

P_1P_2

Conclusion :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the deuteron are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the deuteron lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the deuteron to undergo to a circular orbit of radius of 0.7160 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.1092 \text{ m}, -0.6403 \text{ m}, -0.6406 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak. And uninterruptedly goes on completing its circle until it fuses with the deuteron of later injected bunch (that reaches at point "F") at point "F"

Time period of the confined particles

resultant force

$$F_r^2 = F_x^2 + F_y^2 + F_z^2$$

where, $F_x = qV_y B_z$

$$F_y = qV_x B_z$$

$$F_z = qV_x B_y$$

For the VBM Fusion reactor

$$B_y = B_z = B = 1 \text{ Tesla}$$

so,

$$F_x = qV_y B, \quad F_y = qV_x B$$

and $F_z = qV_x B$

hence $F_y = F_z = F = qV_x B$

putting the values

$$F_r^2 = F_x^2 + 2F^2$$

$$q^2 V_y^2 B^2 + 2 q^2 V_x^2 B^2$$

$$F_r^2 = q^2 B^2 (V_y^2 + 2 V_x^2)$$

$$F_r = Bq (V_y^2 + 2 V_x^2)^{1/2}$$

2- Radius of the particle

$$R = mv^2 / F_R$$

$$\underline{mv^2}$$

$$Bq (2V_x^2 + V_y^2)^{1/2}$$

3- Time period of the particle

$$T = 2\pi r / V$$

$$= 2\pi / V$$

$$\frac{mv^2}{Bq (2V_x^2 + V_y^2)^{1/2}}$$

$$Bq (2V_x^2 + V_y^2)^{1/2}$$

$$= 2\pi m / Bq \times \underline{V}$$

$$(2V_x^2 + V_y^2)^{1/2}$$

$$\text{where, } V = (V_x^2 + V_y^2 + V_z^2)^{1/2}$$

$$\text{but here } V_z = 0$$

$$\text{so, } V = (V_x^2 + V_y^2)^{1/2}$$

$$T = 2\pi m / Bq \times \underline{V}$$

$$(2V_x^2 + V_y^2)^{1/2}$$

$$T = 2\pi m / Bq \times (V_x^2 + V_y^2 / 2V_x^2 + V_y^2)^{1/2}$$

$$\text{here, } 2V_x^2 + V_y^2 > V_x^2 + V_y^2$$

so, the time period of the confined particle depends on the x-component of the final velocity of the particle while in the cyclotron it does not depend on the velocity of the particle.

Time period of the particle

For deuteron

$$T = 2\pi m / Bq \times \underline{V}$$

$$(2V_x^2 + V_y^2)^{1/2}$$

$$\begin{aligned} (2V_x^2 + V_y^2)^{1/2} &= 2 \times (0.271 \times 10^7)^2 + (0.1565 \times 10^7)^2 \text{ m}^2/\text{s}^2 \\ &= 2 \times 0.073441 \times 10^{14} + 0.02449225 \times 10^{14} \text{ m}^2/\text{s}^2 \end{aligned}$$

$$= 0.17137425 \text{ m}^2/\text{s}^2$$

$$(2V_x^2 + V_y^2)^{1/2} = 0.4139 \times 10^7 \text{ m}^2/\text{s}^2$$

put the value

$$V = 0.3130 \times 10^7 \text{ B} = 1 \text{ Tesla}$$

$$q = 1.6 \times 10^{-19} \text{ C}, \quad m = 3.3434 \times 10^{-27} \text{ kg}$$

$$T = 2 \times 3.14 \times 3.3434 \times 10^{-27} \times 0.3130 \times 10^7 \text{ s}$$

$$\begin{aligned} & 1 \times 1.6 \times 10^{-19} \times 0.4139 \times 10^7 \\ &= \frac{6.571920776 \times 10^{-20}}{0.66224 \times 10^{-12}} \text{ s} \\ &= 9.92 \times 10^{-8} \text{ second} \end{aligned}$$

or

$2\pi r/v$

$$r = 4.947 \times 10^{-2} \text{ m}$$

$$v = 0.3130 \times 10^7 \text{ m/s}$$

$$T = \frac{2 \times 3.14 \times 4.947 \times 10^{-2}}{0.3130 \times 10^7} \text{ s}$$

$$\begin{aligned} &= \frac{31.06716 \times 10^{-2}}{0.3130 \times 10^7} \text{ s} \\ &= 9.92 \times 10^{-8} \text{ second} \end{aligned}$$

Time of confinement of deuteron (s) :-

The time of confinement of plasma is the time for which the plasma can exist before it radiates away its energy through cyclotron radiations.

Power loss by cyclotron radiations :

By the Larmor formula, power loss is given as-

$$P = \frac{2e^2 a^2}{3C^3}$$

expression for acceleration using Lorentz force :

$$ma = \frac{e v B}{c}$$

by substitution

$$P = \frac{2e^4 v^2 B^2}{3c^5 m^2}$$

$$\frac{dE}{dt} = \frac{-2e^2v^2B^2}{3c^5m^2} = \frac{-4e^4EB^2}{3c^5m^3} [\because \frac{1}{2}mv^2 = E]$$

$$\frac{dE}{E} = \frac{-4e^4EB^2}{3c^5m^3} dt$$

$$E = E_0 e^{\frac{-4e^4EB^2}{3c^5m^3} t} = E_0 e^{-\frac{t}{t_0}}$$

$$t_0 = \frac{3c^5m^3}{-4e^4EB^2} =$$

Time of confinement of deuteron

$$t_e = \frac{3c^5m^3}{4e^4B^2}$$

$c = 3 \times 10^{10}$ cm/s
 $m = 3.3434 \times 10^{-24}$ gram
 $e = 4.8 \times 10^{-10}$ esu
 $B = 1 \times 10^{-1}$ Tesla = 10^3 Gauss

$$t_e = \frac{3 \times (3 \times 10^{10})^5 \times (3.3434 \times 10^{-24})^3}{4 \times (4.8 \times 10^{-10})^4 \times (10^3)^2}$$

$$= \frac{3 \times 243 \times 10^{50} \times 37.3736 \times 10^{-72}}{4 \times 530.84 \times 10^{-40} \times 10^6}$$

$$= \underline{272445.3544 \times 10^{-22}}$$

$$2123.36 \times 10^{-34}$$

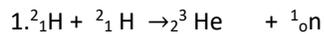
$$= 12.83 \times 10^{12} \text{ seconds}$$

$$= 1.283 \times 10^{13} \text{ seconds}$$

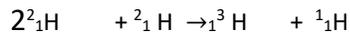
Conclusion : Time of confinement (t_e) of the deuteron is = 1.283×10^{11} seconds. Thus we do not expect to see emission from deuterons (plasma) . As each and every deuteron injected into the tokamak at the center of fusion (point F) is with enough energy required for fusion, so, in the VBM fusion reactor there is no need of solenoid (primary transformer) to heat the plasma (secondary transformer) while in the thermonuclear fusion reactors there is a solenoid to heat the plasma.

The fusion reactions :-

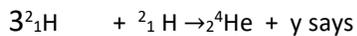
In the VBM fusion reactor based on D-D cycle, the following fusion reactions occurs .



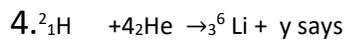
[injected] [confined][not confined]



[injected] [confined]



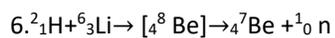
[injected] [confined]



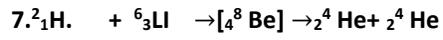
[injected][confined][confined]



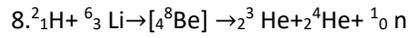
[injected] [confined] [not confined] [not confined]



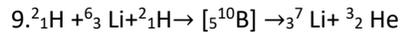
[injected] [confined] [not confined]



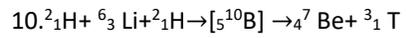
[injected] [confined][not confined][not confined]



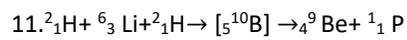
[injected] [confined][not confined] [not confined]



[injected] [confined] [confined] [not confined] [not confined]



[injected] [confined] [confined] [not confined] [not confined]



[injected][confined] [confined] [not confined] [not confined]

How fusion occurs

1 Formation of compound nucleus : -

As the deuteron of Nth bunch reaches at point ' F ' , it fuses with the deuteron of first bunch(confined deuteron passing through the point ' F '] to form a compound nucleus .

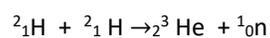
2 The splitting of compound nucleus : -

The compound nucleus splits into three particles . out of three particles , two are finite nuclei and third one is reduced mass. Due to splitting of compound nucleus, all the three particles separates from each other with a velocity(\vec{v}_{cn}) equal to the velocity of the compound nucleus.

Propulsion of the particles : -

Reduced mass converts into energy and act as a propellant for both the produced final nuclei.

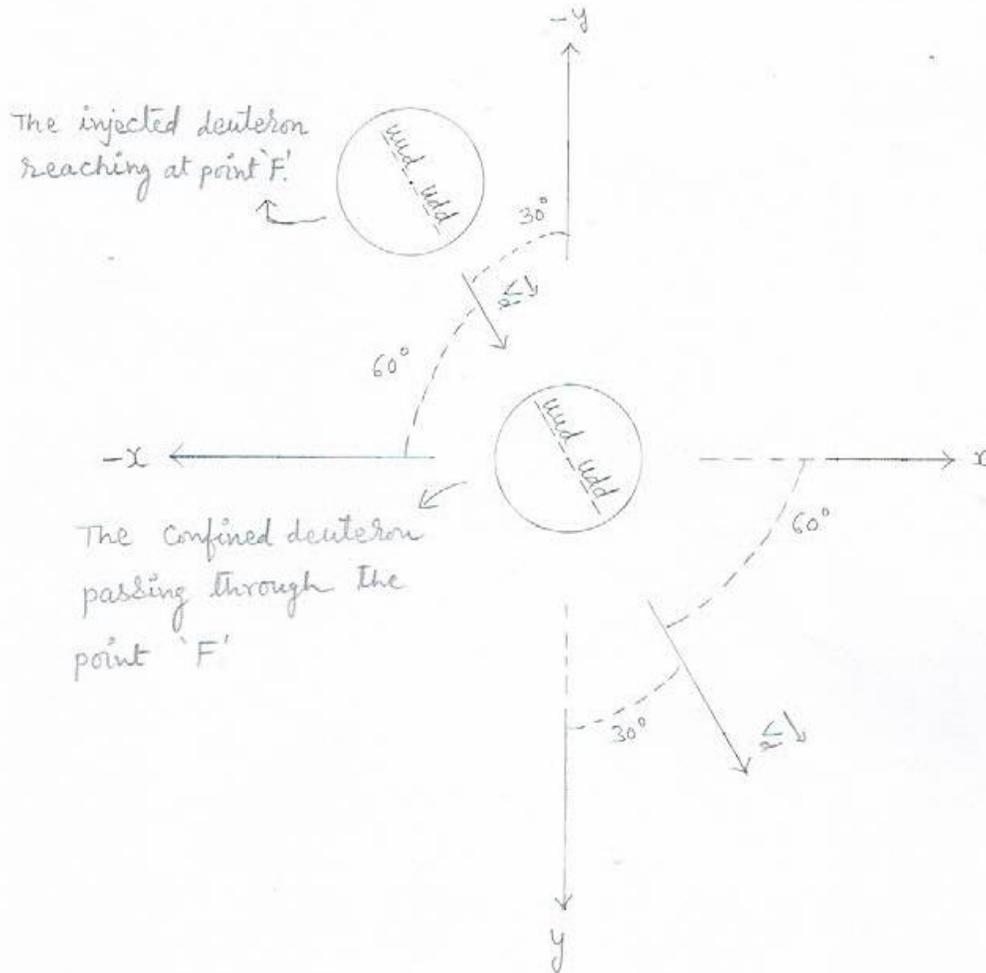
For fusion reaction



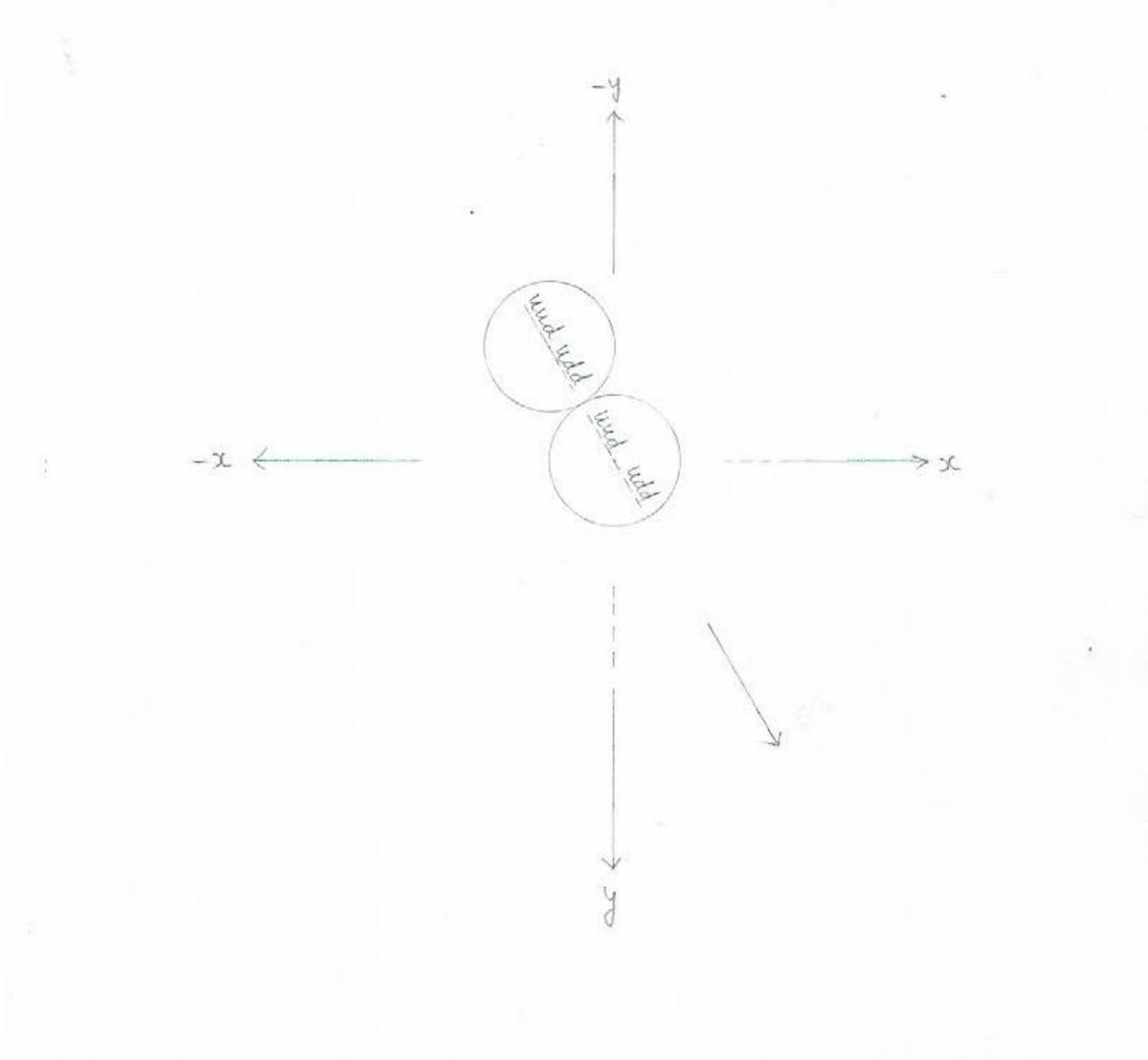
interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined deuteron] with the confined deuteron passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined deuteron.

interaction of nuclei (1)



interaction of nuclei (2)

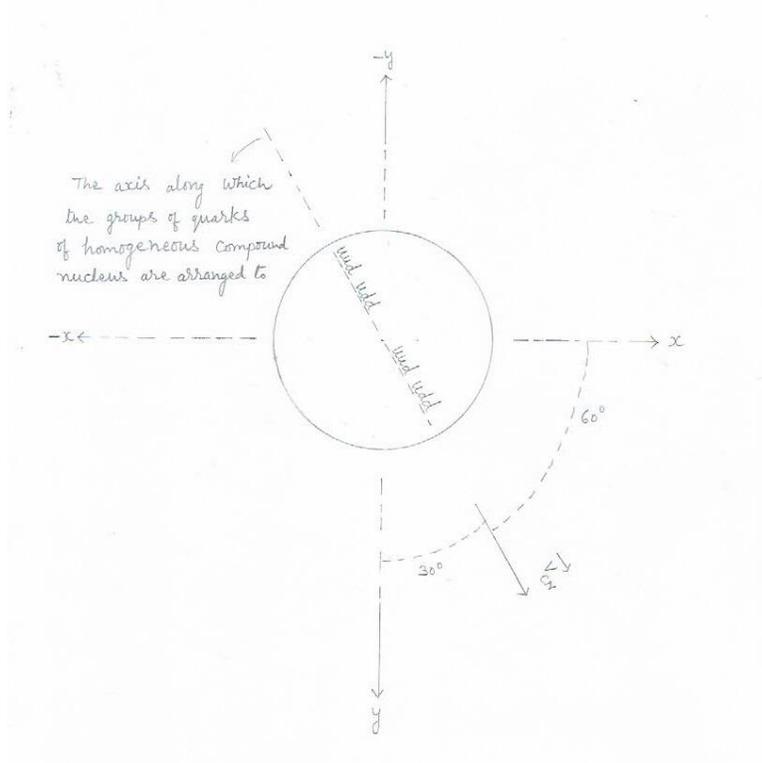


Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron) behave like a liquid and form a homogeneous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 4 groups of quarks surrounded by the gluons.

Formation of homogenous compound nucleus



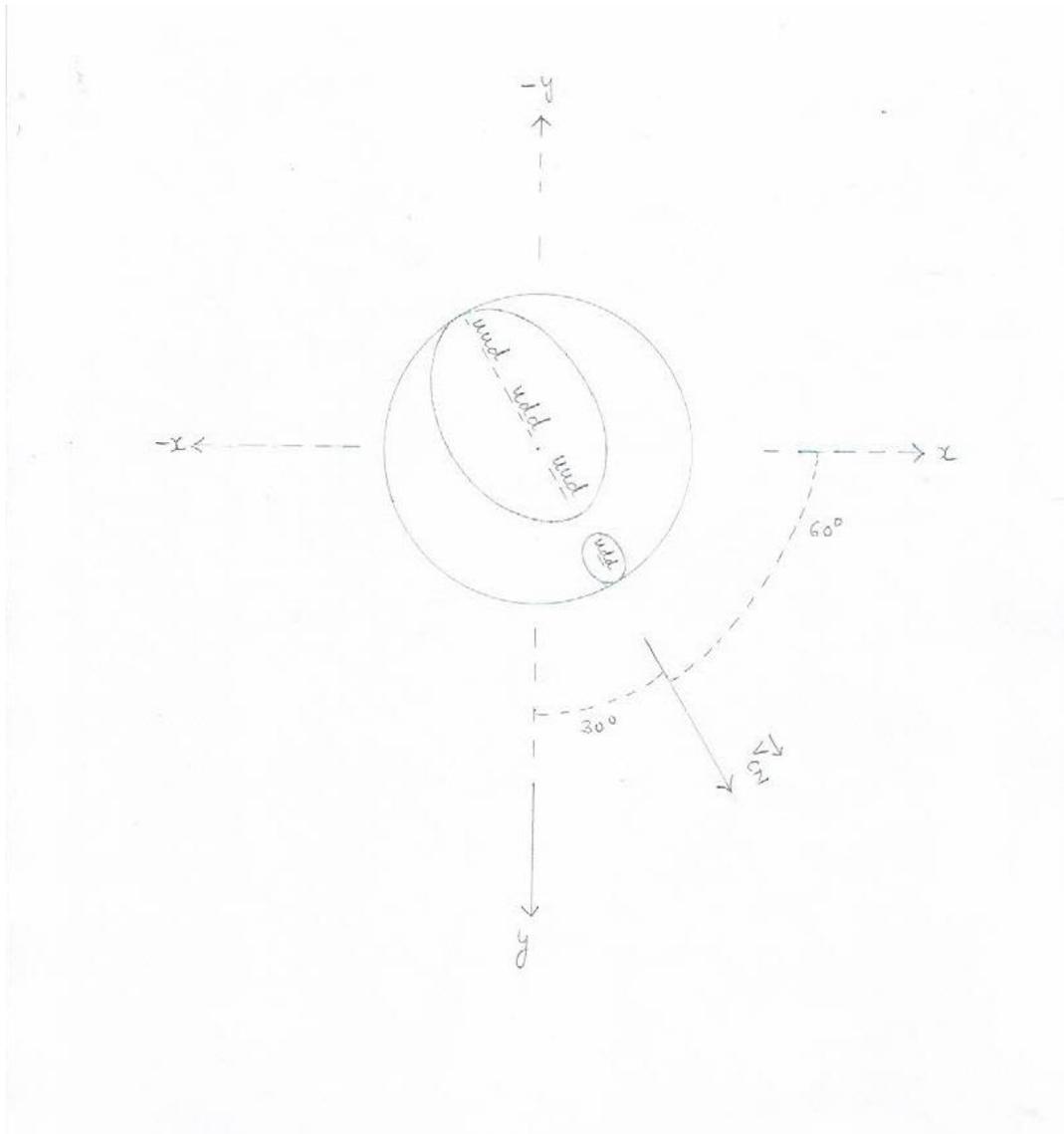
Formation of homogenous compound nucleus

3 Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the helion-3) than the reactant one (the deuteron) includes the other two (nearby located) groups of quarks with their surrounding gluons and rearrange to form the 'A' lobe of the heterogeneous compound nucleus.

While, the remaining groups of quarks to become a stable nucleus (neutron) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe 'A'] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus.

Thus, due to formation of two dissimilar lobes within into the homogeneous compound nucleus, the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.



Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the helium-3 nucleus and the smaller one is the neutron while the remaining space represents the remaining gluons .

Within into the homogenous compound nucleus ,the greater nucleus is the lobe 'A ' while the smaller one is the lobe 'B' .

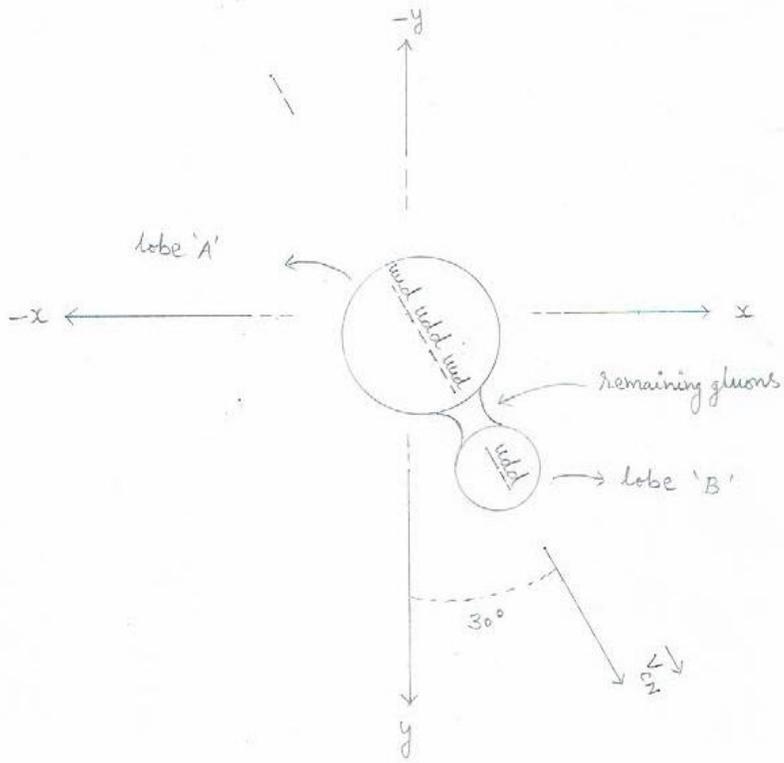
Final stage of the heterogeneous compound nucleus : -

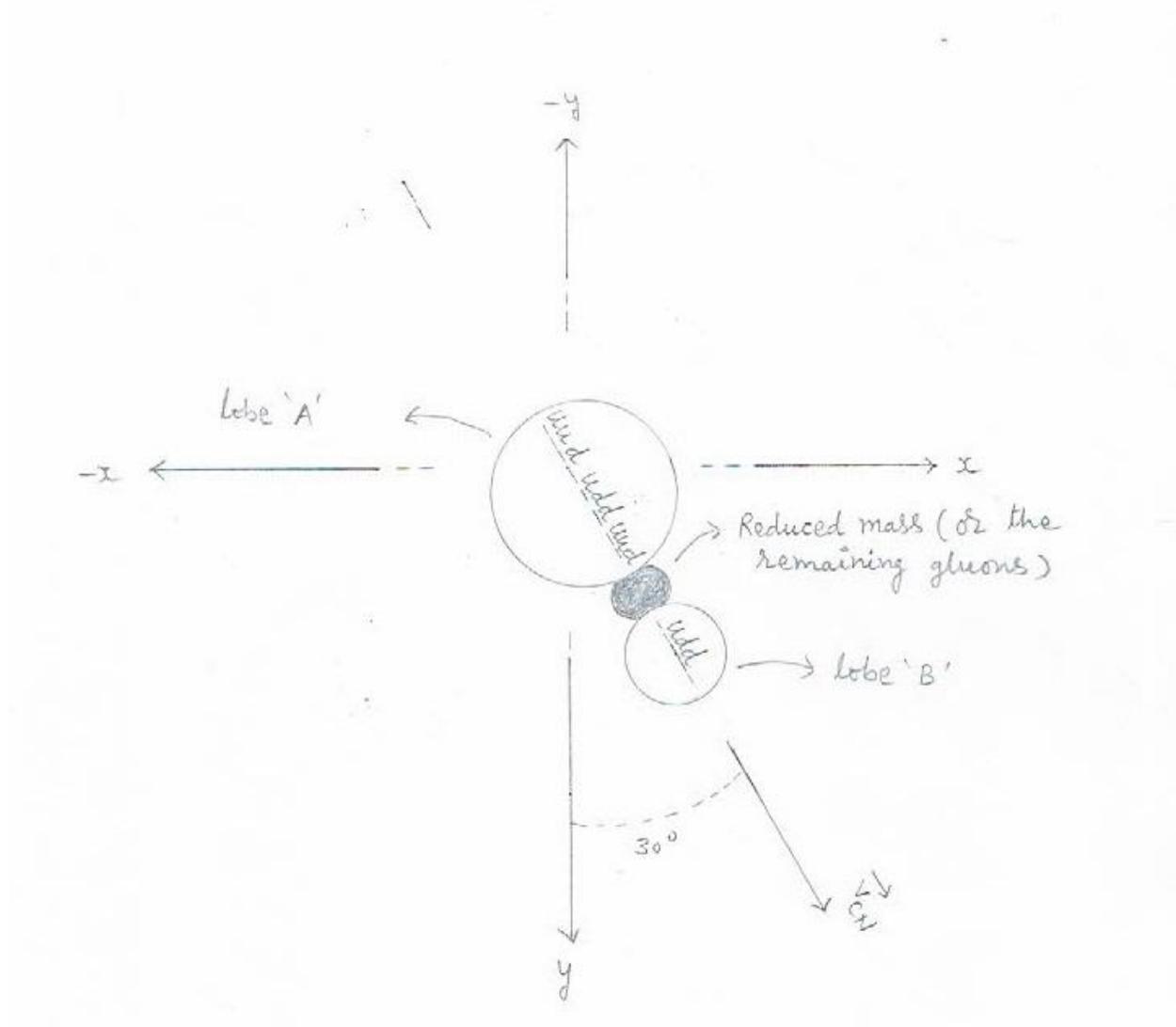
The process of formation of lobes creates void (s) between the lobes . so, the remaining gluons (or the mass) that are not involved in the formation of any lobe) rearrange to fill the void (s) between the lobes . Thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight.

Heterogenous compound nucleus





Final stage of a heteronuclear compound nucleus.

Formation of compound nucleus :

As the deuteron of n^{th} bunch reaches at point F, it fuses with the confined deuteron of 1^{st} bunch to form a compound nucleus.

Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron of 1^{st} bunch, the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves) its energy equal to 5.0622 keV.

so, just before fusion,

the kinetic energy of n^{th} deuteron is –

$$\begin{aligned} E_b &= 153.6 \text{ keV} - 5.0622 \text{ keV} \\ &= 148.5378 \text{ keV} \\ &= 0.1485378 \text{ MeV} \end{aligned}$$

velocity of n^{th} deuteron just before fusion

$$\begin{aligned} E_b &= \frac{1}{2} m_d V_b^2 = 0.1485378 \text{ MeV} \\ v &= \left(\frac{2 \times 0.1485378 \times 1.6 \times 10^{-13} \text{ J}}{3.3434 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}} \text{ m/s} \\ v &= \left(\frac{0.47532096 \times 10^{14}}{3.3434} \right)^{\frac{1}{2}} \text{ m/s} \\ &= [0.14216694382 \times 10^{14}]^{\frac{1}{2}} \text{ m/s} \end{aligned}$$

$$= 0.3770 \times 10^7 \text{ m/s}$$

Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron of 1^{st} bunch, the confined deuteron (of earlier injected bunch) loses (radiates its energy in the form of electromagnetic waves) its energy equal to 5.0622 keV.

so, just before fusion,

the kinetic energy of n^{th} deuteron is –

$$\begin{aligned} E_b &= 153.6 \text{ keV} - 5.0622 \text{ keV} \\ &= 148.5378 \text{ keV} \end{aligned}$$

$$E_b = 0.1485378 \text{ MeV}$$

Kinetic energy of compound nucleus :- Kinetic energy of compound nucleus is the sum of the kinetic energy of injected deuteron (just before fusion) and kinetic energy of confined deuteron (just before fusion)

$$\begin{aligned} E_{cn} &= \frac{1}{2} m_d V_b^2 + \frac{1}{2} m_d V_b^2 \\ &= m_d V_b^2 = 2 \times 148.5378 \text{ KeV} \end{aligned}$$

Mass of compound nucleus (M) : Twice the mass of a deuteron.

Velocity of compound nucleus :

$$\begin{aligned} V_{cn} &= (2 \times E_{cn} / M)^{1/2} \\ &= (2 \times m_d V_b^2 / 2 \times m_d)^{1/2} \\ &= V_b \end{aligned}$$

Components of velocity of compound nucleus at point F.

$$1 \vec{v}_x = V_{cn} \cos \alpha = V_b \cos \alpha = V_b \cos 60^\circ$$

$$= 0.3770 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 0.1885 \times 10^7 \text{ m/s}$$

$$2 \vec{v}_y = V_{cn} \cos \beta = V_b \cos \beta = V_b \cos 30^\circ$$

$$= 0.3770 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 0.3264 \times 10^7 \text{ m/s}$$

$$3 \vec{v}_z = V_{cn} \cos \gamma = V_b \cos \gamma = V_b \cos 90^\circ$$

$$= v \times 0 = 0 \text{ m/s}$$

4.. Mass of the compound nucleus (M) :

$$M = 2 \times \text{mass of deuteron}$$

$$= 2 \times 2.0135 \text{ amu}$$

$$= 4.027 \text{ amu}$$

$$= 6.6868 \times 10^{-27} \text{ kg}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus , due to its instability , splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – helion-3, neutron and reduced mass (Δm) .

Out of them , the two particles (the helion-3 and neutron) are stable while the third one (reduced mass) is unstable .

According to the law of inertia, each particle that is produced due to splitting of the compound nucleus , has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}).

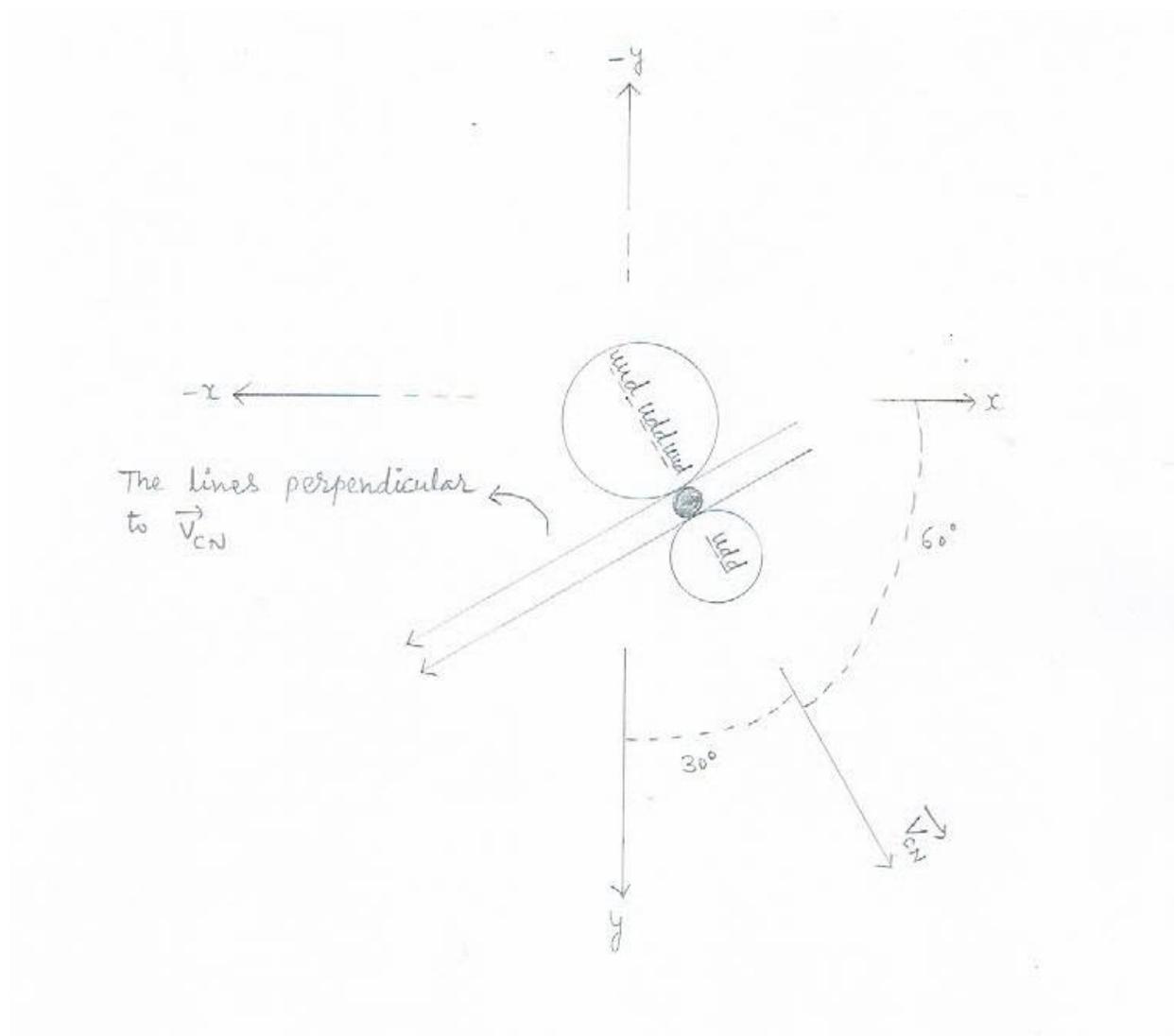
So, for conservation of momentum

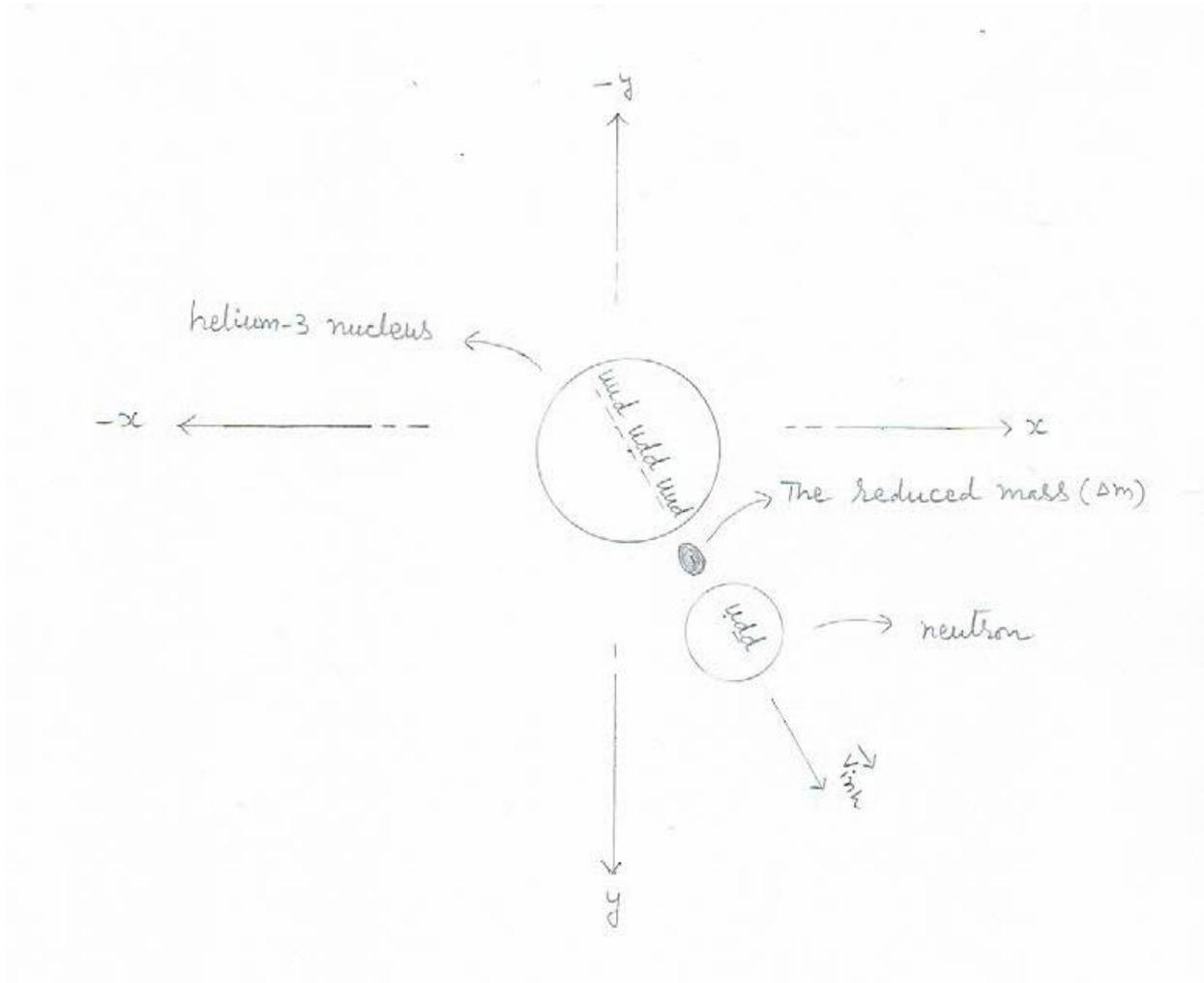
$$M\vec{V}_{cn} = (m_{\text{He-3}} + \Delta m + m_n)\vec{V}_{cn}$$

Where ,

M	= mass of the compound nucleus
\vec{V}_{cn}	= velocity of the compound nucleus
m_{He}	= mass of the helium-3 nucleus
Δm	= reduced mass
m_n	= mass of the neutron

The splitting of the heterogenous compound nucleus





Inherited velocity (\vec{v}_{inh}) of the particles : -

Each particle that is produced due to splitting of the compound nucleus has an inherited velocity (\vec{V}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{CN}).

I . for helium – 3 nucleus

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the helium – 3

$$1 \rightarrow \frac{V_{inh}}{V_x} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1885 \times 10^7 \text{ m/s}$$

$$2 \rightarrow \frac{V_{inh}}{V_y} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.3264 \times 10^7 \text{ m/s}$$

$$3 \rightarrow \frac{V_{inh}}{V_z} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

II . Inherited velocity of the neutron

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the neutron

$$1 \rightarrow \frac{V_{inh}}{V_x} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1885 \times 10^7 \text{ m/s}$$

$$2 \rightarrow \frac{V_{inh}}{V_y} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.3264 \times 10^7 \text{ m/s}$$

$$3 \rightarrow \frac{V_{inh}}{V_z} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and thus acts as a propellant for both the particles. (A like, if we put a bowl on the cracker and put the cracker on fire, the bowl and the earth will have equal and opposite momentum.

Similarly, both the particles ${}^3_2\text{He}$ and ${}^1_0\text{n}$ will have equal and opposite momentum. For this the total energy (E_T) is divided between the particles in inverse proportion to their masses.

Reduced mass

$$\Delta m = [m_d + m_d] - [m_{\text{He-3}} + m_n]$$

$$\Delta m = [2 \times 2.01355] - [3.014932 + 1.00866] \text{ amu}$$

$$\Delta m = [4.0271 - 4.023592] \text{ amu}$$

$$\Delta m = 0.003508 \text{ amu}$$

$$\Delta m = 0.003508 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm) .

$$E_{\text{inh}} = \frac{1}{2} \Delta m V_{\text{inh}}^2$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.003508 \times 1.6605 \times 10^{-27} \times 0.14216694382 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00041406364 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.0002587 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.003508 \times 931 \text{ Mev}$$

$$E_R = 3.265948 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{\text{inh}} + E_R$$

$$E_T = 0.0002587 + 3.265948 \text{ Mev}$$

$$E_T = 3.2662067 \text{ Mev}$$

Increased kinetic energy of the particles :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses. so, the increased kinetic energy (E_{inc}) of the particles :-

1.. For ${}^3_2\text{He}$

$$E_{inc} = \frac{m_n}{m_{\text{He-3}} + m_n} \times E_T$$

$$E_{inc} = \frac{1.00866}{1.00866 + 3.014932} \times 3.2662067 \text{ Mev}$$

$$E_{inc} = \frac{1.00866}{4.023592} \times 3.2662067 \text{ Mev}$$

$$E_{inc} = 0.25068645131 \times 3.2662067 \text{ Mev}$$

$$E_{inc} = 0.818793 \text{ Mev}$$

2.. For ${}^1_0\text{n}$

$$E_{inc} = [E_T] - [\text{increased energy of the helium -3}]$$

$$E_{inc} = [3.2662067 - 0.818793] \text{ Mev}$$

$$E_{inc} = 2.4474137 \text{ Mev}$$

$$\left(\quad \quad \quad \right)$$

6..Increased velocity of the particles .

(1) For helium – 3

$$E_{inc} = \frac{1}{2} m_{He-3} V_{inc}^2$$

$$V_{inc} = \sqrt{2E_{inc}/m_{He-3}}$$

$$= \frac{2 \times 0.818793 \times 1.6 \times 10^{-13}}{5.00629 \times 10^{-27}}^{1/2} \text{ m/s}$$

$$= \frac{2.6201376 \times 10^{-13}}{5.00629 \times 10^{-27}}^{1/2} \text{ m/s}$$

$$= [0.52336912164 \times 10^{14}]^{1/2}$$

$$= 0.7234 \times 10^7 \text{ m/s}$$

For Neutron

$$V_{inc} = \left[\frac{2E_{inc}}{m_n} \right]^{1/2}$$

$$= \left(\frac{2 \times 2.4474137 \times 1.6 \times 10^{-13} \text{ J}}{1.6749 \times 10^{-27} \text{ kg}} \right)^{1/2}$$

$$= \left(\frac{7.83172384 \times 10^{-13}}{1.6749 \times 10^{-27}} \right)^{1/2} \text{ m/s}$$

$$= [4.67593518419 \times 10^{14}]^{1/2} \text{ m/s}$$

$$= 2.1623 \times 10^7 \text{ m/s}$$

7 Angle of propulsion

1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum .

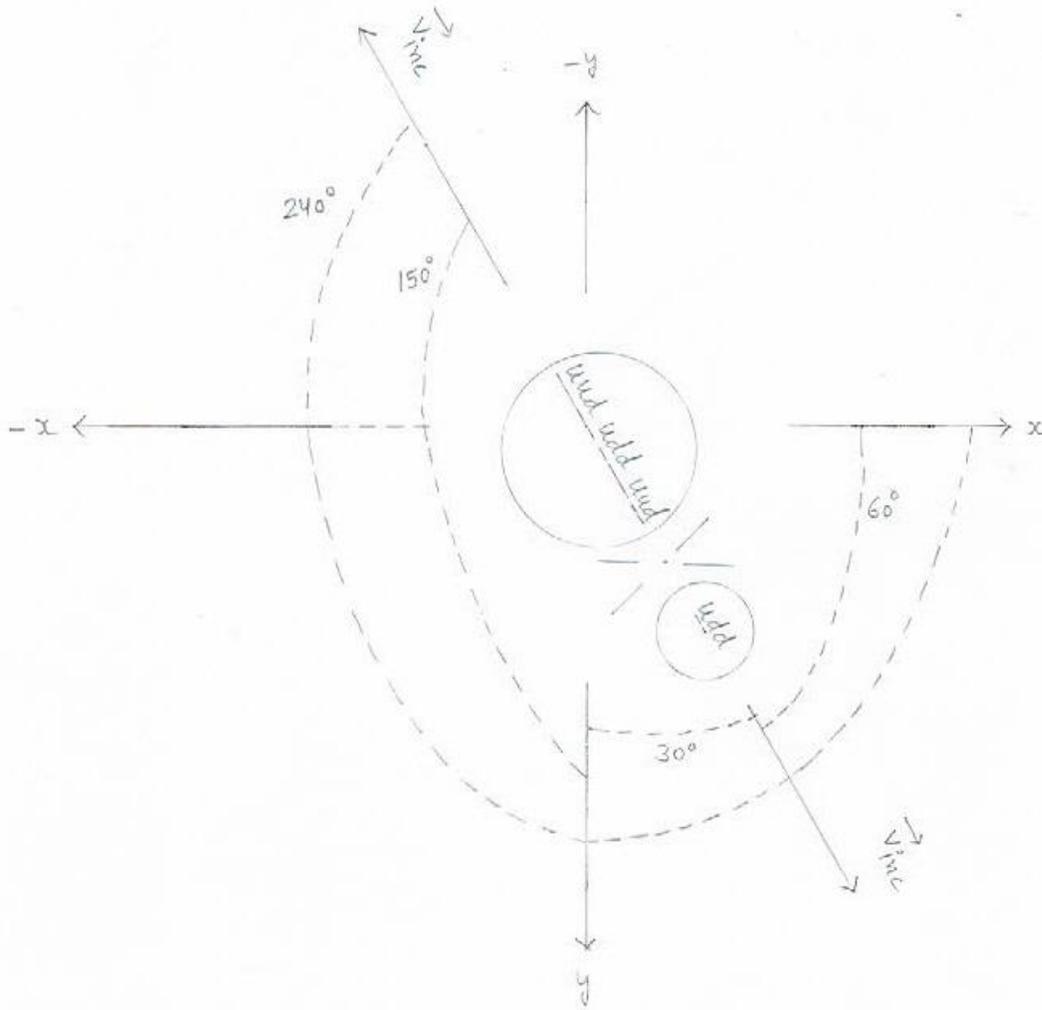
2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus(\vec{V}_{CN}) .]

Now,

At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

so, the neutron is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

While the helium -3 nucleus is propelled making 240° angle with x-axis, 150° angle with y-axis and 90° anglewith z-axis .



The direction along which the neutron is propelled is parallel to the $\overline{V_{cn}}$. while both particles (neutron and helium-3)are propelled making 180° angle with each other.

Components of the increased velocity of particles.

(i) For neutron

$$\mathbf{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.1623 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos 60^\circ = 0.5$$

$$\begin{aligned} \vec{v}_x &= 2.1623 \times 10^7 \times 0.5 \text{ m/s} \\ &= 1.0811 \times 10^7 \text{ m/s} \\ 2 \vec{v}_y &= v_{inc} \cos \beta \end{aligned}$$

$$\cos \beta = \cos 30^\circ = 0.866$$

$$\begin{aligned} \vec{v}_y &= 2.1623 \times 10^7 \times 0.866 \text{ m/s} \\ &= 1.8725 \times 10^7 \text{ m/s} \\ 3 \vec{v}_z &= v_{inc} \cos \gamma \end{aligned}$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\vec{v}_z = v_{inc} \times 0 = 0 \text{ m/s}$$

For Helium -3 nucleus

$$1 \vec{v}_x = v_{inc} \cos \alpha$$

$$v_{inc} = 0.7234 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos 240^\circ = -0.5$$

$$\begin{aligned} \vec{v}_x &= 0.7234 \times 10^7 \times (-0.5) \text{ m/s} \\ &= -0.3617 \times 10^7 \text{ m/s} \end{aligned}$$

$$2 \vec{v}_y = v_{inc} \cos \beta$$

$$\cos \beta = \cos 150^\circ = -0.8660$$

$$\begin{aligned} \vec{v}_y &= 0.7234 \times 10^7 \times (-0.866) \text{ m/s} \\ &= -0.6264 \times 10^7 \end{aligned}$$

$$3 \vec{v}_z = v_{inc} \cos \gamma$$

$$\vec{v}_z = v_{inc} \cos 90^\circ = v_{inc} \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9.. Components of the final velocity of the particles

Ifor neutron

According to -	Inherited Velocity (\vec{v}_{inh})	Increased Velocity (\vec{v}_{inc})	Final velocity (\vec{v}_f) $= (\vec{v}_{inh}) + (\vec{v}_{inc})$
X-axis	$\vec{v}_x = 0.1885 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.0811 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.2696 \times 10^7 \text{ m/s}$

y -axis	$\vec{v}_y = 0.3264 \times 10^7 \text{ m/s}$	$\vec{v}_y = 1.8725 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.1989 \times 10^7 \text{ m/s}$
z-axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..For helium-3 nuclens

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) = (\vec{v}_{inh}) + (\vec{v}_{inc})
X-axis	$\vec{v}_x = 0.1885 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.3617 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.1732 \times 10^7 \text{ m/s}$
y - axis	$\vec{v}_y = 0.3264 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.6264 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.3 \times 10^7 \text{ m/s}$
z -axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final Kinetic energy of the particle- neutron

$$V^2 = v_x^2 + v_y^2 + v_z^2$$

$$= (1.2696 \times 10^7)^2 + (2.1989 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$= (1.61188416 \times 10^{14}) + 4.83516121 \times 10^{14} + 0 \text{ m}^2/\text{s}^2$$

$$V^2 = 6.44704537 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V = 2.5391 \times 10^7 \text{ m/s}$$

$$\text{K.E.} = \frac{1}{2} m v^2 = \frac{1}{2} \times 1.6749 \times 10^{-27} \times 6.44704537 \times 10^{14} \text{ J}$$

$$= 5.3990781451 \times 10^{-13}$$

$$= 3.3744 \text{ Mev}$$

Angles made by the neutron , when it is at point F:-

if α , β , γ are angles made by the neutron with respect to the axes x,y, and z respectively. Then

$$\cos \alpha = \frac{v_x}{V} = \frac{\vec{v}_x}{V}$$

$$\cos \alpha = \frac{1.2696 \times 10^7 \text{ m/s}}{2.5391 \times 10^7 \text{ m/s}}$$

$$2.5391 \times 10^7 \text{ m/s}$$

$$\cos \alpha = 0.5000$$

$$\alpha = 60 \text{ degree}$$

$$2 \quad \cos \beta = \frac{V_{\cos \beta}}{V} = \frac{V_y}{V}$$

$$= \frac{2.1989 \times 10^7 \text{ m/s}}{2.5391 \times 10^7 \text{ m/s}} = 0.866$$

$$\beta = 30 \text{ degree}$$

$$3 \quad \cos \gamma = \frac{V_z}{V} = \frac{V_z}{V}$$

$$= 0$$

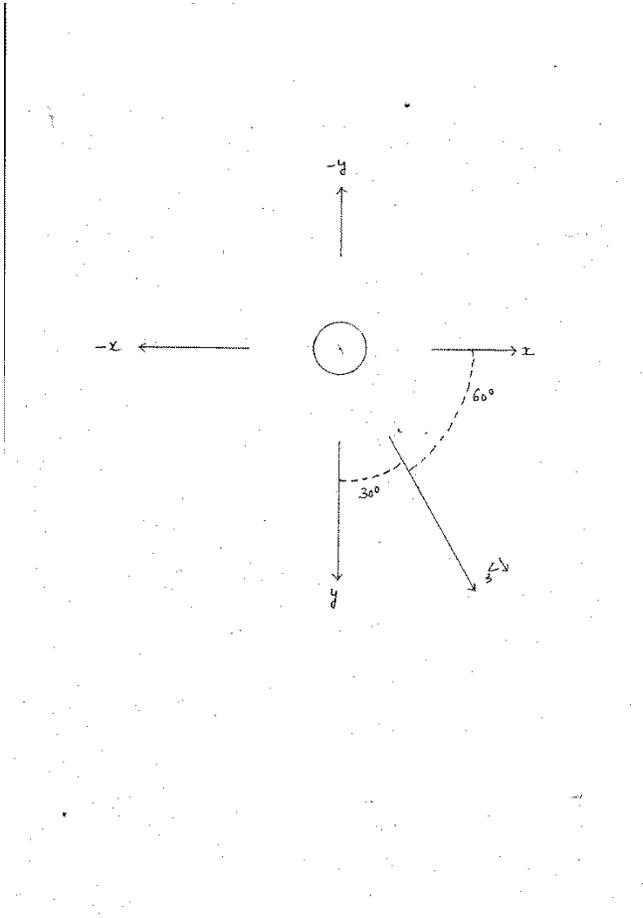
v

$$= 0$$

$$\gamma = 90^\circ$$

The real path followed by the neutron

The angles that make the final velocity of the neutron with positive x, y and z-axes.



where

$a=60$ degree

$b= 30$ degree

$y= 90$ degree

a,b and y are as usual used.

Components of final momentum of helium-3 nucleus

$$\begin{aligned} \vec{p}_x &= m_{\text{He-3}} \vec{v}_x \\ &= 5.00629 \times 10^{-27} \times (-0.1431 \times 10^7) \text{ kg m/s} \\ &= -0.7164 \times 10^{-20} \text{ kg m/s} \end{aligned}$$

$$\begin{aligned} 2 \vec{p}_y &= m_{\text{He-3}} \vec{v}_y \\ &= 5.00629 \times 10^{-27} \times (-0.2478 \times 10^7) \text{ kg m/s} \\ &= -1.2405 \times 10^{-20} \text{ kg m/s} \end{aligned}$$

$$\begin{aligned} 3 \vec{p}_z &= m_{\text{He-3}} \vec{v}_z \\ &= m_{\text{He-3}} \times 0 \text{ kg m/s} \\ &= 0 \text{ kg m/s} \end{aligned}$$

10.. Final Kinetic energy of the particle – helium 3 nucleus

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$= (0.1732 \times 10^7)^2 + (0.3 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$= (0.02999824 \times 10^{14}) + (0.09 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V^2 = 0.11999824 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V = 0.3464 \times 10^7 \text{ m/s}$$

$$mv^2 = 5.00629 \times 10^{-27} \times 0.11999824 \times 10^{14} \text{ J}$$

$$= 0.6007 \times 10^{-13} \text{ J}$$

$$\text{K.E.} = \frac{1}{2} mv^2 = \frac{1}{2} \times 5.00629 \times 10^{-27} \times 0.11999824 \times 10^{14} \text{ J}$$

$$= 0.30037299446 \times 10^{-13} \text{ J}$$

$$= 0.1877 \text{ MeV}$$

Angles made by the He-3 nucleus respect to point F :-

The He-3 nucleus is produced at point F. if α , β , γ are the angles made by the He-3 nucleus with respect to the axes x, y, and z respectively. Then

$$\cos \alpha = \frac{V \cos \alpha \rightarrow}{V}$$

$$= \frac{-0.1732 \times 10^7 \text{ m/s}}{0.3464 \times 10^7 \text{ m/s}} = -0.500$$

$$\alpha = 240^\circ$$

$$2 \cos \beta = \frac{V \cos \beta \rightarrow}{V}$$

$$= \frac{-0.3 \times 10^7 \text{ m/s}}{0.3464 \times 10^7 \text{ m/s}} = -0.866$$

$$\beta = 150^\circ$$

$$3 \cos \gamma = \frac{\rightarrow}{V}$$

$$= \frac{0}{0.3464 \times 10^7}$$

$$= 0$$

$$\gamma = 90^\circ$$

Forces acting on the helium-3 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\vec{v}_x = -0.1732 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -$$

$$1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 2 \times 1.6 \times 10^{-19} \times 0.1732 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.5547 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

so,

$$\vec{F}_y = 0.5547 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 2 \times 1.6 \times 10^{-19} \times 0.1732 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.5549 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (+) Z-axis,

so,

$$\vec{F}_z = 0.5549 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = -0.3 \times 10^7$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_x = 2 \times 1.6 \times 10^{-19} \times 0.3 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

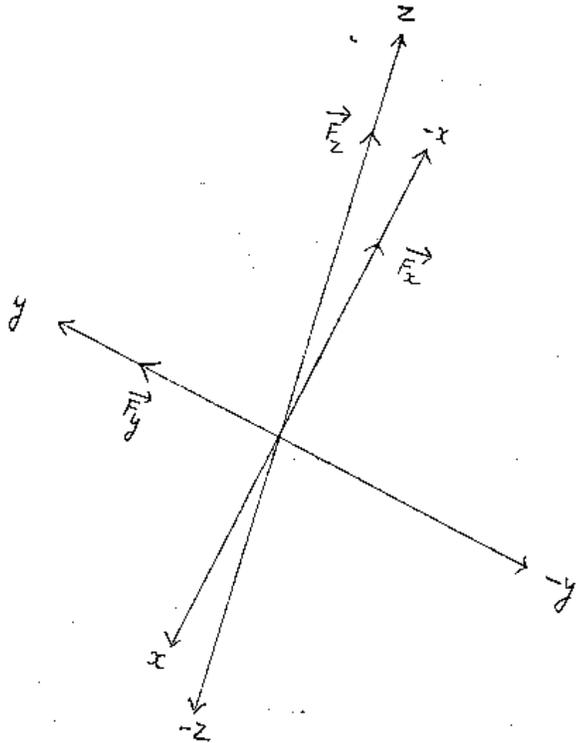
$$= 0.9609 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x-axis,

so,

$$\vec{F}_x = -0.9609 \times 10^{-13} \text{ N}$$

forces acting on the helium-3 nucleus



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 0.9609 \times 10^{-13} \text{ N}$$

$$F_y = 0.5547 \times 10^{-13} \text{ N}$$

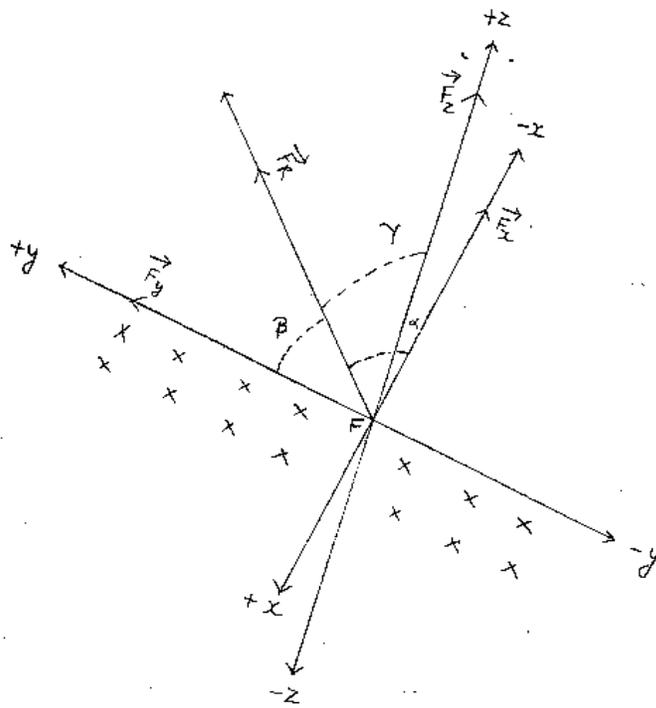
$$F_z = 0.5549 \times 10^{-13} \text{ N}$$

$$\begin{aligned} F_R^2 &= (0.9609 \times 10^{-13})^2 + (0.5547 \times 10^{-13})^2 + (0.5549 \times 10^{-13})^2 \quad \text{N}^2 \\ &= (0.92332881 \times 10^{-26}) + (0.30769209 \times 10^{-26}) + (0.30791401 \times 10^{-26}) \quad \text{N}^2 \end{aligned}$$

$$F_R^2 = 1.53893491 \times 10^{-26} \quad \text{N}^2$$

$$F_R = 1.2405 \times 10^{-13} \text{ N}$$

Resultant force acting on the helium-3 nucleus



Radius of the circular path :

Resultant force acts as a centripetal force on the helium-3 nucleus . so, the helium-3 nucleus tries to follow a confined circular path.

The radius of the circular orbit to be followed by the helium-3 nucleus is –

$$R = mv^2 / F_R$$

$$mv^2 = 0.6007 \times 10^{-13} \text{ J}$$

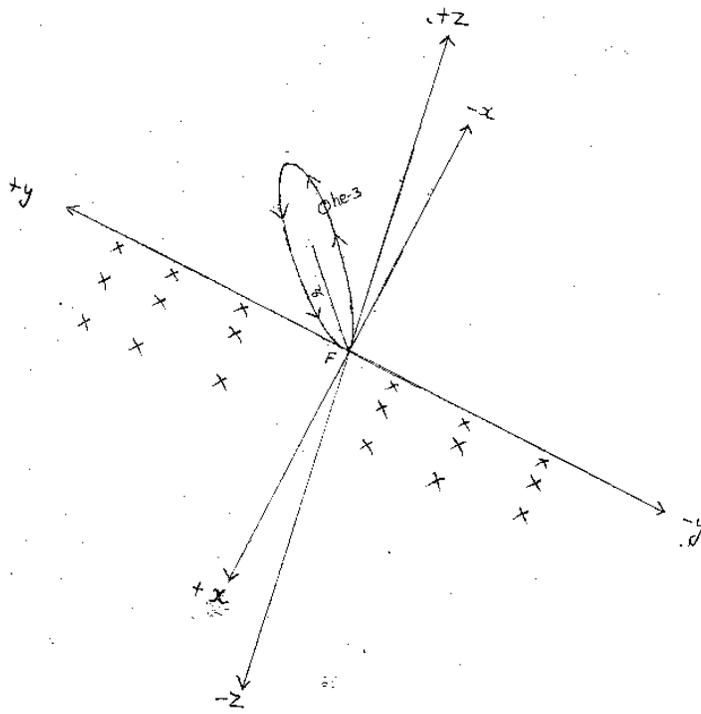
$$R = \frac{0.6007 \times 10^{-13} \text{ J}}{1.2405 \times 10^{-13} \text{ N}}$$

$$= 0.4842 \text{ m}$$

The circular orbit to be followed by the helion-3 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

\vec{F}_r = The resultant force acting on the particle (at point ' F ') towards the centre of the circle .

C_{He-3} = center of the circular orbit to be followed by the helion-3.



The plane of the circular orbit to be followed by the helion ⁻³ makes angles with respect to positive x, y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_{R \cos \alpha}}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = -0.9609 \times 10^{-13} \text{ N}$$

$$\frac{\vec{F}_x}{F_r} = \frac{-0.9609 \times 10^{-13}}{1.2405 \times 10^{-13}}$$

$$F_r = 1.2405 \times 10^{-13} \text{ N}$$

$$\cos \alpha = -0.7746$$

$$\alpha = 219.23 \text{ degree} \quad [\because \cos(219.23) = -0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = 0.5547 \times 10^{-13} \text{ N}$$

$$F_r = 1.2405 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4471$$

$$\beta = 63.44 \text{ degree} \quad [\because \cos(63.44) = 0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{\vec{F}_z}{F_r}$$

$$\vec{F}_z = 0.5549 \times 10^{-13} \text{ N}$$

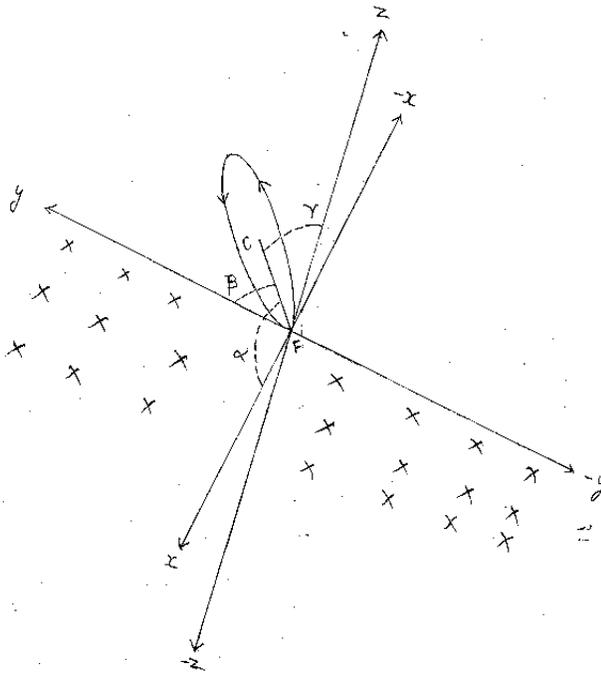
$$F_r = 1.2405 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4473$$

$$\gamma = 63.425 \text{ degree}$$

The plane of the circular orbit to be followed by the helion -3 makes angles with respect to positive x, y, and z axes as follows :-



Where,

$$\alpha = 219.23 \text{ degree}$$

$$\beta = 63.44 \text{ degree}$$

$$\gamma = 63.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the helium-3

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$= 2 \times 0.4842 \text{ m}$$

$$= 0.9684 \text{ m}$$

$$d = 2 \times r$$

$$\cos \alpha = -0.7746$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 0.9684 \times (-0.7746) \text{ m}$$

$$x_2 - x_1 = -0.7501 \text{ m}$$

$$x_2 = -0.7501 \text{ m} [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

d

$$\cos \beta = 0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 0.9684 \times 0.4471 \text{ m}$$

$$y_2 - y_1 = 0.4329 \text{ m}$$

$$y_2 = 0.4329 \text{ m} [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

d

$$\cos \gamma = 0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 0.9684 \times 0.4473 \text{ m}$$

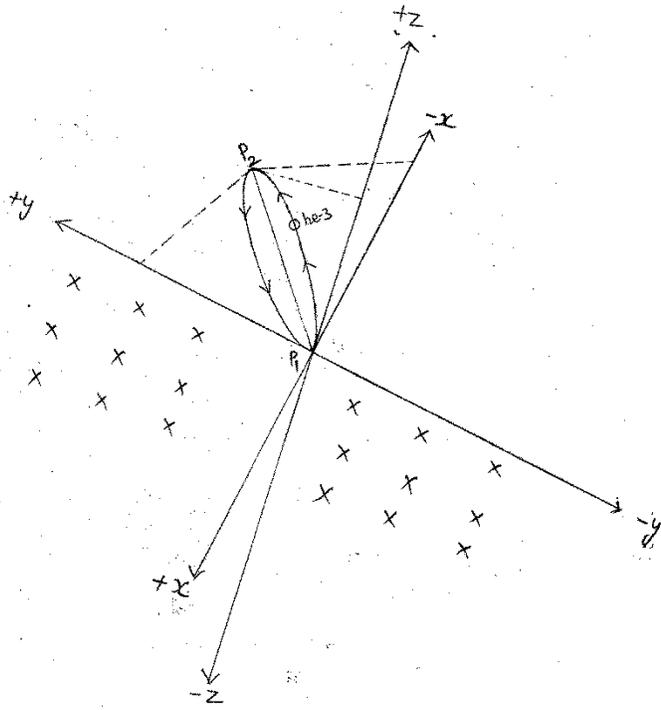
$$z_2 - z_1 = 0.4331 \text{ m}$$

$$z_2 = 0.4331 \text{ m} [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the helium-3 nucleus are as shown below.

The line ____ is the diameter of the circle .

P_1P_2



Conclusion :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **-x , +y and +z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 0.4842 m.

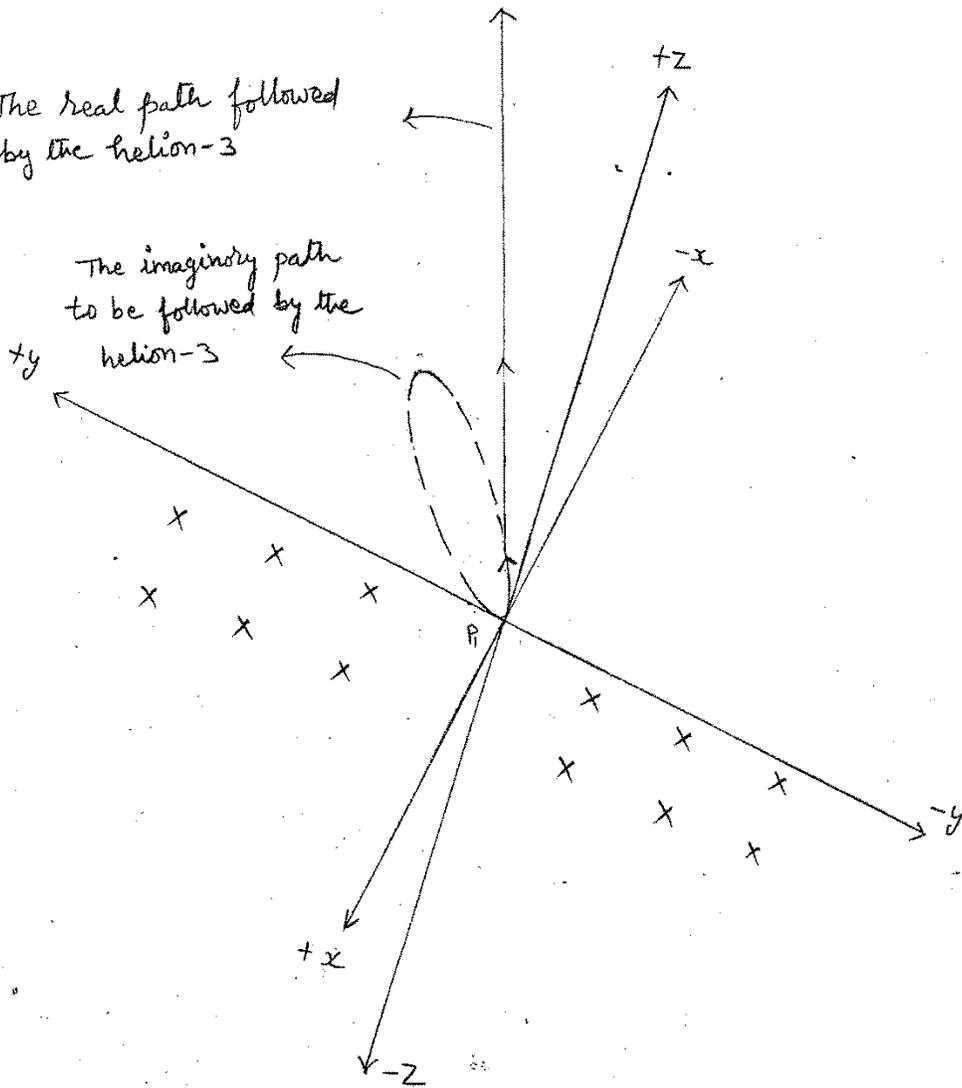
It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.7501 \text{ m}, 0.4329 \text{ m}, 0.4331 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the helium-3 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

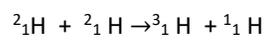
Hence the helium-3 nucleus is not confined.

The real path followed
by the helion-3

The imaginary path
to be followed by the
helion-3



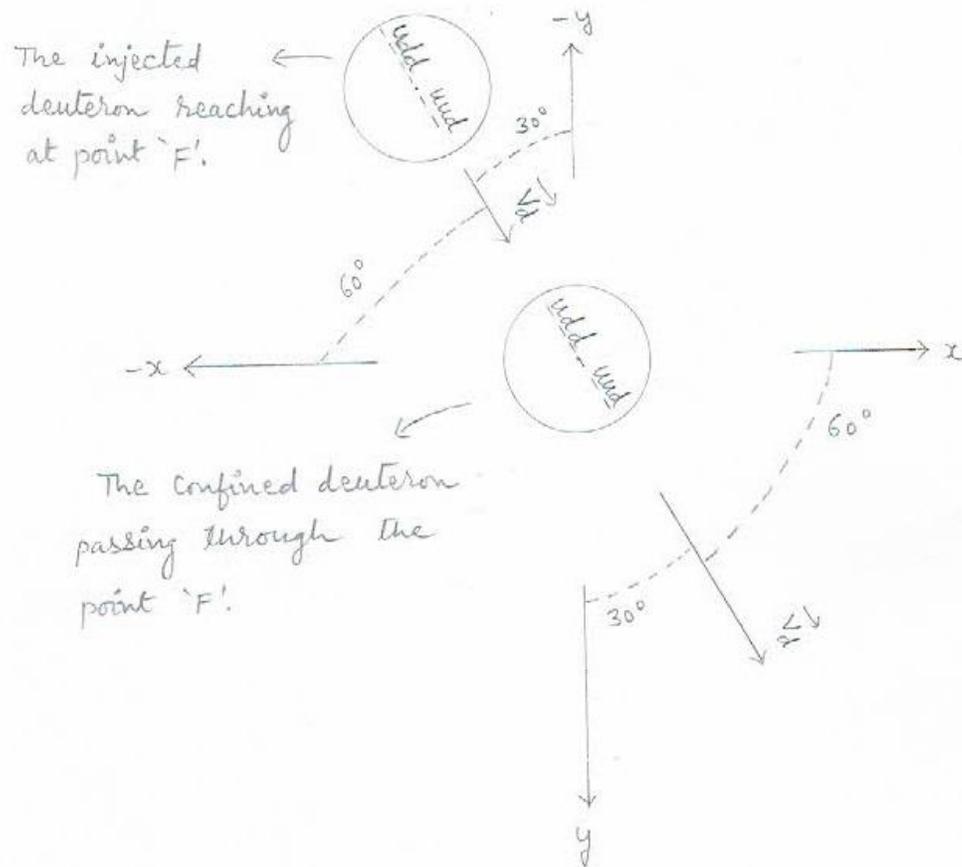
For fusion reaction



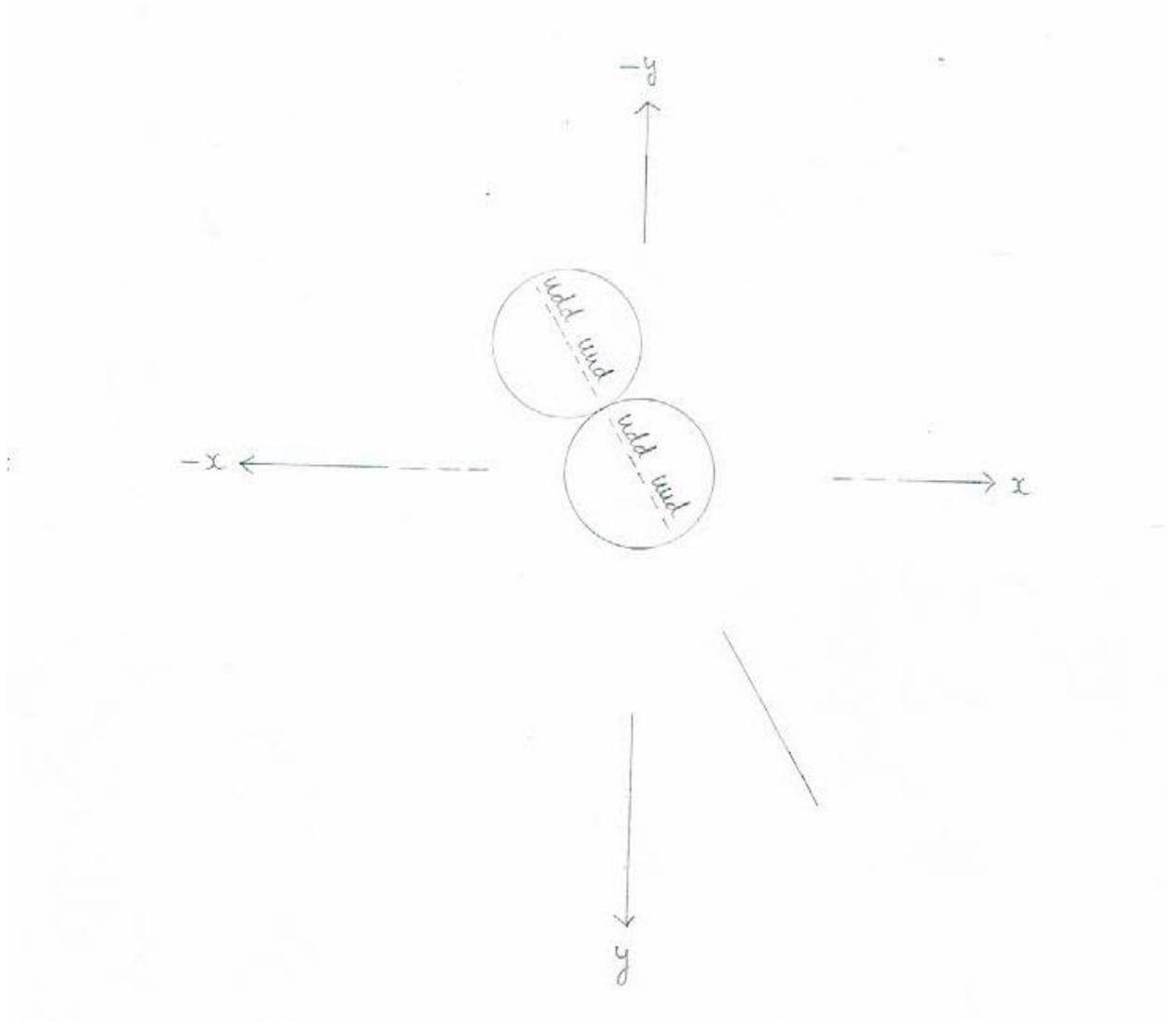
interaction of nuclei :-

The injected deuteron reaches at point F, and interacts [experiences a repulsive force due to the confined deuteron] with the confined deuteron passing through the point F. the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined deuteron.

interaction of nuclei (1)



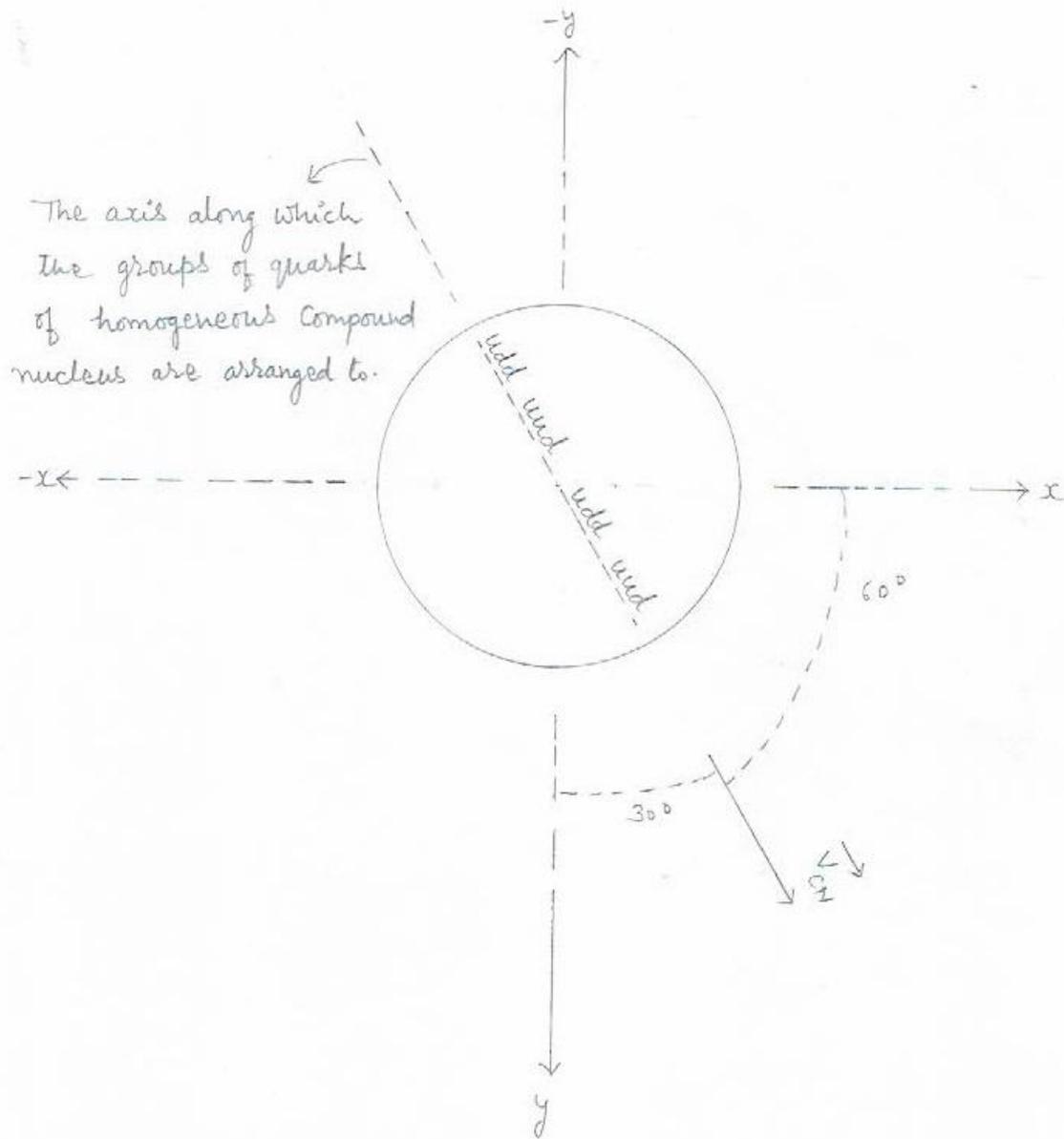
interaction of nuclei(2)



1..Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron) behave like a liquid and form a homogeneous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus in a homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 4 groups of quarks with surrounded gluons.



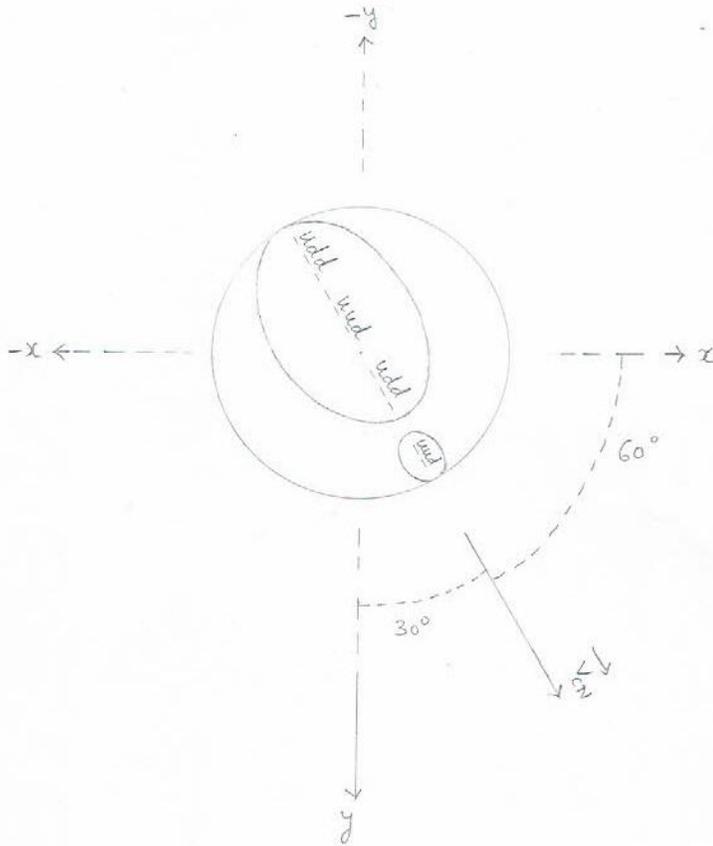
Formation of homogenous compound nucleus

3 Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the triton) than the reactant one (the deuteron) includes the other two (nearby located) groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

While , the remaing groups of quarks to become a stable nucleus (the proton) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe ' A '] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two dissimilar lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.



Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the triton and the smaller one is the proton while the remaining space represents the remaining gluons ..

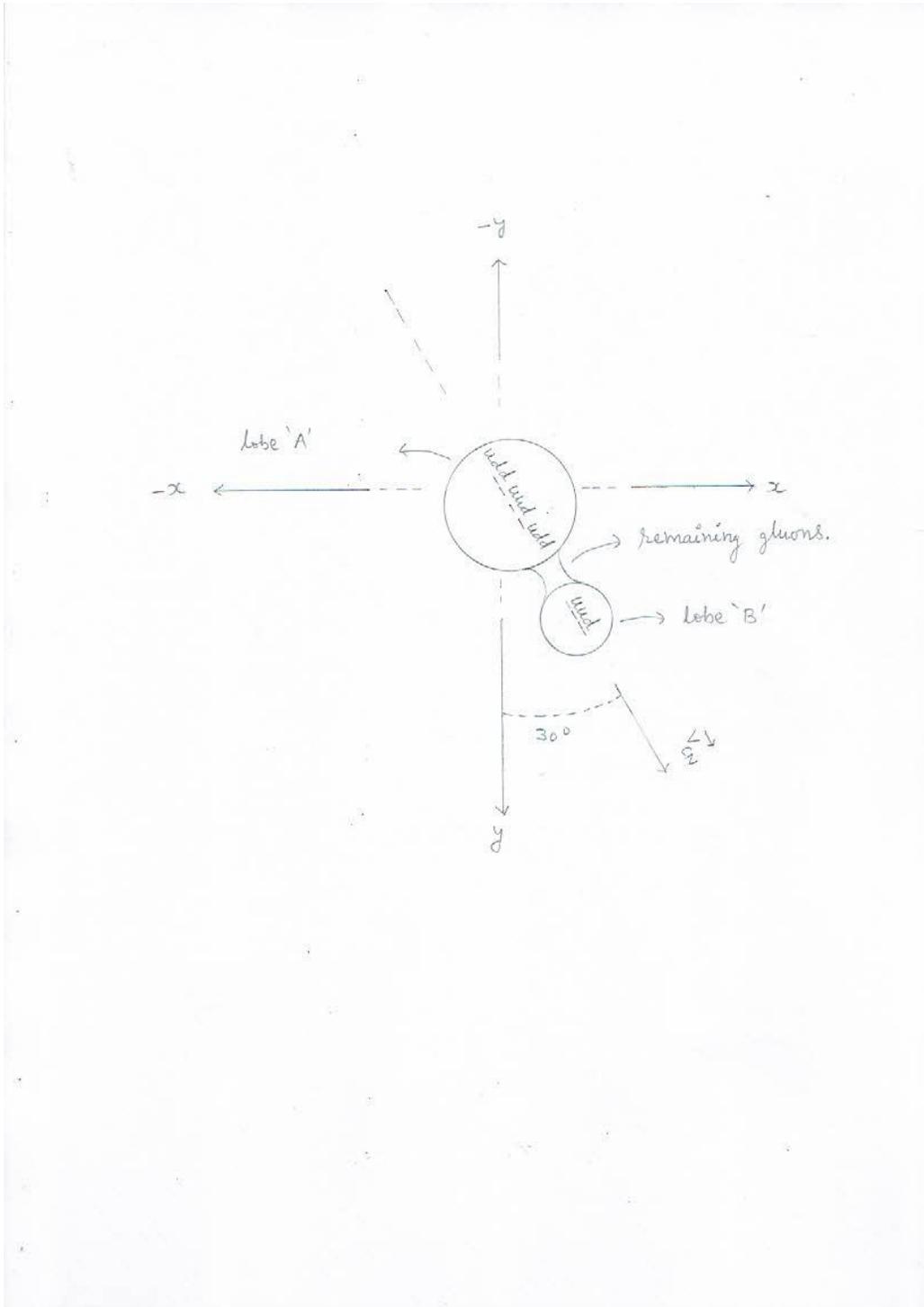
within into the homogenous compound nucleus , the greater nucleus is the lobe 'A ' while the smaller nucleus is the lobe 'B' .

4..Final stage of the heterogeneous compound nucleus : -

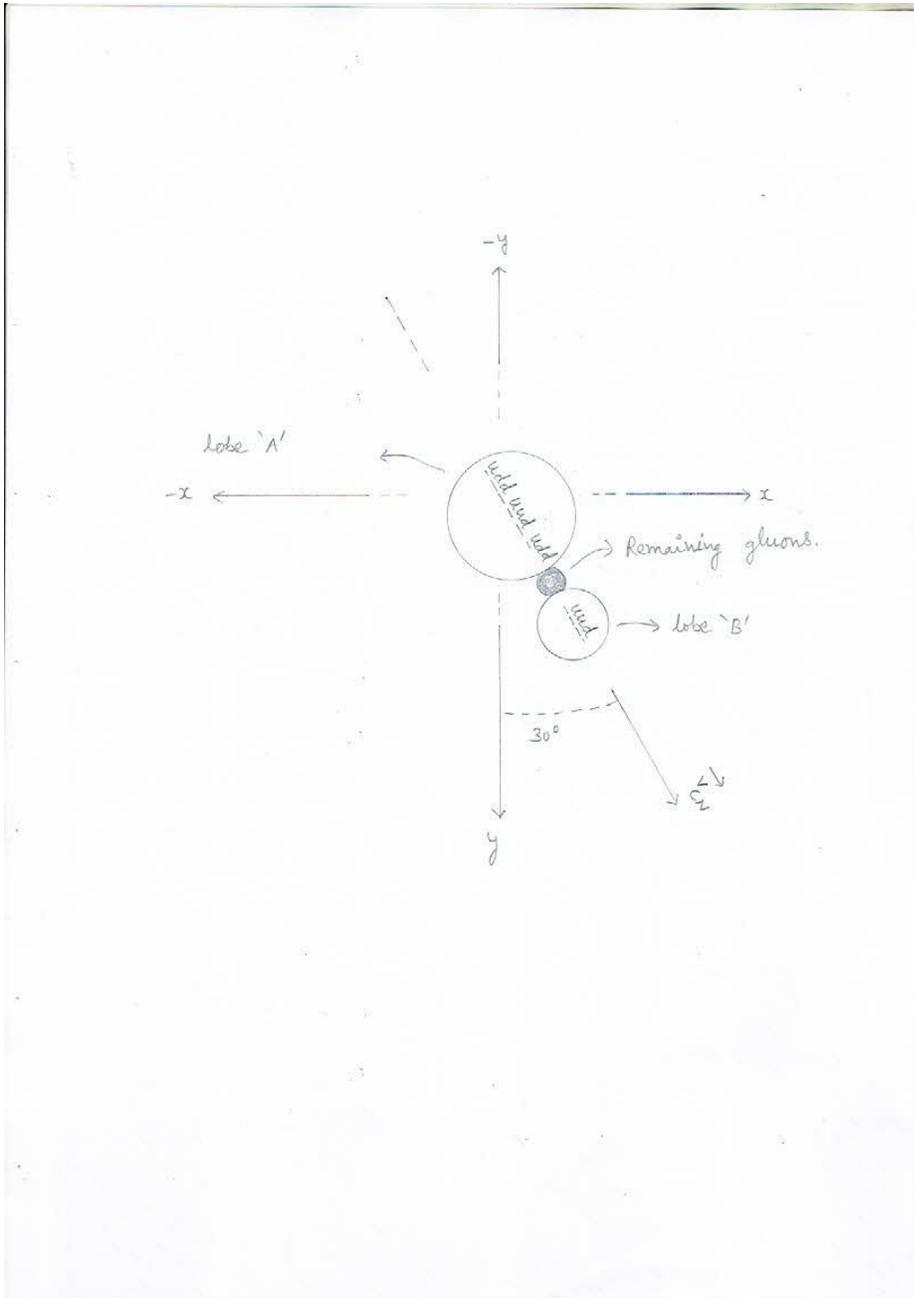
The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids (s) between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogenous compound nucleus



Final stage of a heterogeneous compound nucleus.

The splitting of the heterogeneous compound nucleus :-

The heterogeneous compound nucleus, due to its instability, splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – triton, the proton and the reduced mass (Δm).

Out of them, the two particles (the triton and proton) are stable while the third one (reduced mass) is unstable.

According to the law of inertia, each particle that is produced due to splitting of the compound nucleus, has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}).

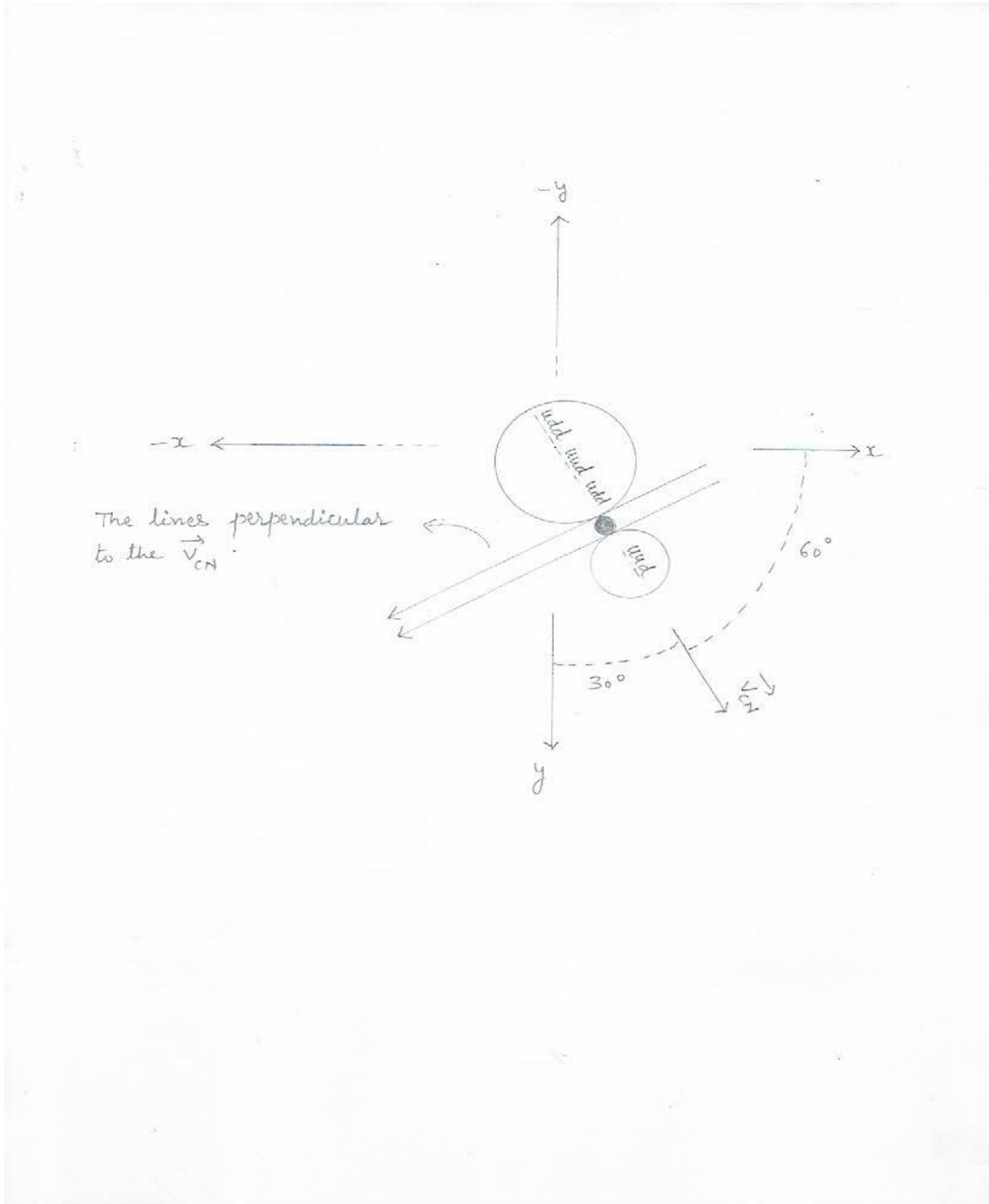
So, for conservation of momentum

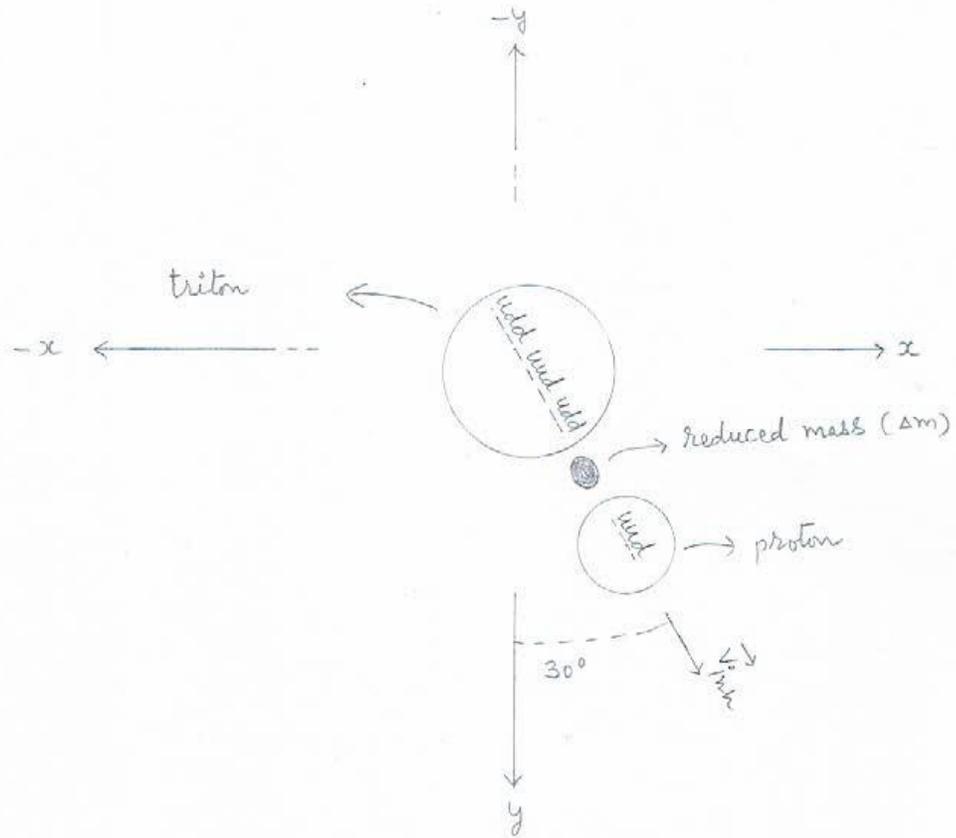
$$M\vec{V}_{cn} = (m_t + \Delta m + m_p)\vec{V}_{cn}$$

Where,

M	= mass of the compound nucleus
\vec{V}_{cn}	= velocity of the compound nucleus
m_t	= mass of the triton
Δm	= reduced mass
m_p	= mass of the proton

The splitting of the heterogeneous compound nucleus





Components of Inherited velocity of the particles :-

Each particles has inherited velocity (\vec{V}_{inh}) equal to the velocity of the compound nucleus(\vec{V}_{cn}) .

I. For triton (${}^3_1\text{H}$)

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the triton

$$1 \rightarrow \frac{V_x}{V_x} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1885 \times 10^7 \text{ m/s}$$

$$2 \rightarrow \frac{V_y}{V_y} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.3264 \times 10^7 \text{ m/s}$$

$$3 \rightarrow \frac{V_z}{V_z} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

II . Inherited velocity of the proton

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the proton

$$1 \rightarrow \frac{V_x}{V_x} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1885 \times 10^7 \text{ m/s}$$

$$2 \rightarrow \frac{V_y}{V_y} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.3264 \times 10^7 \text{ m/s}$$

$$3 \rightarrow \frac{V_z}{V_z} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

iii Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propels both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_d] - [m_t + m_p]$$

$$\Delta m = [2 \times 2.01355] - [3.0155 + 1.00727] \text{ amu}$$

$$\Delta m = [4.0271] - [4.02277] \text{ amu}$$

$$\Delta m = 0.00433 \text{ amu}$$

$$\Delta m = 0.00433 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$\Delta m = 0.007189 \times 10^{-27} \text{ kg}$$

Inherited kinetic energy of reduced mass (Δm) .

$$E_{\text{inh}} = \frac{1}{2} \Delta m v_{\text{cn}}^2$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.007189 \times 10^{-27} \times 0.14216694382 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00051101907 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.000319 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.00433 \times 931 \text{ Mev}$$

$$E_R = 4.03123 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{\text{inh}} + E_R$$

$$E_T = [0.000319] + [4.03123] \text{ Mev}$$

$$E_T = 4.031549 \text{ Mev}$$

Increased in the energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to inverse masses. so, the increased energy (E_{inc}) of the particles :-

1.. Increased energy of the triton

$$E_{inc} = \frac{m_p}{m_t + m_p} \times E_T$$

$$E_{inc} = \frac{1.00727 \text{ amu}}{1.00727 + 3.0155} \times 4.031549 \text{ Mev}$$

$$E_{inc} = \frac{1.00727}{4.02277} \times 4.031549 \text{ Mev}$$

$$E_{inc} = [0.25039214272] \times 4.031549 \text{ Mev}$$

$$E_{inc} = 1.009468 \text{ Mev}$$

2..increased energy of the proton

$$E_{inc} = [E_T] - [\text{increased energy of the triton}]$$

$$E_{inc} = [4.031549] - [1.009468] \text{ Mev}$$

$$E_{inc} = 3.022081 \text{ Mev}$$

6..Increased velocity of the particles .

(1) For triton

$$E_{inc} = \frac{1}{2} m_t v_{inc}^2$$

$$v_{inc} = [2 \times E_{inc} / m_t]^{\frac{1}{2}}$$

$$\begin{aligned}
 &= \left(\frac{2 \times 1.009468 \times 1.6 \times 10^{-13} \text{ J}}{5.0072 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}} \\
 &= \left(\frac{3.2302976 \times 10^{-13}}{5.0072 \times 10^{-27}} \right)^{\frac{1}{2}} \text{ m/s} \\
 &= [0.64513053203 \times 10^{14}]^{\frac{1}{2}} \text{ m/s} \\
 &= 0.8032 \times 10^7 \text{ m/s}
 \end{aligned}$$

(2) For proton

$$v_{inc} = [2 E_{inc} / m_p]^{\frac{1}{2}}$$

$$\begin{aligned}
 &= \left(\frac{2 \times 3.022081 \times 1.6 \times 10^{-13} \text{ J}}{1.6726 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}} \\
 &= \left(\frac{9.6706592 \times 10^{-13}}{1.6726 \times 10^{-27}} \right)^{\frac{1}{2}} \text{ m/s}
 \end{aligned}$$

$$= [5.78181226832 \times 10^{14}]^{1/2} \text{ m/s}$$

$$= 2.4045 \times 10^7 \text{ m/s}$$

7 Angle of propulsion

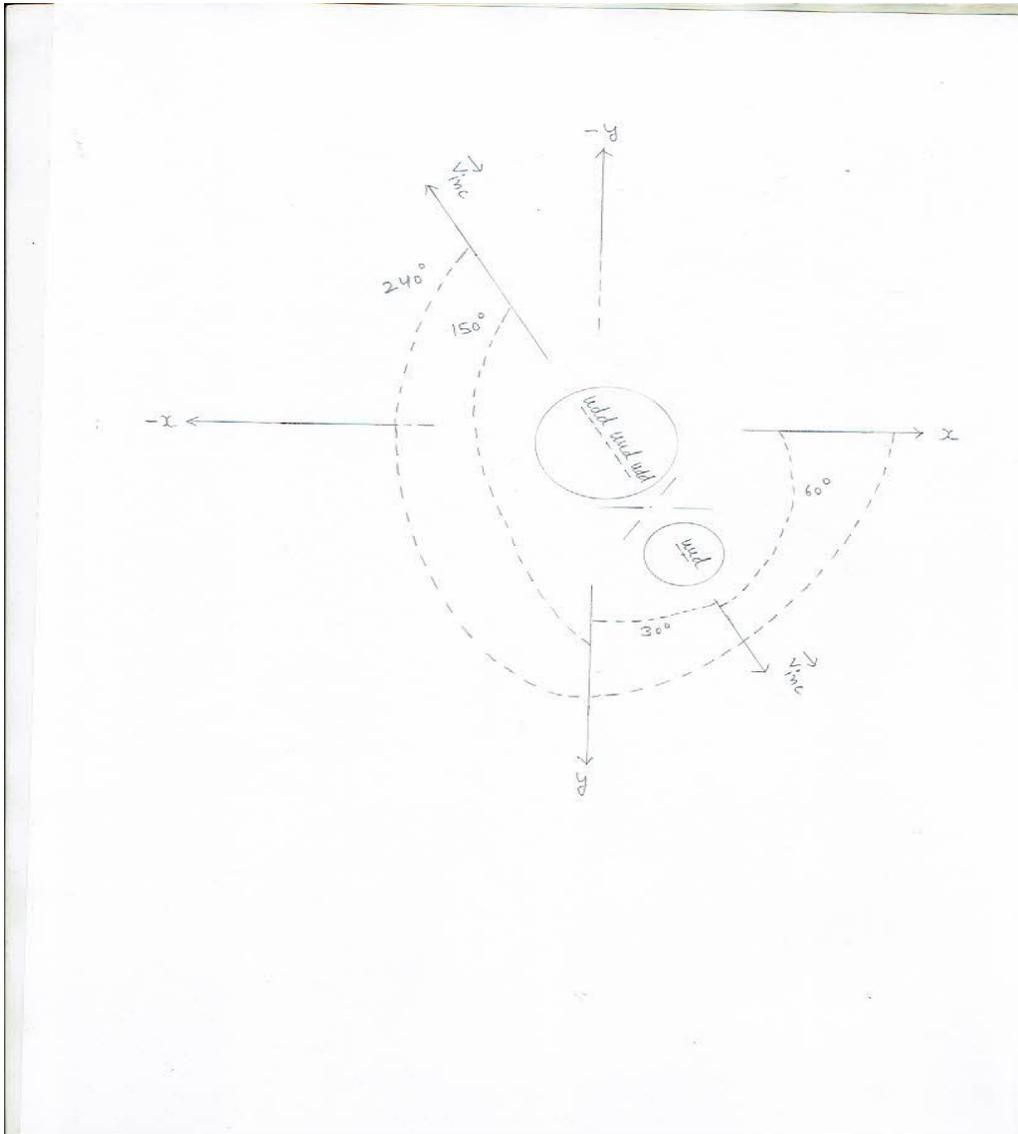
1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum.

2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus (\vec{V}_{CN}) .]

3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

so, the proton is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis

While the triton is propelled making 240° angle with x-axis , 150° angle with y-axis and 90° angle with z-axis .



The direction along which the proton is propelled make angle 180° with the direction along which the triton is propelled.

Components of the increased velocity (V_{inc}) of the particles.

(i) For proton

$$\mathbf{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.4045 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos 60^\circ = 0.5$$

$$\begin{aligned} \vec{v}_x &= 2.4045 \times 10^7 \times 0.5 \text{ m/s} \\ &= 1.2022 \times 10^7 \text{ m/s} \\ 2\vec{v}_y &= v_{inc} \cos \beta \end{aligned}$$

$$\cos \beta = \cos 30^\circ = 0.8666666$$

$$\vec{v}_y = 2.4045 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 2.0822 \times 10^7 \text{ m/s}$$

$$3\vec{v}_z = v_{inc} \cos \gamma = v_{inc} \cos 90^\circ = v_{inc} \times 0 = 0 \text{ m/s}$$

For triton

$$1\vec{v}_x = v_{inc} \cos \alpha$$

$$v_{inc} = 0.8032 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos 240^\circ = -0.5$$

$$\vec{v}_x = 0.8032 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.4016 \times 10^7 \text{ m/s}$$

$$2\vec{v}_y = v_{inc} \cos \beta$$

$$\cos \beta = \cos 150^\circ = -0.866.866.8668666$$

$$= 0.8032 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.6955 \times 10^7 \text{ m/s}$$

$$3\vec{v}_z = v_{inc} \cos \gamma = v_{inc} \cos 90^\circ = v_{inc} \times 0 = 0 \text{ m/s}$$

9.. Components of the final velocity (Vf)of the particles

I Fortriton

According to -	Inherited Velocity (\vec{v}_{inh})	Increased Velocity (\vec{v}_{inc})	Final velocity (\vec{v}_f) = (\vec{v}_{inh}) + (\vec{v}_{inc})
X - axis	$\vec{v}_x = 0.1885 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.4016 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.2131 \times 10^7 \text{ m/s}$

y-axis	$\vec{v}_y = 0.3264 \times 10^7 \text{ m/s}$	$\vec{v}_y = 0.6955 \times 10^7 \text{ m/s}$	$\vec{v}_y = 0.3691 \times 10^7 \text{ m/s}$
z-axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..For proton

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) = (\vec{v}_{inh}) + (\vec{v}_{inc})
X-axis	$\vec{v}_x = 0.1885 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.2022 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.3907 \times 10^7 \text{ m/s}$
y-axis	$\vec{v}_y = 0.3264 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.0822 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.4086 \times 10^7 \text{ m/s}$
z-axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final Kinetic energy of the particle -triton

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$= (0.2131 \times 10^7)^2 + (0.3691 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$= (0.04541161 \times 10^{14}) + (0.13623481 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V^2 = 0.18164642 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V = 0.4261 \times 10^7 \text{ m/s}$$

$$mv^2 = 5.0072 \times 10^{-27} \times 0.18164642 \times 10^{14} \text{ J}$$

$$= 0.9095 \times 10^{-13} \text{ J}$$

$$\text{K.E.} = \frac{1}{2} mv^2 = \frac{1}{2} \times 5.0072 \times 10^{-27} \times 0.13391461 \times 10^{14} \text{ J}$$

$$= 0.45476997711 \times 10^{-13} \text{ J}$$

$$= 0.2842 \text{ Mev}$$

Forces acting on the triton

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.2131 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 1.6 \times 10^{-19} \times 0.2131 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 0.3413 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

$$\text{so,}$$

$$\vec{F}_y = 0.3413 \times 10^{-13} \text{ N}$$

$$2 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = -0.3691 \times 10^7 \text{ m/s}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_x = 1.6 \times 10^{-19} \times 0.3691 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 0.5911 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x-axis,

$$\text{so,}$$

$$\vec{F}_x = -0.5911 \times 10^{-13} \text{ N}$$

$$3 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 1.6 \times 10^{-19} \times 0.2131 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N}$$

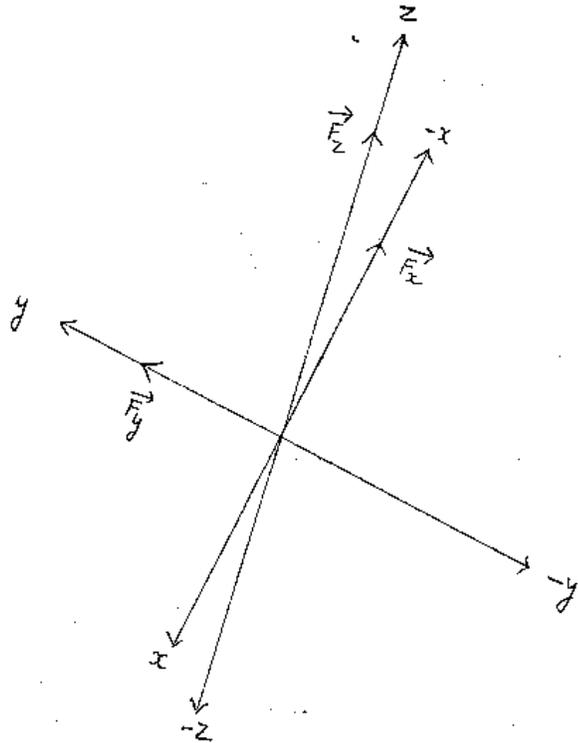
$$= 0.3414 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_z is according to (+) z-axis,

$$\text{so,}$$

$$\vec{F}_z = 0.3414 \times 10^{-13} \text{ N}$$

Forces acting on the triton



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 0.5911 \times 10^{-13} \text{ N}$$

$$F_y = 0.3413 \times 10^{-13} \text{ N}$$

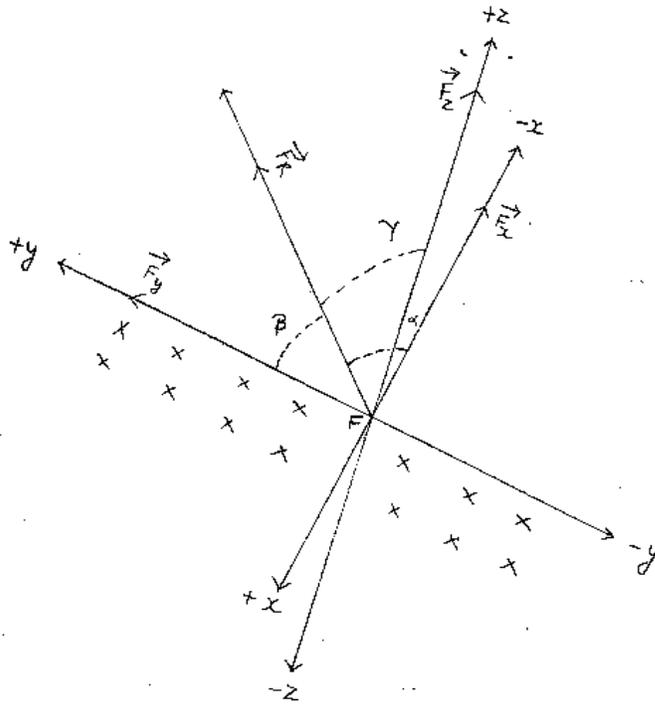
$$F_z = 0.3414 \times 10^{-13}$$

$$\begin{aligned} F_R^2 &= (0.5911 \times 10^{-13})^2 + (0.3413 \times 10^{-13})^2 + (0.3414 \times 10^{-13})^2 \text{ N}^2 \\ &= (0.34939921 \times 10^{-26}) + (0.11648569 \times 10^{-26}) + (0.11655396 \times 10^{-26}) \text{ N}^2 \end{aligned}$$

$$F_R^2 = 0.58243886 \times 10^{-26} \text{ N}^2$$

$$F_R = 0.7631 \times 10^{-13} \text{ N}$$

Resultant force acting on the triton



Radius of the circular path :

Resultant force acts as a centripetal force on the triton . so, the triton tries to follow a confined circular path.

The radius of the circular orbit to be obtained by the triton is –

$$r = mv^2 / F_R$$

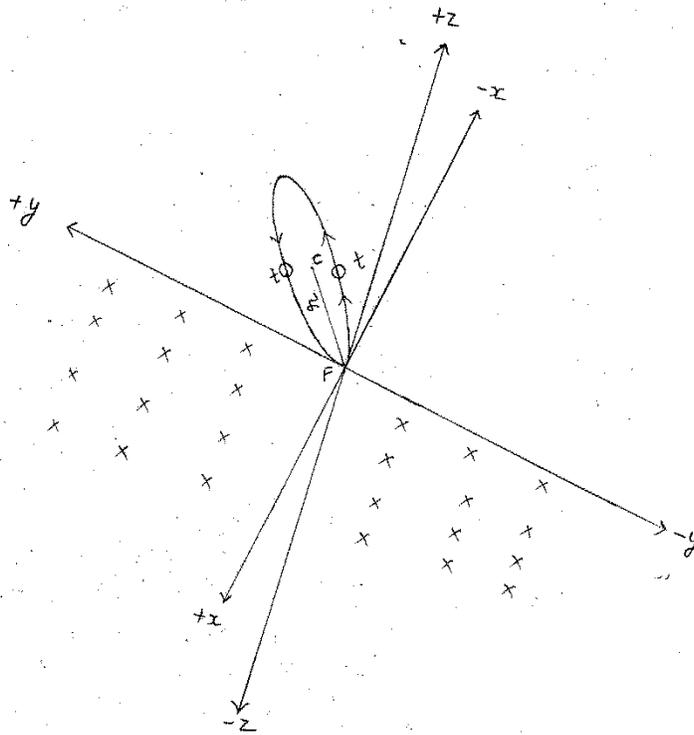
$$r = \frac{0.9095 \times 10^{-13} \text{ J}}{0.7631 \times 10^{-13} \text{ N}}$$

$$r = 1.1918 \text{ m}$$

The circular orbit to be followed by the triton lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

\vec{F}_r = The resultant force acting on the particle (at point ' F ') towards the centre of the circle .

C_t = center of the circular orbit to be followed by the triton.



The plane of the circular orbit to be followed by the triton makes angles with respect to positive x , y and z-axes as follows :-

1 with- axis

$$\cos \alpha = \frac{F_x \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = -0.5911 \times 10^{-13} \text{ N}$$

$$F_r = 0.7631 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7746$$

$$\alpha = 219.23 \text{ degree } [\because \cos (219.23) = -0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{F_{r \rightarrow y}}{F_r}$$

$$\frac{F_{r \rightarrow y}}{F_r} = 0.3413 \times 10^{-13} \text{ N}$$

$$F_r = 0.7631 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4472$$

$$\beta = 63.43 \text{ degree } [\because \cos (63.43) = 0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{F_{r \rightarrow z}}{F_r}$$

$$\frac{F_{r \rightarrow z}}{F_r} = \underline{0.3414 \times 10^{-13} \text{ N}}$$

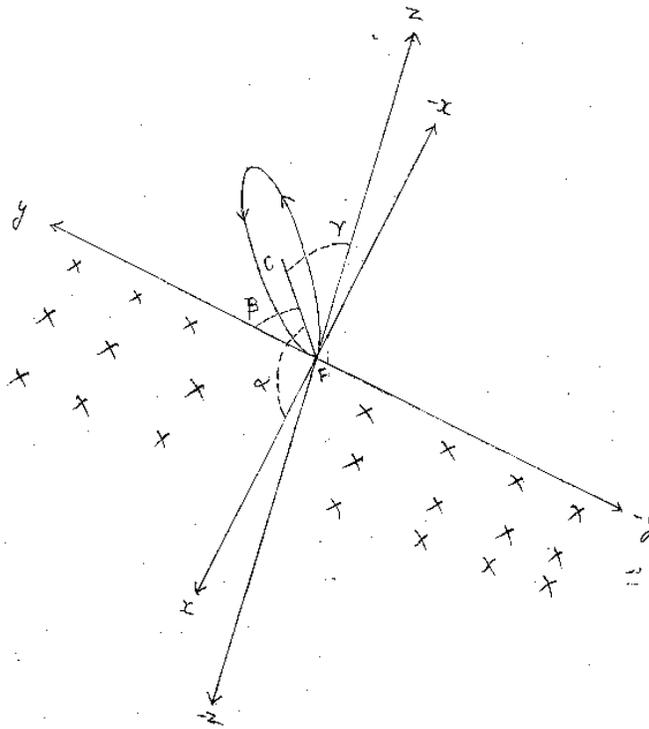
$$F_r = 0.7631 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4473$$

$$\gamma = 63.425 \text{ degree}$$

The plane of the circular orbit to be followed by the triton makes angles with positive x , y , and z axes as follows:-



Where,

$$\alpha = 219.23 \text{ degree}$$

$$\beta = 63.43 \text{ degree}$$

$$\gamma = 63.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the triton

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$d = 2 \times r$$

$$= 2 \times 1.1918 \text{ m}$$

$$= 2.3836 \text{ m}$$

$$\cos \alpha = -0.7746$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 2.3836 \times (-0.7746) \text{ m}$$

$$x_2 - x_1 = -1.8463 \text{ m}$$

$$x_2 = -1.8463 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$d$$

$$\cos \beta = 0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 2.3836 \times 0.4472 \text{ m}$$

$$y_2 - y_1 = 1.0659 \text{ m}$$

$$y_2 = 1.0659 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$d$$

$$\cos \gamma = 0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 2.3836 \times 0.4473 \text{ m}$$

$$z_2 - z_1 = 1.0661 \text{ m}$$

$$z_2 = 1.0661 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2(x_2, y_2, z_2)$ located on the circumference of the circular orbit to be followed by the triton.

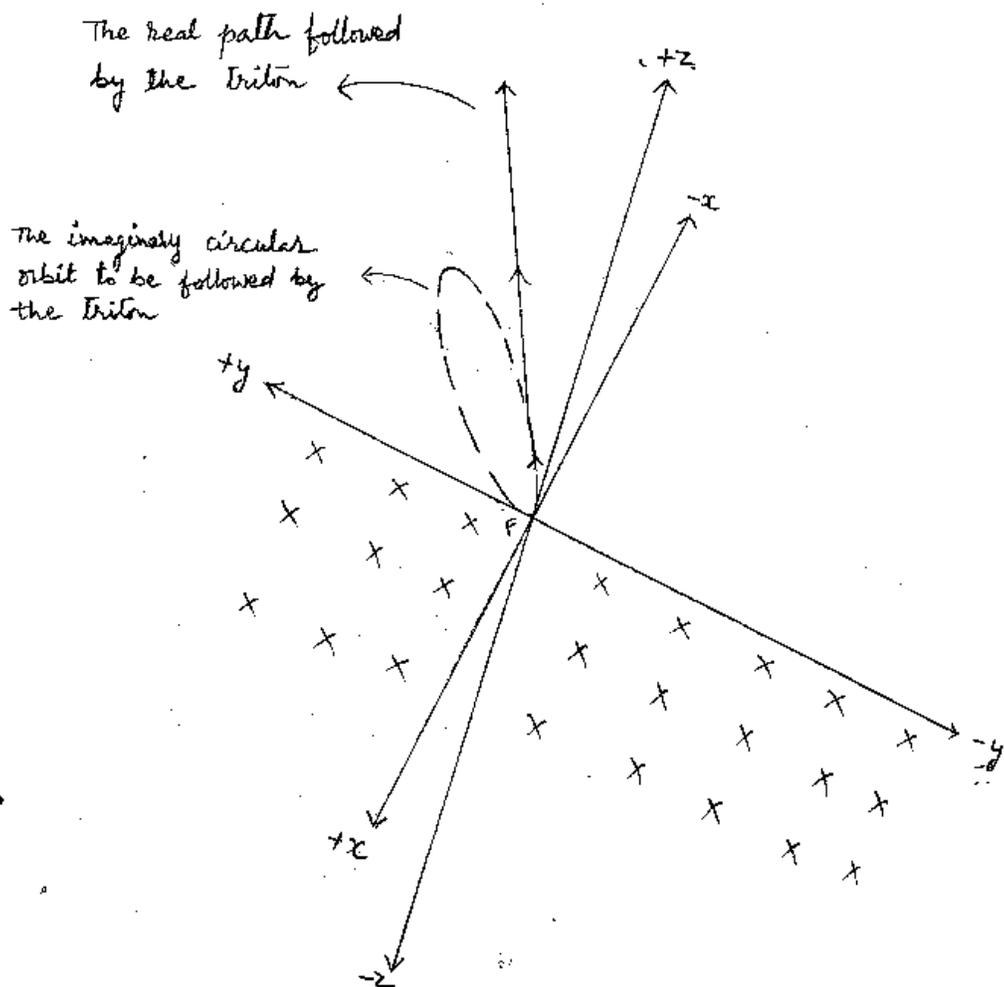
The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the triton are along **-x, +y and +z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the triton lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the triton to undergo to a circular orbit of radius 1.1918m . It starts its circular motion from point P₁(0,0,0) and tries to reach at point P₂(-1.8463 m, 1.0659 m, 1.0661 m) where the magnetic fields are not applied.

So , It starts its circular motion from point P₁(0,0,0) and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the triton gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

Hence the triton is not confined.



10.. Final Kinetic energy of the particle - proton

$$\begin{aligned}
 V^2 &= V_x^2 + V_y^2 + V_z^2 \\
 &= (1.3907 \times 10^7)^2 + (2.4086 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2 \\
 &= (1.93404649 \times 10^{14}) + (5.80135396 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2 \\
 V^2 &= 7.73540045 \times 10^{14} \text{ m}^2/\text{s}^2 \\
 V &= 2.7812 \times 10^7 \text{ m/s} \\
 mv^2 &= 1.6726 \times 10^{-27} \times 7.73540045 \times 10^{14} \text{ J} \\
 &= 12.9382 \times 10^{-13} \text{ J} \\
 \text{K.E.} &= \frac{1}{2} mv^2 = \frac{1}{2} \times 1.6726 \times 7.73540045 \times 10^{14} \text{ J} \\
 &= 6.4691 \\
 &= 4.0431 \text{ Mev}
 \end{aligned}$$

Forces acting on the proton

$$F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = 1.3907 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 1.6 \times 10^{-19} \times 1.3907 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 2.2273 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_y is according to (-) y-axis ,

so ,

$$\vec{F}_y = - 2.2273 \times 10^{-13} \text{ N}$$

$$2 \ F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = 2.4086 \times 10^7$$

$$\vec{B}_z = - 1.001 \times 10^{-1} \text{tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_x = 1.6 \times 10^{-19} \times 2.4086 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 3.8576 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_x is according to (+) x- axis ,

so ,

$$\vec{F}_x = 3.8576 \times 10^{-13} \text{ N}$$

$$3 \ F_z = q V_x B_y \sin \theta$$

$$\vec{V}_x = 1.0013 \times 10^{-1} \text{m/s}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 1.6 \times 10^{-19} \times 1.3907 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

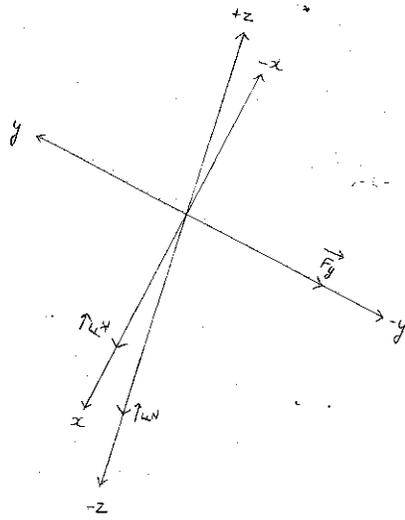
$$= 2.2280 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_z is according to (-) z axis ,

so ,

$$\vec{F}_z = - 2.2280 \times 10^{-13} \text{ N}$$

The forces acting on the proton



Resultant force (F_R) :

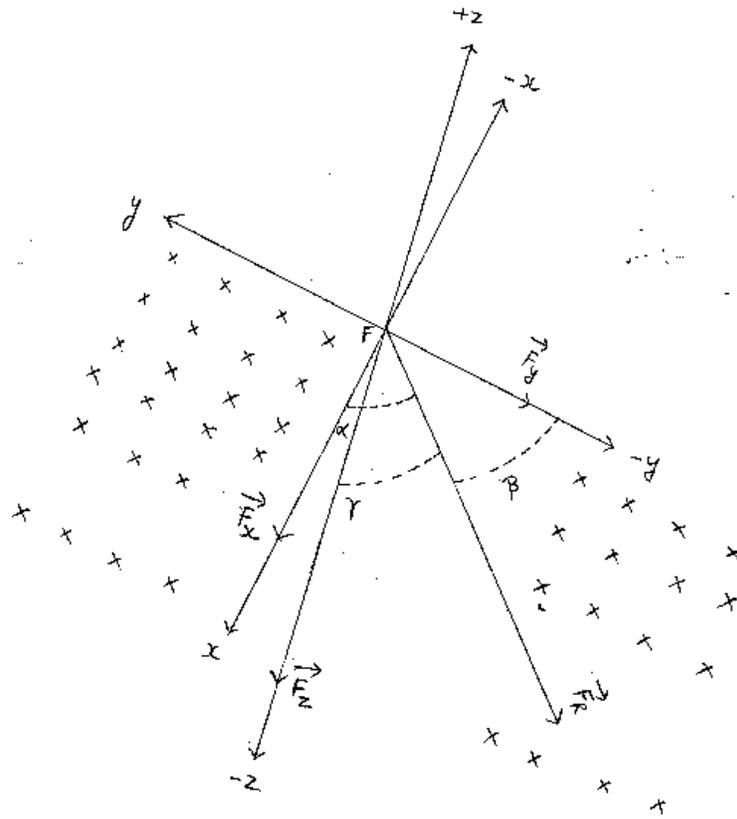
$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 3.8576 \times 10^{-13} \text{ N}$$

$$F_y = 2.2273 \times 10^{-13} \text{ N}$$

$$F_z = 2.2280 \times 10^{-13}$$

$$\begin{aligned}F_R^2 &= (3.8576 \times 10^{-13})^2 + (2.2273 \times 10^{-13})^2 + (2.2280 \times 10^{-13})^2 \text{ N}^2 \\&= (14.88107776 \times 10^{-26}) + (4.96086529 \times 10^{-26}) + (4.963984 \times 10^{-26}) \text{ N}^2 \\F_R^2 &= 24.80592705 \times 10^{-26} \text{ N}^2 \\F_R &= 4.9805 \times 10^{-13} \text{ N}\end{aligned}$$



Radius of the circular path :

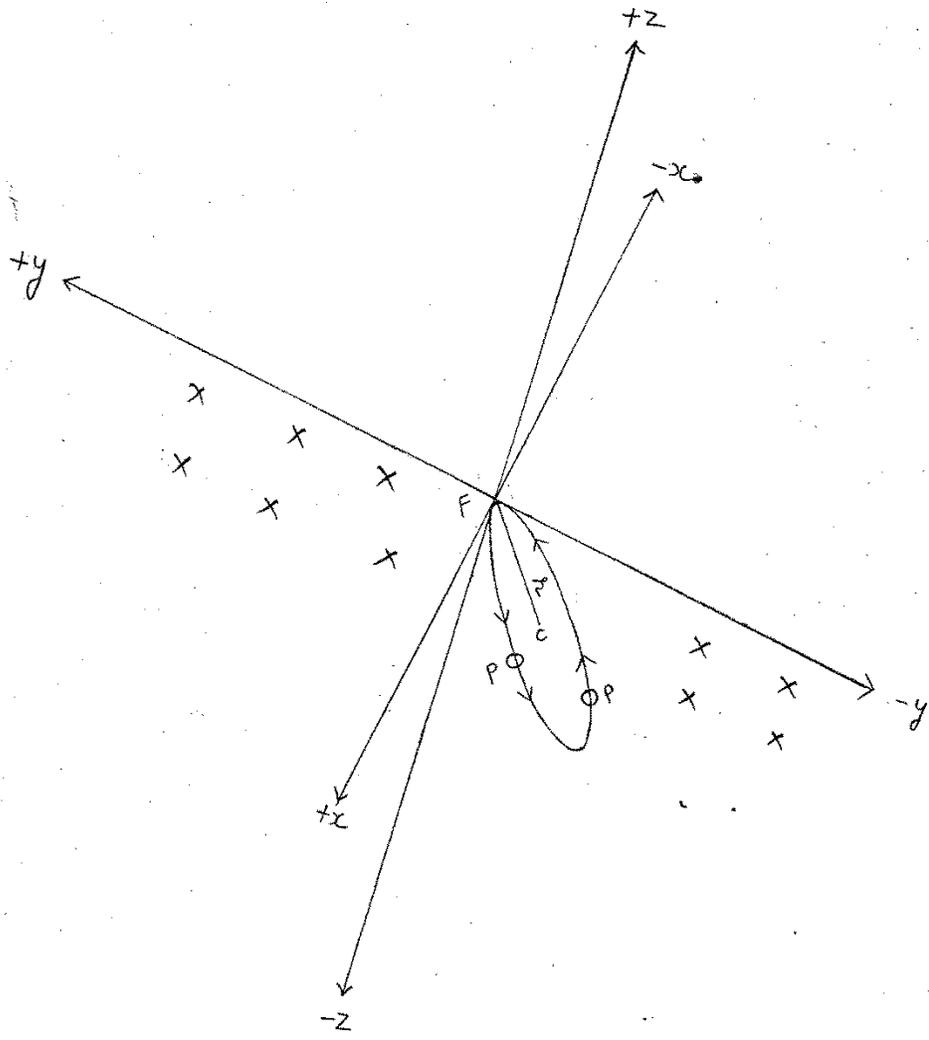
Resultant force acts as a centripetal force on the proton . so, the proton tries to follow a confined circular path.

The radius of the circular orbit to be obtained by the proton is –

$$r = mv^2 / F_R$$

$$r = \frac{12.9382 \times 10^{-13} \text{ J}}{4.9805 \times 10^{-13} \text{ N}}$$

$$r = 2.5977 \text{ m}$$



The plane of the circular orbit to be followed by the proton makes angles with respect to positive x, y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_{R \cos \alpha}}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = 3.8576 \times 10^{-13} \text{ N}$$

$$F_r = 4.9805 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos (39.24) = 0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = - 2.2273 \times 10^{-13} \text{ N}$$

$$F_r = 4.9805 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = - 0.4472$$

$$\beta = 243.43 \text{ degree } [\because \cos (243.43) = -0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{\vec{F}_z}{F_r}$$

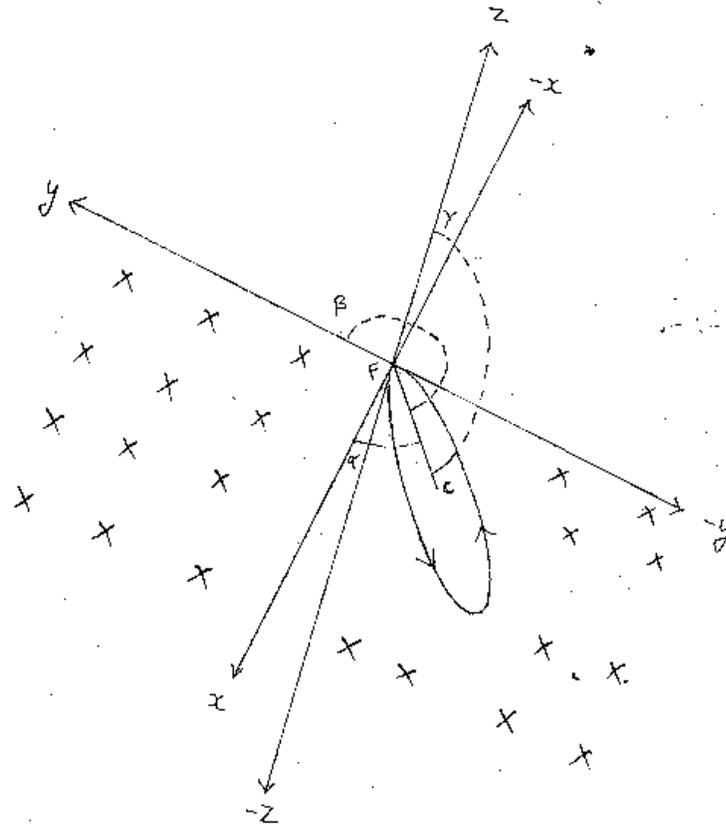
$$\vec{F}_z = - 2.2280 \times 10^{-13} \text{ N}$$

$$F_r = 4.9805 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = - 0.4473$$

$$\gamma = 243.425 \text{ degree}$$



The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2(x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the proton

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$= 2 \times 2.5977 \text{ m}$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 5.1954 \times 0.7745 \text{ m}$$

$$x_2 - x_1 = 4.0238 \text{ m}$$

$$x_2 = 4.0238 \text{ m } [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 5.1954 \times (-0.4472) \text{ m}$$

$$y_2 - y_1 = -2.3233 \text{ m}$$

$$y_2 = -2.3233 \text{ m } [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 5.1954 \times (-0.4473) \text{ m}$$

$$z_2 - z_1 = -2.3239 \text{ m}$$

$$z_2 = -2.3239 \text{ m } [\because z_1 = 0]$$

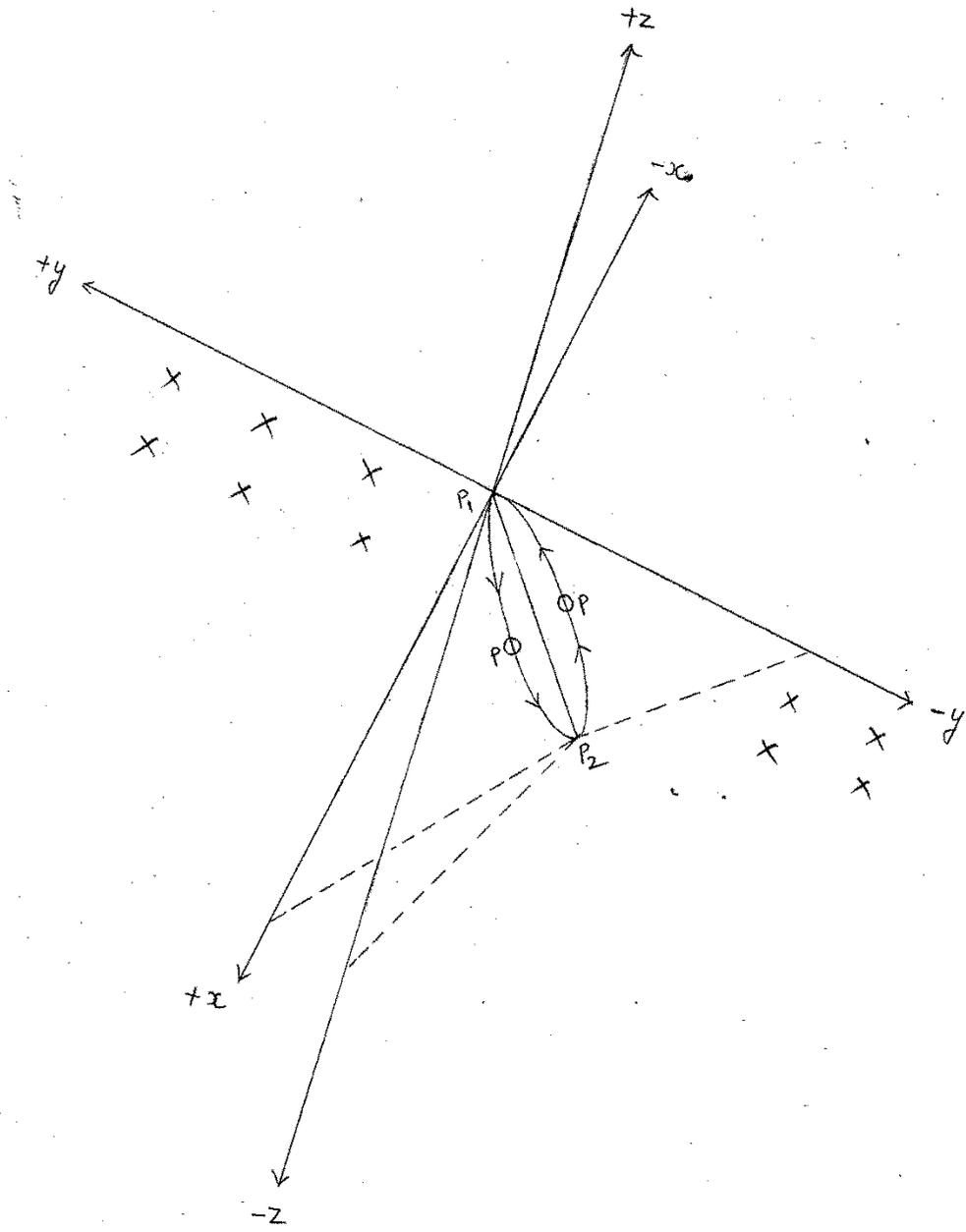
$$d = 2 \times r$$

$$= 5.1954 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$\cos \beta = -0.4472$$

$$\cos \gamma = -0.4473$$



Conclusion :-

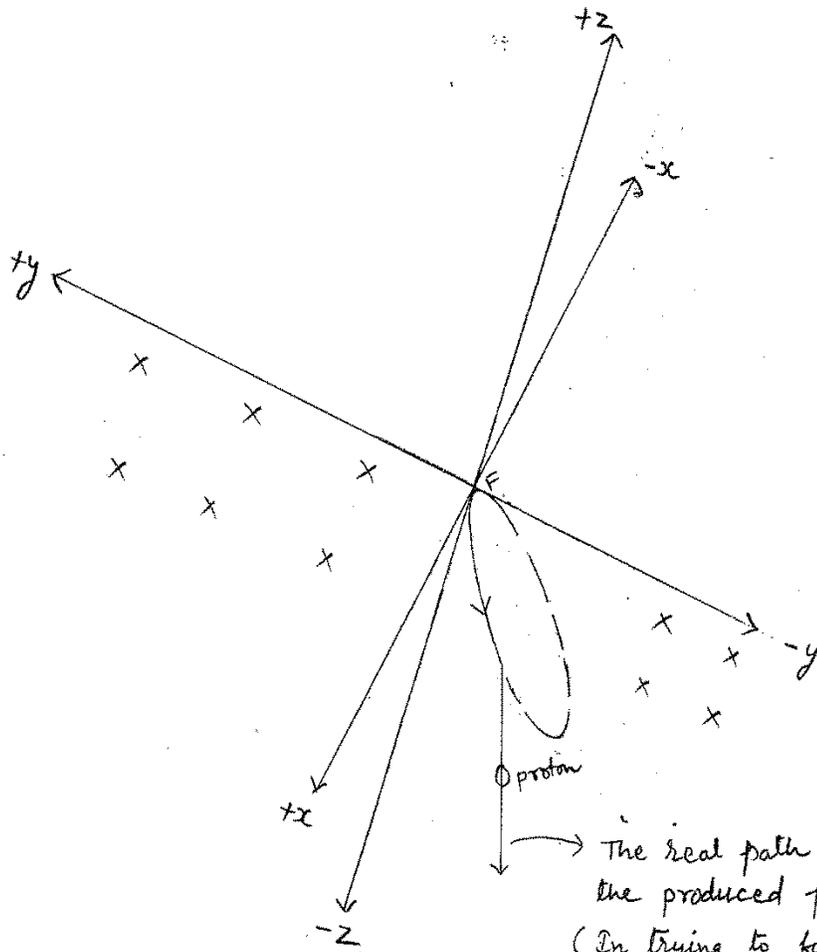
The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x**, **-y** and **-z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 2.5977 m.

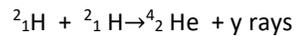
It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(4.0238 \text{ m}, -2.3233 \text{ m}, -2.3239 \text{ m})$. in trying to complete its circle , due to lack of space ,it strike to the base wall of the tokamak.

Hence the proton is not confined.



The real path followed by the produced proton.
 (In trying to follow the circular orbit the produced proton strikes to base wall of the tokamak. So, it can not complete its circle.)

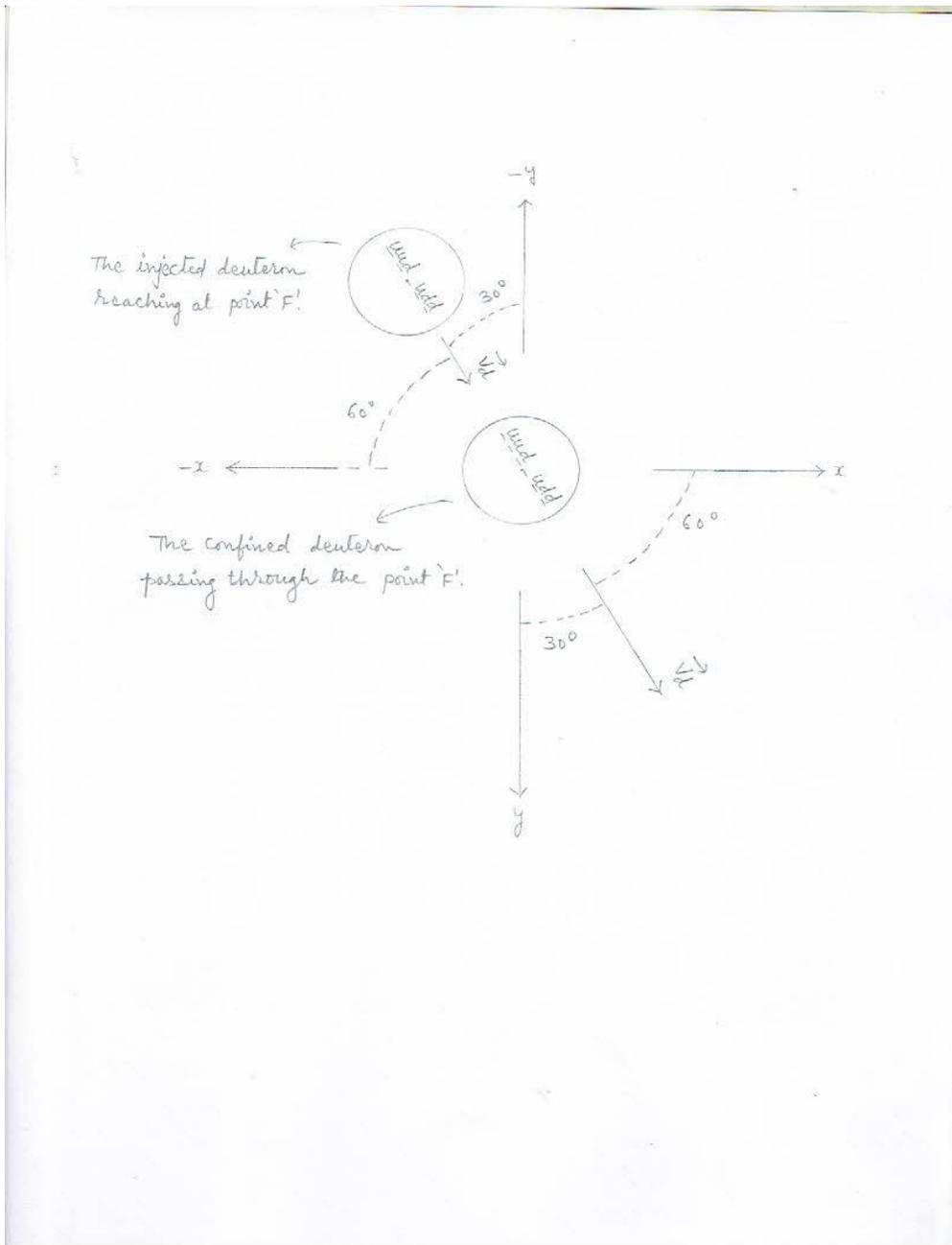
For fusion reaction



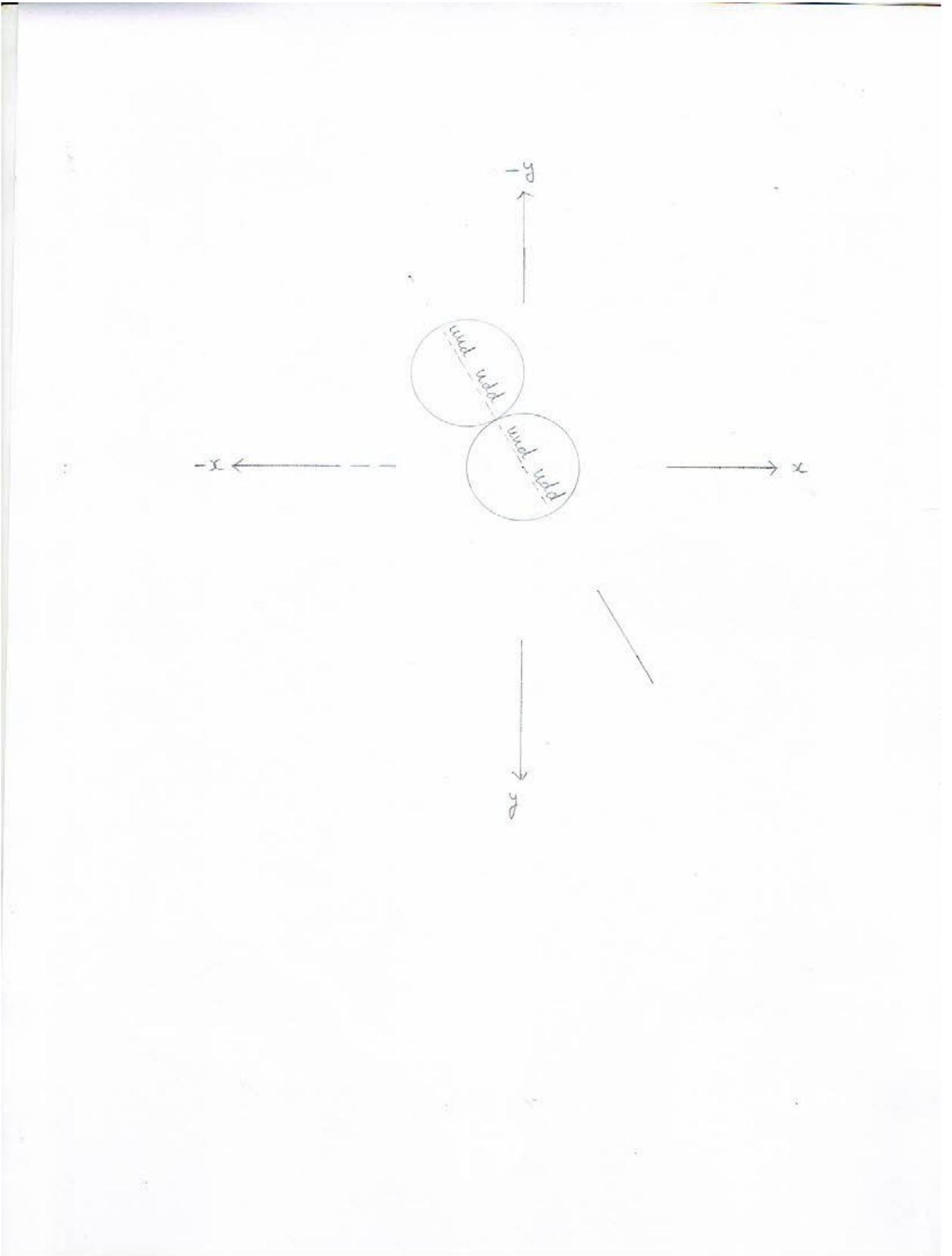
interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined deuteron] with the confined deuteron passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined deuteron.

interaction of nuclei(1)



interaction of nuclei (2)

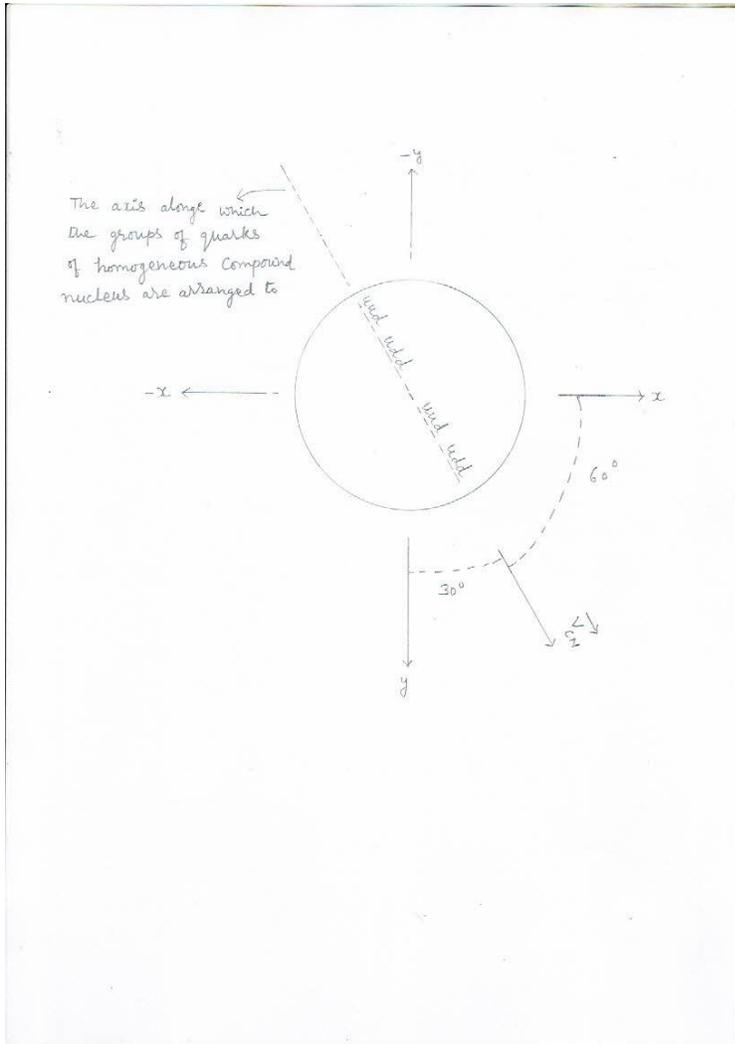


1. Formation of the homogeneous compound nucleus :-

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron) behave like a liquid and form a homogeneous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus in a homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 4 groups of quarks with surrounded gluons.

The homogenous compound nucleus



The axis along which the group of quarks of the homogenous compound nucleus are arranged is parallel to direction of velocity of compound nucleus.

V_{CN} = velocity of the compound nucleus

3 Formation of lobes within into the homogeneous compound nucleus [^4_2m] or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

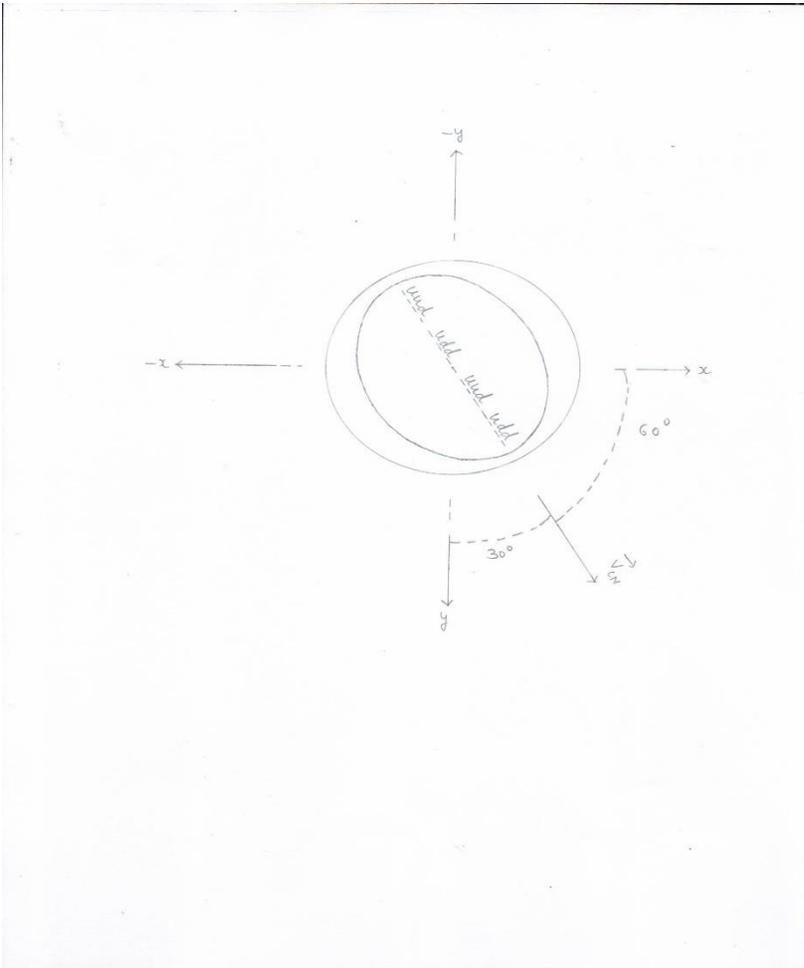
The homogenous compound nucleus ${}^4_2\text{m}$ is unstable . so, for stability ,the central group of quarks with its surrounding gluons to become a stable and the just lower nucleus (the helion-4) than the homognous one ${}^4_2\text{m}$ includes the other 3 groups of quarks with their surrounding gluons and rearrange to form the 'A ' lobe of the heterogeneous compound nucleus.

While , the remaining gluons [the gluons (or mass) that is not included in the formation of the lobe 'A '] rearrange to form the 'B' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

The homogenous compound nucleus ${}^4_2\text{m}$ has more mass than the helium-4 nucleus.

Formation of lobes Within into the homogeneous compound nucleus :-



where,

1 inner side - lobe 'A' formed [that is helium-4 nucleus is formed]

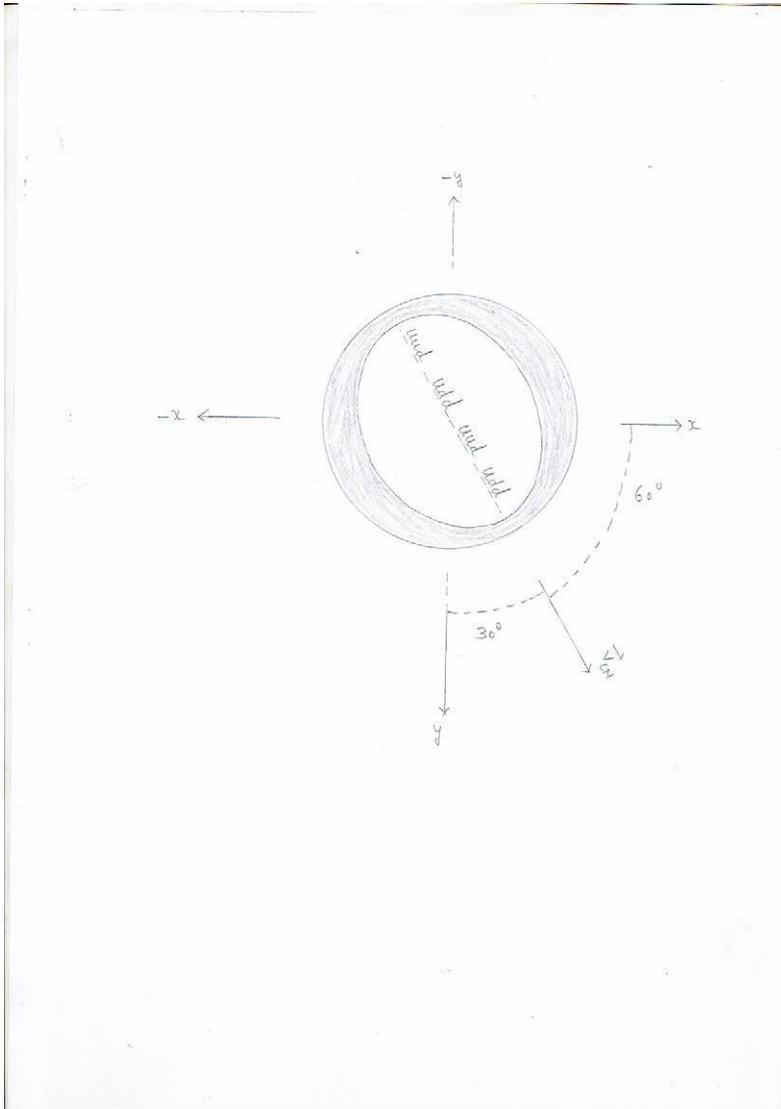
outer side – The remaining gluons [or the reduced mass] .

4..Final stage of the heterogeneous compound nucleus :-

The remaining gluons (that compose the 'B' lobe of the heterogeneous compound nucleus) remain loosely bonded to the helium-4 nucleus [that compose the 'A' lobe of the heterogeneous

compound nucleus] thus the heterogenous compound nucleus , finally, becomes like a coconut into which the outer shield is made up of the remaining gluons while the inner part is made up of the helium-4 nucleus.

Final stage of the heterogenous compound nucleus :-



The splitting of the heterogenous compound nucleus

The remaining gluons are loosely bonded to the helium-4 nucleus.

At the poles of the helium-4 nucleus, the remaining gluons are lesser in amount than at the equator . So, during the rearrangement of the remaining gluons [or during the formation of the 'B' lobe of the heterogenous compound nucleus] , the remaining gluons to be homogenously distributed all around , rush from the eqator to the poles.

In this way, the loosely bonded remaining gluons separates from the helium-4 nucleus and also divides itself into two parts giving us three particles –the first one is the one-half of the reduced mass, second one is the helium-4nucleus and the third one is theanother half of the reduced mass.

Thus the heterogenous compound nucleus splits according to the lines perpendicular to the velocity of the compound nucleus into three paticles the first one is the one-half of the reduced mass ($\Delta m/2$) , the second one is the helium -4 nucleus and the third one is the another one-half of the reduced mass ($\Delta m/2$).

By the law of inertia, each particle that has separated from the compound nucleus has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}) .

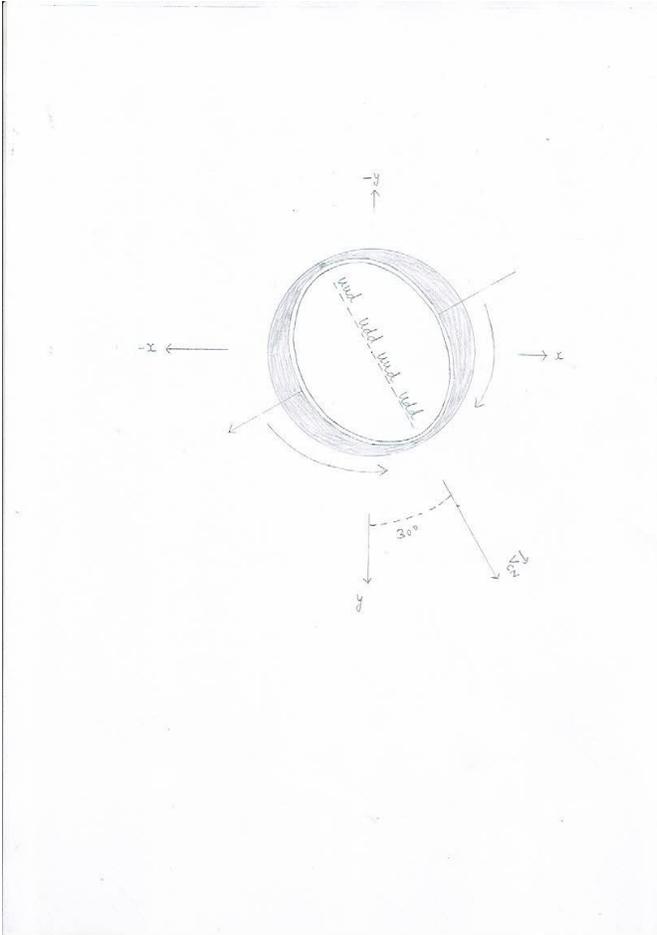
So, for conservation of momentum

$$M\vec{V}_{cn} = (\Delta m/2 + m_{\text{He-4}} + \Delta m/2)\vec{V}_{cn}$$

Where ,

- M = mass of the compound nucleus
- \vec{V}_{cn} = velocity of the compound nucleus
- $m_{\text{He-4}}$ = mass of the helium-4 nucleus
- $\Delta m/2$ = one –half of the reduced mass

The splitting of the heterogenous compound nucleus :-



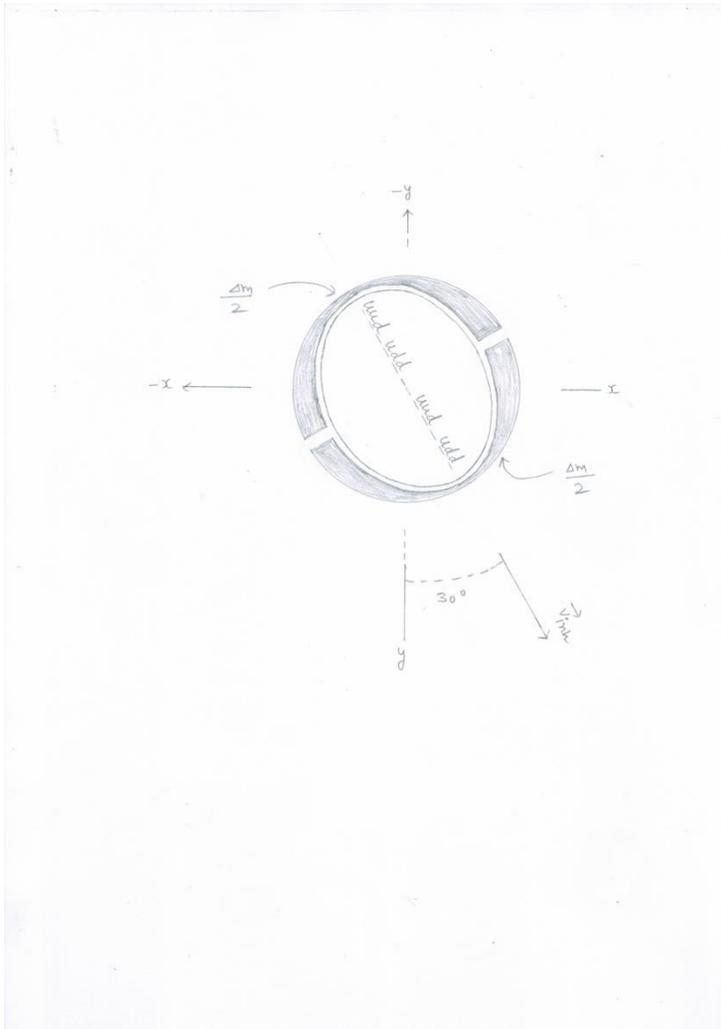
The remaining gluons are loosely bonded to the helium-4 nucleus.

At the poles of the helium-4 nucleus, the remaining gluons are lesser in amount than at the equator. So, during the rearrangement of the remaining gluons [or during the formation of the 'B' lobe of the heterogenous compound nucleus] the remaining gluons, for balance, rush from the equator to poles.

In this way, the loosely bonded remaining gluons separate from the helium-4 nucleus giving us three particles: helium-4 nucleus, $\Delta m/2$ and $\Delta m/2$.

Thus, the heterogenous compound nucleus splits according to the lines perpendicular to the velocity of the compound nucleus into three particles: one half of reduced mass ($\Delta m/2$), helium-4 nucleus and another half of the reduced mass ($\Delta m/2$).

The splitting of the heterogenous compound nucleus :-



The heterogeneous compound nucleus splits into three particles – The one-half of the reduced mass, the helium-4 nucleus (inside) and another half of the reduced mass.

Inherited velocity (\vec{v}_{inh}) of the particles :-

Each particle that is produced due to the splitting of the compound nucleus has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{v}_{cn}).

I. Inherited velocity of the helium-4 nucleus

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the helium – 4 nucleus

$$1 \quad \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1885 \times 10^7 \text{ m/s}$$

$$2 \quad \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.3264 \times 10^7 \text{ m/s}$$

$$3 \quad \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

ii Inherited velocity of the each one-half of the reduced mass

$$V_{inh} = V_{CN} = 0.3770 \times 10^7 \text{ m/s}$$

Propulsion of the particles

1.. Reduced mass

$$\Delta m = [m_d + m_d] - [m_{He-4}]$$

$$\Delta m = [2 \times 2.01355] - [4.0015] \text{ amu}$$

$$\Delta m = [4.0271] - [4.0015] \text{ amu}$$

$$\Delta m = 0.0256 \text{ amu}$$

$$\Delta m = 0.0256 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$\Delta m = 0.0425088 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass .

$$E_{inh} = \frac{1}{2} \Delta m V^2 = \frac{1}{2} \Delta m V_{CN}^2$$

$$V_{CN}^2 = 0.14216694382 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$E_{inh} = \frac{1}{2} \times 0.0425088 \times 10^{-27} \times 0.14216694382 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00302167309 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.001888 \text{ Mev}$$

$$E_{\text{Released}} = \Delta m C^2$$

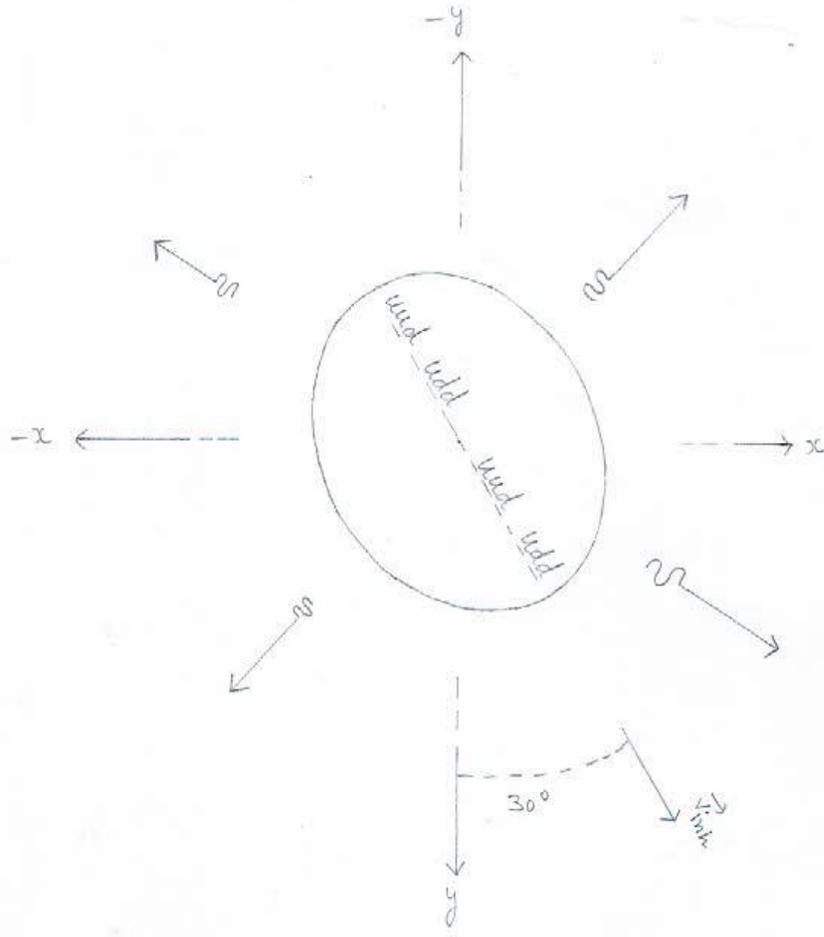
$$= 0.0256 \times 931 \text{ Mev}$$

$$= 23.8336 \text{ Mev}$$

$$E_{\text{Total}} = E_{\text{Inherited}} + E_{\text{Released}}$$

$$= [0.001888] + [23.8336] \text{ Mev}$$

$$= 23.835488 \text{ Mev}$$



.. Components of the final velocity(\vec{V}_f)of helium-4 nucleus

Forhelium-4

According to -	Inherited Velocity(\vec{V}_{inh})	Increased Velocity(\vec{V}_{inc})	Final velocity (\vec{V}_f)= $(\vec{V}_{inh})+(\vec{V}_{inc})$
X –axis	$\vec{v}_x = 0.1885 \times 10^7 \text{ m/s}$	$\vec{v}_x = 0 \text{ m/s}$	$\vec{v}_x = 0.1885 \times 10^7 \text{ m/s}$
y – axis	$\vec{v}_y = 0.3264 \times 10^7 \text{ m/s}$	$\vec{v}_y = 0 \text{ m/s}$	$\vec{v}_y = 0.3264 \times 10^7 \text{ m/s}$
z – axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

Final velocity (\vec{v}_f)of the helion-4 nucleus :-

$$V_f^2 = V_x^2 + V_y^2 + V_z^2$$

$$= 0.3770$$

Final kinetic energy of the helium-4 nucleus

$$E = \frac{1}{2} m_{\text{He-4}} V_f^2$$

$$V_f^2 = 0.14216694382 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$E = \frac{1}{2} \times 6.64449 \times 10^{-27} \times 0.14216694382 \times 10^{14} \text{ J}$$

$$= 0.47231341827 \times 10^{-13} \text{ J}$$

$$= 0.2951958 \text{ MeV}$$

$$m_{\text{He-4}} V_f^2 = 6.64449 \times 10^{-27} \times 0.14216694382 \times 10^{14} \text{ J}$$

$$= 0.9446 \times 10^{-13} \text{ J}$$

Forces acting on the helium-4 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\rightarrow_{V_x} = 0.1885 \times 10^7 \text{ m/s}$$

$$\rightarrow_{B_z} = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_y &= 2 \times 1.6 \times 10^{-19} \times 0.1885 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 0.6038 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = -0.6038 \times 10^{-13} \text{ N}$$

$$2 F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_z &= 2 \times 1.6 \times 10^{-19} \times 0.1885 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N} \\ &= 0.6039 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = -0.6039 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = 0.3264 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

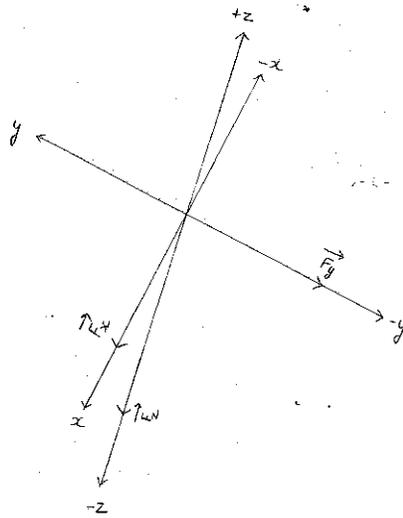
$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_x &= 2 \times 1.6 \times 10^{-19} \times 0.3264 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 1.0455 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x axis, so,

$$\vec{F}_x = 1.0455 \times 10^{-13} \text{ N}$$

The forces acting on the helium-4 nucleus



Resultant force acting on the helium-4 nucleus (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 1.0455 \times 10^{-13} \text{ N}$$

$$F_y = 0.6038 \times 10^{-13} \text{ N}$$

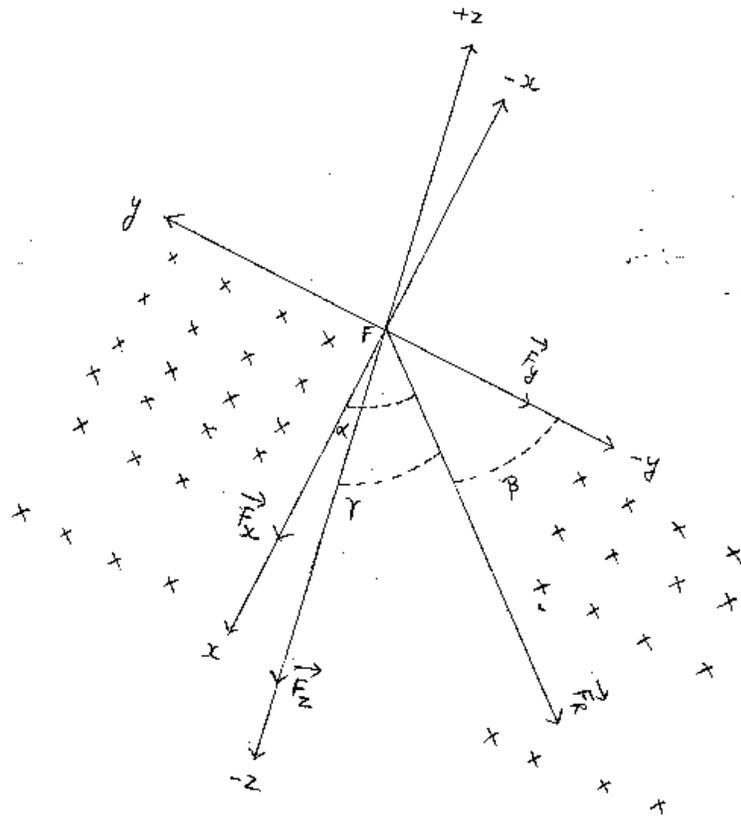
$$F_z = 0.6039 \times 10^{-13} \text{ N}$$

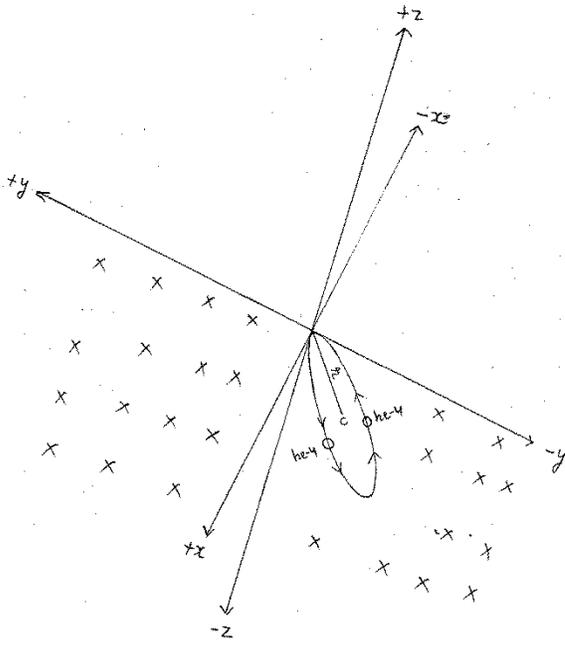
$$F_R^2 = (1.0455 \times 10^{-13})^2 + (0.6038 \times 10^{-13})^2 + (0.6039 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (1.09307025 \times 10^{-26}) + (0.36457444 \times 10^{-26}) + (0.36469521 \times 10^{-26}) \quad N^2$$

$$F_R^2 = 1.8223399 \times 10^{-26} \quad N^2$$

$$F_R = 1.3499 \times 10^{-13} N$$





The circular orbit followed by the helium-4 lies in the plane made up of positive x-axis, negative y-axis and the negative z-axis.

\vec{Fr} = The resultant force .

C= center of the circular orbit followed by the helium-4 nucleus.

The plane of the circular orbit followed by the helium -4 makes angles with positive x , y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = 1.0455 \times 10^{-13} \text{ N}$$

$$F_r = 1.3499 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos (39.24) = 0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = -0.6038 \times 10^{-13} \text{ N}$$

$$F_r = 1.3499 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4472$$

$$\beta = 243.43 \text{ degree } [\because \cos (243.43) = -0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{F_z}{F_r}$$

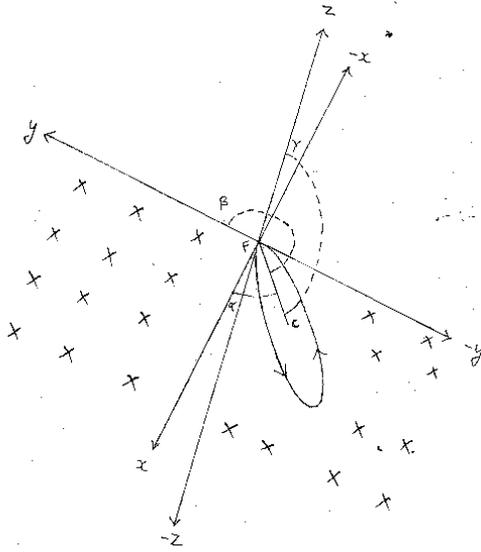
$$\frac{F_z}{F_r} = -0.6039 \times 10^{-13} \text{ N}$$

$$F_r = 1.3499 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.425 \text{ degree}$$



The plane of the circular orbit followed by the helium -4 makes angles with respect to positive x, y and z-axes as follows :-

Where,

$$\alpha = 39.24 \text{ degree}$$

$$\beta = 243.43 \text{ degree}$$

$$\gamma = 243.425 \text{ degree}$$

Radius of the circular orbit followed by the helium -4 nucleus :

$$r = mv^2 / F_R$$

$$mv^2 = 0.9446 \times 10^{-13} \text{ J}$$

$$F_r = 1.3499 \times 10^{-13} \text{ N}$$

$$r = \frac{0.9446 \times 10^{-13} \text{ J}}{1.3499 \times 10^{-13} \text{ N}}$$

$$r = 0.6997 \text{ m}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the helion-4 nucleus.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$d$$

$$= 2 \times 0.6997 \text{ m}$$

$$d = 2 \times r$$

$$= 1.3994 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 1.3994 \times 0.7745 \text{ m}$$

$$x_2 - x_1 = 1.0838 \text{ m}$$

$$x_2 = 1.0838 \text{ m} [\because x_1 = 0]$$

$$\cos\beta = \frac{y_2 - y_1}{d}$$

$$\cos\beta = -0.4472$$

$$y_2 - y_1 = d \times \cos\beta$$

$$y_2 - y_1 = 1.3994 \times (-0.4472) \text{ m}$$

$$y_2 - y_1 = -0.6258 \text{ m}$$

$$y_2 = -0.6258 \text{ m} \quad [\because y_1 = 0]$$

$$\cos\gamma = \frac{z_2 - z_1}{d}$$

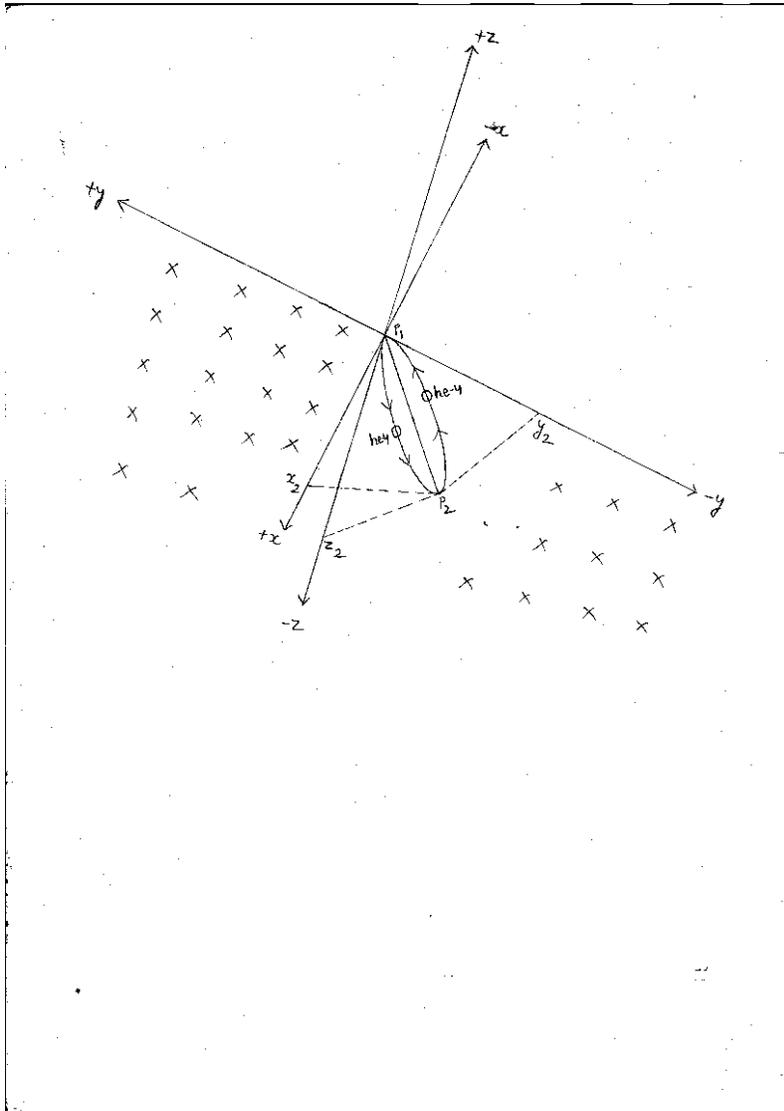
$$\cos\gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos\gamma$$

$$z_2 - z_1 = 1.3994 \times (-0.4473) \text{ m}$$

$$z_2 - z_1 = -0.6259 \text{ m}$$

$$z_2 = -0.6259 \text{ m} \quad [\because z_1 = 0]$$



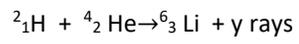
Conclusion :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-4 nucleus are along **+x, -y and -z** axes respectively. So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-4 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the helium-4 nucleus to undergo to a circular orbit of radius of 0.6997 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.0838 \text{ m}, -0.6258 \text{ m}, -0.6259 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

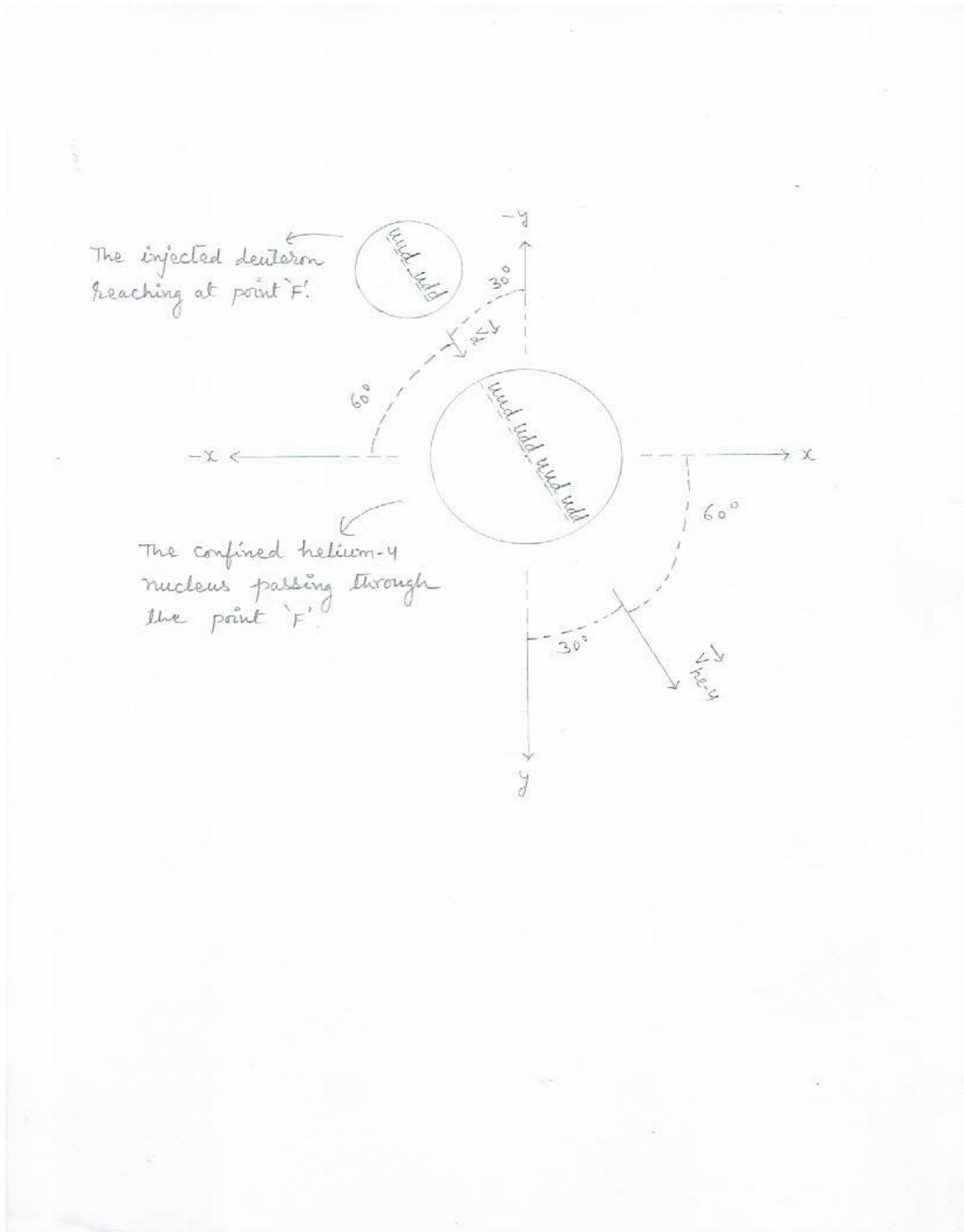
For fusion reaction



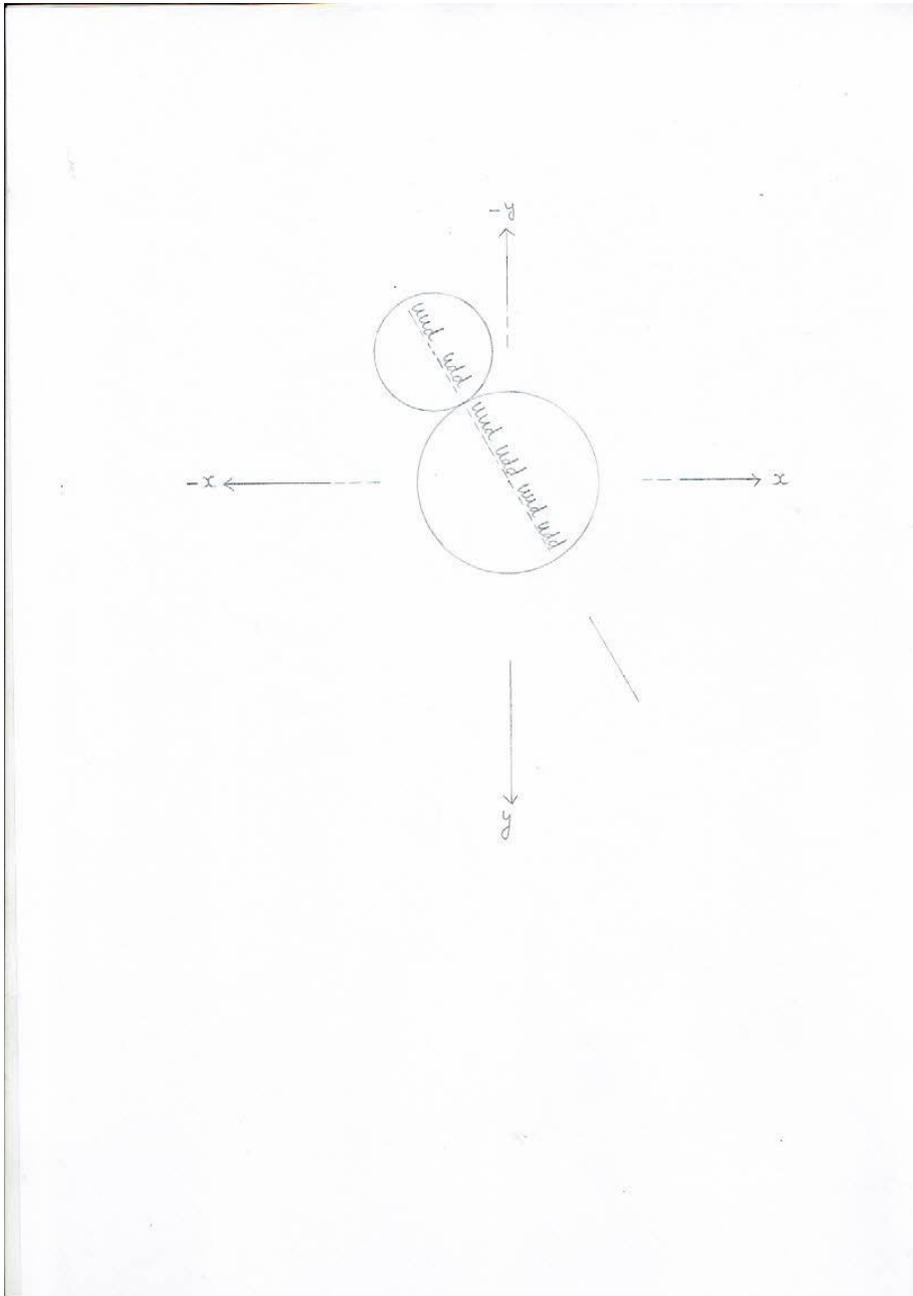
interaction of nuclei : -

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined helion-4] with the confined helion-4 passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined helion-4.

interaction of nuclei(1)



interaction of nuclei(2)

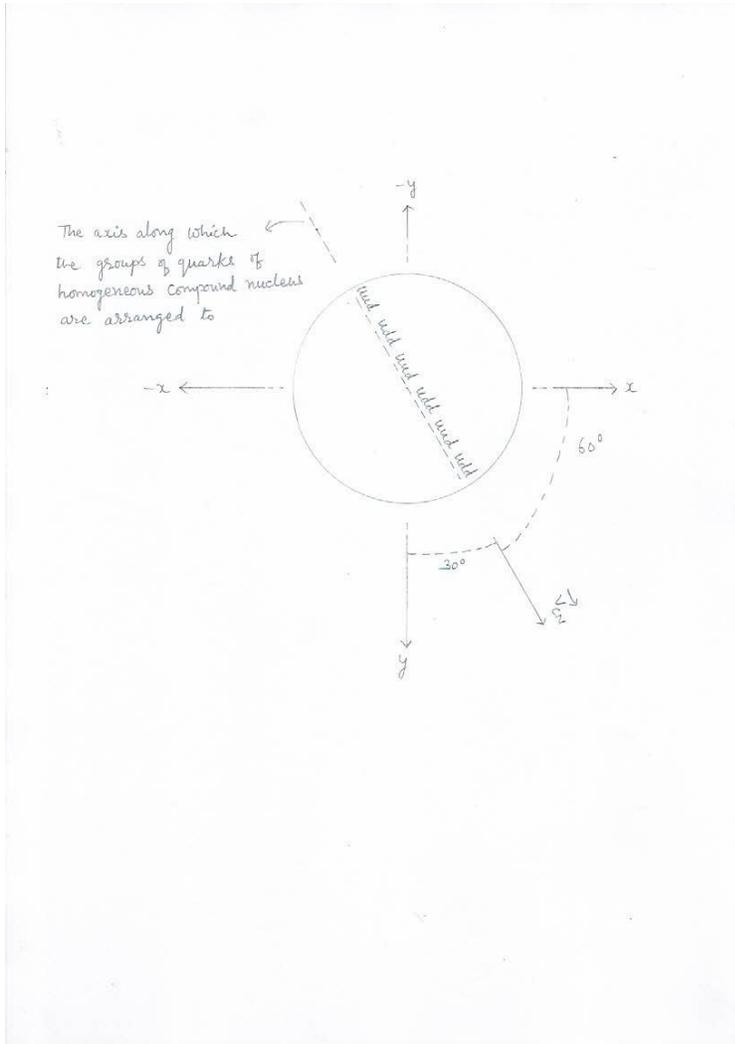


1..Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron and helion-4) behave like a liquid and form a homogeneous compound nucleus . having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus in a homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 6 groups of quarks with surrounded gluons.

The homogenous compound nucleus



The axis along which the group of quarks of the homogenous compound nucleus are arranged to is parallel to the direction of the velocity of compound nucleus.

V_{CN} = velocity of the compound nucleus

3. Formation of lobes within into the homogeneous compound nucleus [^4_2m] or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

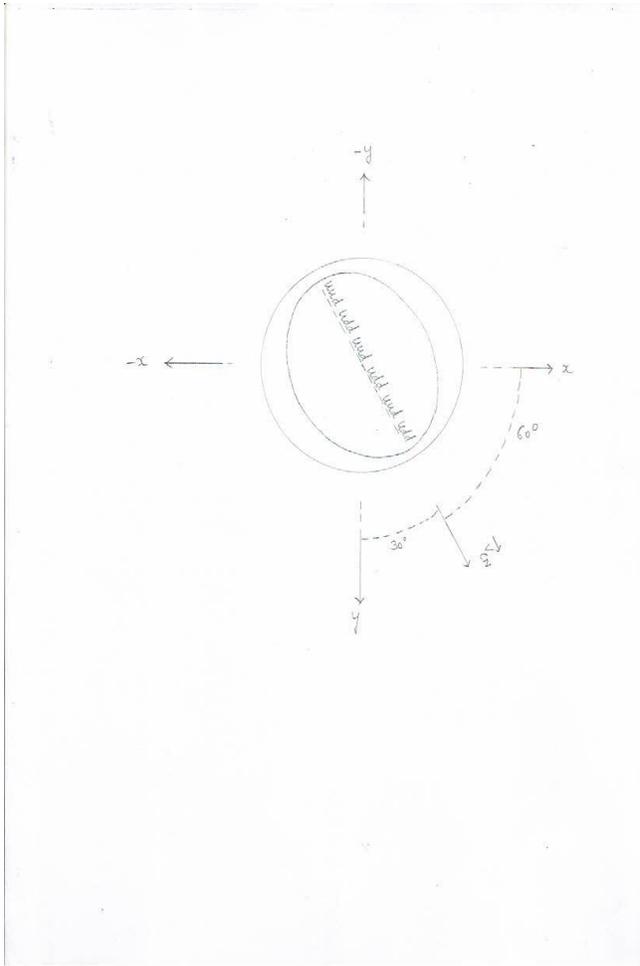
The homogenous compound nucleus [${}^6_3\text{Li}$] is unstable . so, for stability ,the central group of quarks with its surrounding gluons to become a stable and the just lower nucleus (the lithion-6) than the homognous one [${}^6_3\text{Li}$] includes the other 6 groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

While , the remaing gluons [the gluons (or mass) that is not included in the formation of the lobe ' A '] rearrange to form the 'B' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

The homogenous compound nucleus [${}^6_3\text{Li}$] has more mass than the lithion-6 nucleus.

Formation of lobes Within into the homogeneous compound nucleus :-



where,

1 inner side - lobe 'A' formed [that is helium-4 nucleus is formed]

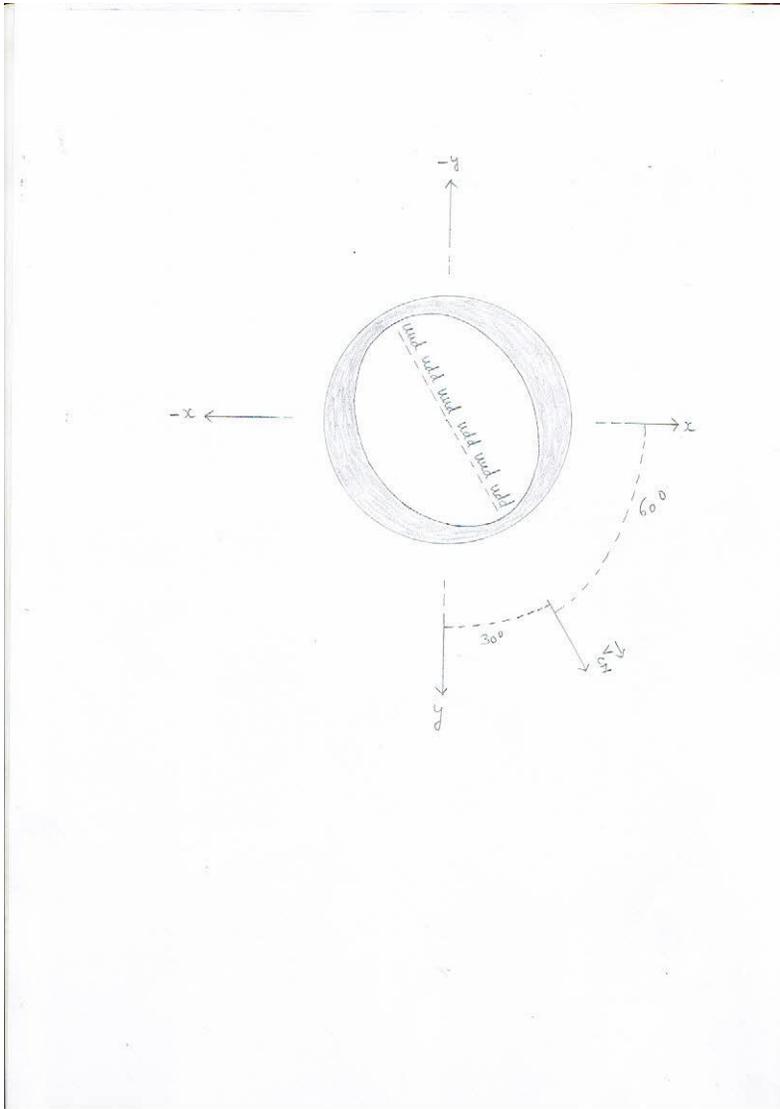
outer side – The remaining gluons [or the reduced mass] .

4..Final stage of the heterogeneous compound nucleus :-

The remaining gluons (that compose the 'B' lobe of the heterogeneous compound nucleus) remaining loosely bonded to the lithium-6 nucleus [that compose the 'A' lobe of the heterogeneous

compound nucleus] thus the heterogenous compound nucleus , finally, becomes like a coconut into which the outer shield is made up of the remaining gluons while the inner part is made up of the lithium-6 nucleus.

Final stage of the heterogenous compound nucleus :-



Formation of compound nucleus :

As the deuteron of n^{th} bunch reaches at point F , it fuses with the confined helium-4 to form a compound nucleus .

(1) Just before fusion, to overcome the electrostatic repulsive force exerted by the helium-4, the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves) its energy equal to 20.2488 keV.

$$\begin{aligned} &\text{so, just before fusion,} \\ &\text{the kinetic energy of } n^{\text{th}} \text{ deuteron is -} \\ E_b &= 153.6 \text{ keV} - 20.2488 \text{ keV} \\ &= 133.3512 \text{ keV} \\ &= 0.1333512 \text{ MeV} \end{aligned}$$

(2) Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron, the confined helium-4 loses (radiates its energy in the form of electromagnetic waves) its energy equal to 40.2420 keV.

$$\begin{aligned} &\text{so, just before fusion,} \\ &\text{the kinetic energy of helium-4 is -} \\ E_b &= 295.1958 \text{ keV} - 40.242 \text{ keV} \\ &= 254.9538 \text{ keV} \\ &= 0.2549538 \text{ MeV} \end{aligned}$$

Kinetic energy of the compound nucleus

$$\begin{aligned} \text{K.E.} &= [E_b \text{ of } {}^2_1\text{D}] + [E_b \text{ of } {}^4_2\text{He}] \\ &= [133.3512 \text{ KeV}] + [254.9538 \text{ KeV}] \\ &= 388.305 \text{ KeV.} \end{aligned}$$

$$= 0.388305 \text{ Mev}$$

$$M = m_d + m_{\text{he-4}}$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [6.64449 \times 10^{-27} \text{ Kg}]$$

$$= 9.98789 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.388305 \text{ Mev}$$

$$V_{\text{CN}} = \left(\frac{2 \times 0.388305 \times 1.6 \times 10^{-13}}{9.98789 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}} \text{ m/s}$$

$$V_{\text{CN}} = \left(\frac{1.242576 \times 10^{-13}}{9.98789 \times 10^{-27}} \text{ m/s} \right)$$

$$V_{\text{CN}} = [0.1244082584 \times 10^{14}]^{\frac{1}{2}} \text{ m/s}$$

$$V_{\text{CN}} = 0.3527 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$\rightarrow V_x = V_{\text{CN}} \cos \alpha$$

$$= 0.3527 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 0.1763 \times 10^7 \text{ m/s}$$

$$\rightarrow V_y = V_{\text{CN}} \cos \beta$$

$$= 0.3527 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 0.3054 \text{ m/s}$$

$$\rightarrow V_z = V_{\text{CN}} \cos \gamma$$

$$= 0.3527 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

The splitting of the heterogenous compound nucleus

The remaining gluons are loosely bonded to the **lithium-6** nucleus.

At the poles of the **lithium-6** nucleus, the remaining gluons are lesser in amount than at the equator . So, during the rearrangement of the remaining gluons [or during the formation of the 'B' lobe of the heterogenous compound nucleus] , the remaining gluons to be homogenously distributed all around , rush from the eqator to the poles.

In this way, the loosely bonded remaining gluons separates from the lithium -6 nucleus and also divides itself into two parts giving us three particles –the first one is the one-half of the reduced mass, second one is the **lithium-6** nucleus and the third one is the one-half of the reduced mass.

Thus the heterogenous compound nucleus splits according to the lines perpendicular to the velocity of the compound nucleus into three particles - the first one is the one-half of the reduced mass ($\Delta m/2$) , the second one is the **lithium-6** nucleus and the third one is the another one-half of the reduced mass ($\Delta m/2$).

By the law of inertia, each particle that is produced due to splitting of the compound nucleus, has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}) .

So, for conservation of momentum

$$M\vec{V}_{cn} = (\Delta m/2 + m_{Li-6} + \Delta m/2) \vec{V}_{cn}$$

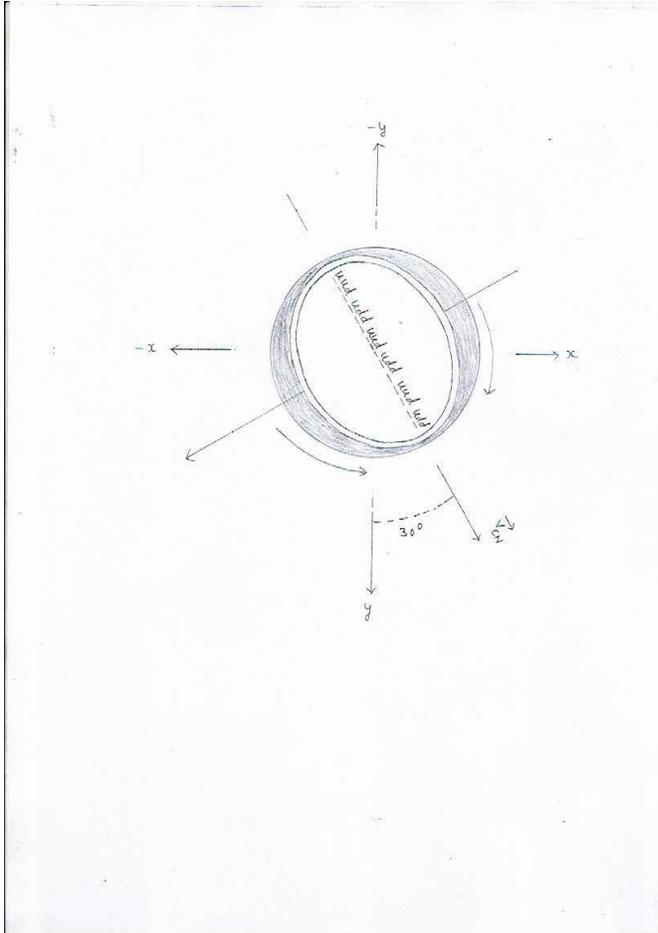
Where ,

$$\begin{array}{ll} M & = \text{mass of the compound nucleus} \\ \vec{V}_{cn} & = \text{velocity of the compound nucleus} \end{array}$$

$m_{\text{Li-6}}$ = mass of the lithium-6 nucleus

$\Delta m/2$ = one-half of the reduced mass

The splitting of the heterogenous compound nucleus :-



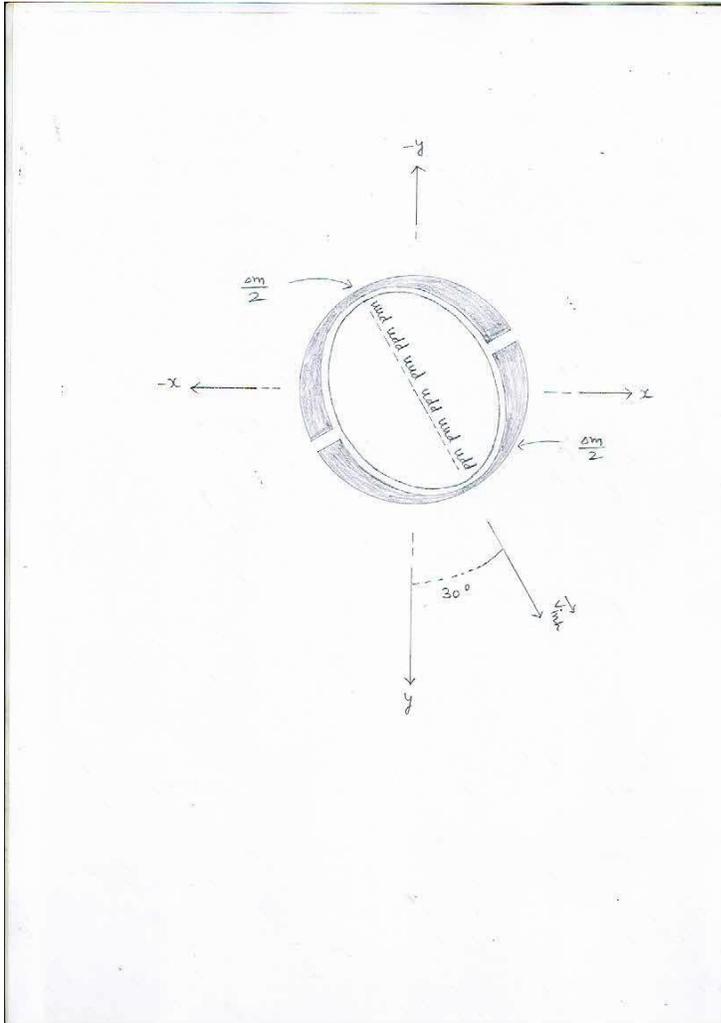
The remaining gluons are loosely bonded to the lithium -6 nucleus.

At the poles of the lithium-6 nucleus, the remaining gluons are lesser in amount than at the equator. So, during the rearrangement of the remaining gluons [or during the formation of the 'B' lobe of the heterogenous compound nucleus] the remaining gluons, to be homogeneously distributed all around (or for balance) , rush from the equator to poles.

In this way, the loosely bonded remaining gluons separate from the lithium -6 nucleus giving us three particles- lithium -6 nucleus, $\Delta m/2$ and $\Delta m/2$

Thus, the heterogenous compound nucleus splits according to the lines perpendicular to the velocity of the compound nucleus into three particles- one half of reduced mass ($\Delta m/2$), lithium -6 nucleus and another half of the reduced mass ($\Delta m/2$).

The splitting of the heterogenous compound nucleus :-



The heterogenous compound nucleus splits into three particles – The one-half of the reduced mass, the lithium -6 nucleus (inside) and another half of the reduced mass.

Inherited velocity (\vec{v}_{inh}) of the particles : -

Each particles that is produced due to splitting of the compound nucleus has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{v}_{CN}).

i . Inherited velocity of the **lithium-6** nucleus

$$V_{inh} = V_{CN} = 0.3527 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the **lithium-6** nucleus

$$1 \rightarrow \vec{v}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1763 \times 10^7 \text{ m/s}$$

$$2 \rightarrow \vec{v}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.3054 \times 10^7 \text{ m/s}$$

$$3 \rightarrow \vec{v}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

ii Inherited velocity of the each one-half of the reduced mass

$$V_{inh} = V_{CN} = 0.3527 \times 10^7 \text{ m/s}$$

Propulsion of the particles

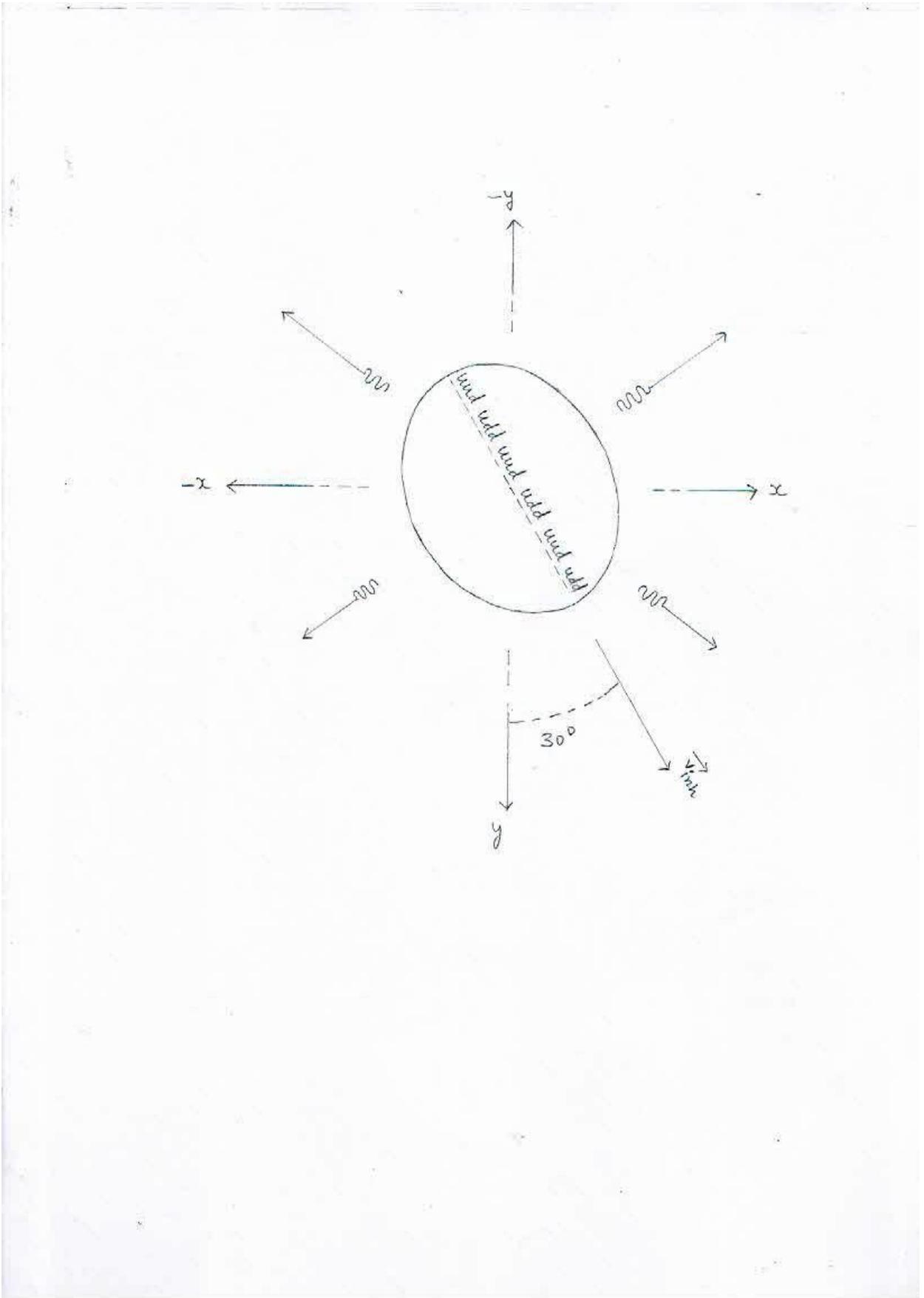
1.. Reduced mass

$$\begin{aligned} \Delta m &= [m_d + m_{\text{he-4}}] - [m_{\text{Li-6}}] \\ \Delta m &= [2.01355 + 4.0015] - [6.01347708] \text{ amu} \\ \Delta m &= [6.01505] - [6.01347708] \text{ amu} \\ \Delta m &= 0.00157292 \text{ amu} \\ \Delta m &= 0.00157292 \times 1.6605 \times 10^{-27} \text{ kg} \\ \Delta m &= 0.00261183366 \times 10^{-27} \text{ kg} \end{aligned}$$

The Inherited kinetic energy of reduced mass .

$$\begin{aligned} E_{\text{inh}} &= \frac{1}{2} \Delta m V^2 = \frac{1}{2} \Delta m V_{\text{CN}}^2 \\ V_{\text{CN}}^2 &= 0.1244082584 \times 10^{14} \text{ m}^2/\text{s}^2 \\ E_{\text{inh}} &= \frac{1}{2} \times 0.00261183366 \times 10^{-27} \times 0.1244082584 \times 10^{14} \text{ J} \\ E_{\text{inh}} &= 0.00016246683 \times 10^{-13} \text{ J} \\ E_{\text{inh}} &= 0.000101 \text{ Mev} \\ E_{\text{Released}} &= \Delta m C^2 \\ &= 0.00157292 \times 931 \text{ Mev} \\ &= 1.4643 \text{ Mev} \end{aligned}$$

$$\begin{aligned} E_{\text{Total}} &= E_{\text{Inherited}} + E_{\text{Released}} \\ &= [0.000101] + [1.4643] \text{ Mev} \\ &= 1.464401 \text{ Mev} \end{aligned}$$



Components of the final velocity(\vec{V}_f)of lithion-6 nucleus

I Forlithion-6

According to -	Inherited Velocity(\vec{V}_{inh})	Increased Velocity(\vec{V}_{inc})	Final velocity (\vec{V}_f) $=(\vec{V}_{inh} + \vec{V}_{inc})$
X – axis	$\vec{v}_x = 0.1763 \times 10^7 \text{ m/s}$	$\vec{v}_x = 0 \text{ m/s}$	$\vec{v}_x = 0.1763 \times 10^7 \text{ m/s}$
y– axis	$\vec{v}_y = 0.3054 \times 10^7 \text{ m/s}$	$\vec{v}_y = 0 \text{ m/s}$	$\vec{v}_y = 0.3054 \times 10^7 \text{ m/s}$
z – axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

$$\vec{V}_f = \vec{V}_{inh} + \vec{V}_{cn} = 0.3527 \times 10^7 \text{ m/s}$$

Final velocity (v_f) of the lithion-6 nucleus:-

$$=0.3527 \text{ m/s}$$

Final kinetic energy of the lithium-6 nucleus

$$E = \frac{1}{2} m_{\text{Li-6}} V_f^2$$

$$V_f^2 = 0.1244082584 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$E = \frac{1}{2} \times 9.9853 \times 10^{-27} \times 0.1244082584 \times 10^{14} \text{ J}$$

$$= 0.6211268913 \times 10^{-13} \text{ J}$$

$$= 0.3882043 \text{ Mev}$$

$$= 388.2043 \text{ Kev}$$

$$m_{\text{Li-6}} V_f^2 = 9.9853 \times 10^{-27} \times 0.1244082584 \times 10^{14} \text{ J}$$

$$= 1.2422 \times 10^{-13} \text{ J}$$

Forces acting on the lithium-6 nucleus

$$1 F_y = q V_x B_z \sin \theta$$

$$\vec{v}_x = 0.1763 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 3 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_y &= 3 \times 1.6 \times 10^{-19} \times 0.1763 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 0.8470 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = -0.8470 \times 10^{-13} \text{ N}$$

$$2 F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_z &= 3 \times 1.6 \times 10^{-19} \times 0.1763 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N} \\ &= 0.8473 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = -0.8473 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = 0.3054 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

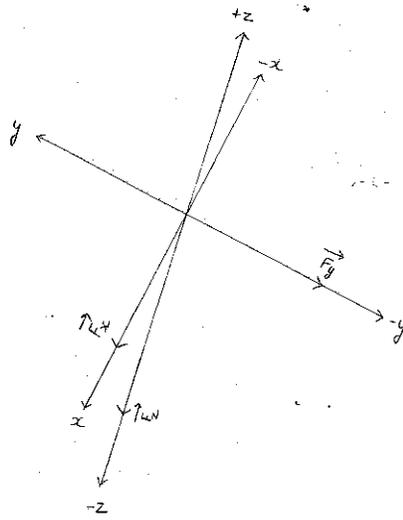
$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_x &= 3 \times 1.6 \times 10^{-19} \times 0.3054 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 1.4673 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x-axis,

$$\vec{F}_x = 1.4673 \times 10^{-13} \text{ N}$$

The forces acting on the lithium - 6



Resultant force acting on the lithium-6 (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 1.4673 \times 10^{-13} \text{ N}$$

$$F_y = 0.8470 \times 10^{-13} \text{ N}$$

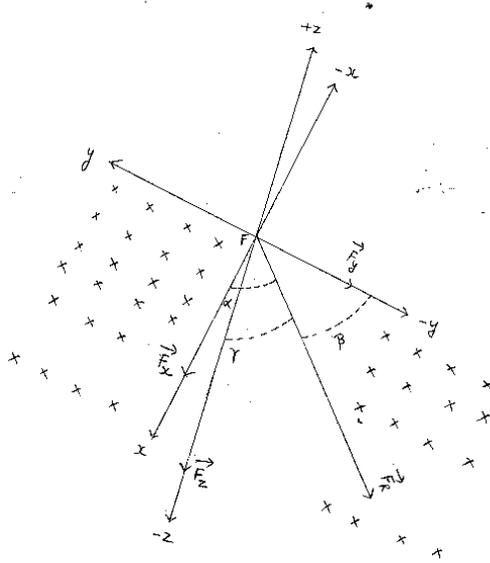
$$F_z = 0.8473 \times 10^{-13} \text{ N}$$

$$F_R^2 = (1.4673 \times 10^{-13})^2 + (0.8470 \times 10^{-13})^2 + (0.8473 \times 10^{-13})^2 \quad \text{N}^2$$

$$F_R^2 = (2.15296929 \times 10^{-26}) + (0.717409 \times 10^{-26}) + (0.71791729 \times 10^{-26}) \quad \text{N}^2$$

$$F_R^2 = 3.58829558 \times 10^{-26} \quad \text{N}^2$$

$$F_R = 1.8942 \times 10^{-13} \quad \text{N}$$



The circular orbit followed by the lithium-6 lies in the plane made up of positive x-axis, negative y-axis and the negative z-axis.

\vec{Fr} = The resultant force .

The plane of the circular orbit followed by the lithium -6 nucleus makes angles with positive x , y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_x}{F_r} \Rightarrow \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = 1.4673 \times 10^{-13} \text{ N}$$

$$F_r = 1.8942 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7746$$

$$\alpha = 39.23^\circ \quad [\because \cos (39.23) = 0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_y}{F_r} \Rightarrow \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = -0.8470 \times 10^{-13} \text{ N}$$

$$F_r = 1.8942 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4471$$

$$\beta = 243.44^\circ \quad [\because \cos (243.44) = -0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_z}{F_r} \Rightarrow \frac{F_z}{F_r}$$

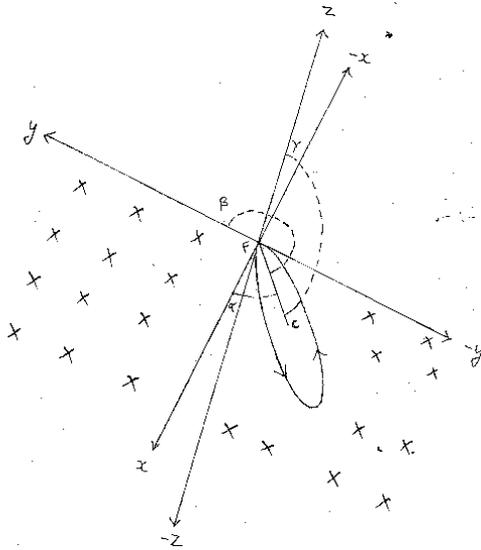
$$\frac{F_z}{F_r} = -0.8473 \times 10^{-13} \text{ N}$$

$$F_r = 1.8942 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.425^\circ \text{ degree}$$



The plane of the circular orbit followed by confined lithium-6 nucleus makes angles with respect to positive x, y and z-axes.

Where,

$$\alpha = 39.23 \text{ degree}$$

$$\beta = 243.44 \text{ degree}$$

$$\gamma = 243.425 \text{ degree}$$

Radius of the circular orbit followed by the lithium-6 nucleus :

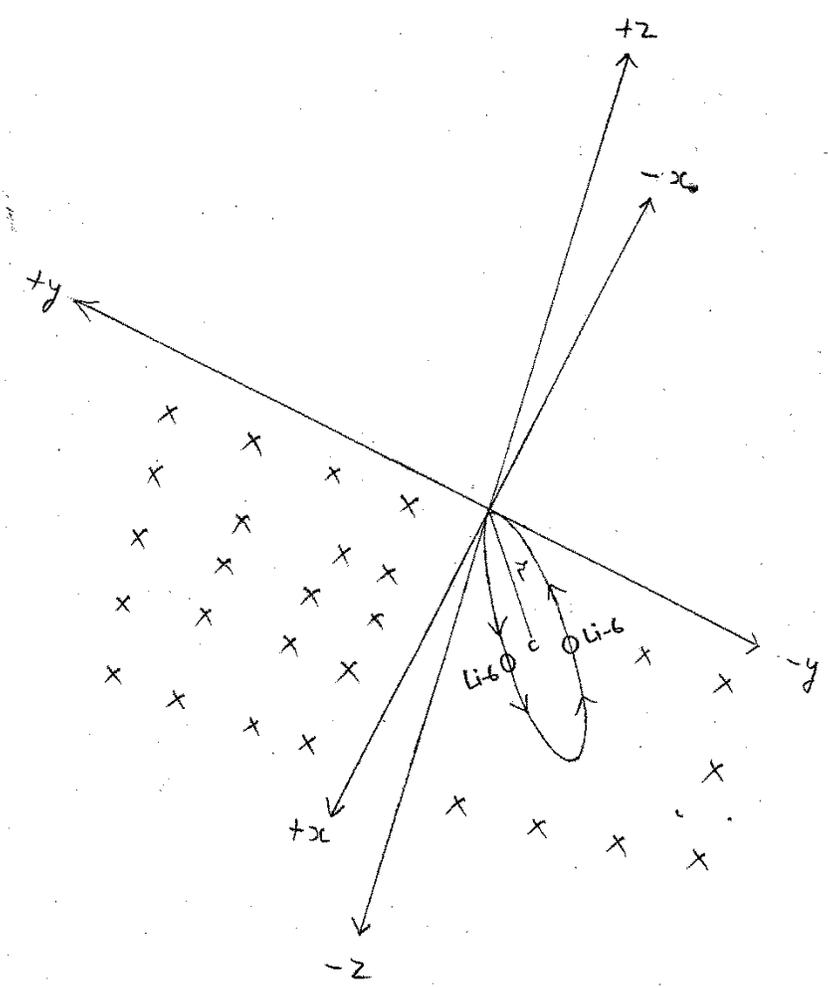
$$r = mv^2 / F_R$$

$$mv^2 = 1.2422 \times 10^{-13} \text{ J}$$

$$F_r = 1.8942 \times 10^{-13} \text{ N}$$

$$r = \frac{1.2422 \times 10^{-13} \text{ J}}{1.8942 \times 10^{-13} \text{ N}}$$

$$r = 0.6557 \text{ m}$$



The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the lithium -6 nucleus.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$d = 2 \times r$$

$$= 2 \times 0.6557 \text{ m} \\ = 1.3114 \text{ m}$$

$$\cos \alpha = 0.7746$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 1.3114 \times 0.7746 \text{ m}$$

$$x_2 - x_1 = 1.0158 \text{ m}$$

$$x_2 = 1.0158 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = -0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 1.3114 \times (-0.4472) \text{ m}$$

$$y_2 - y_1 = -0.5863 \text{ m}$$

$$y_2 = -0.5863 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

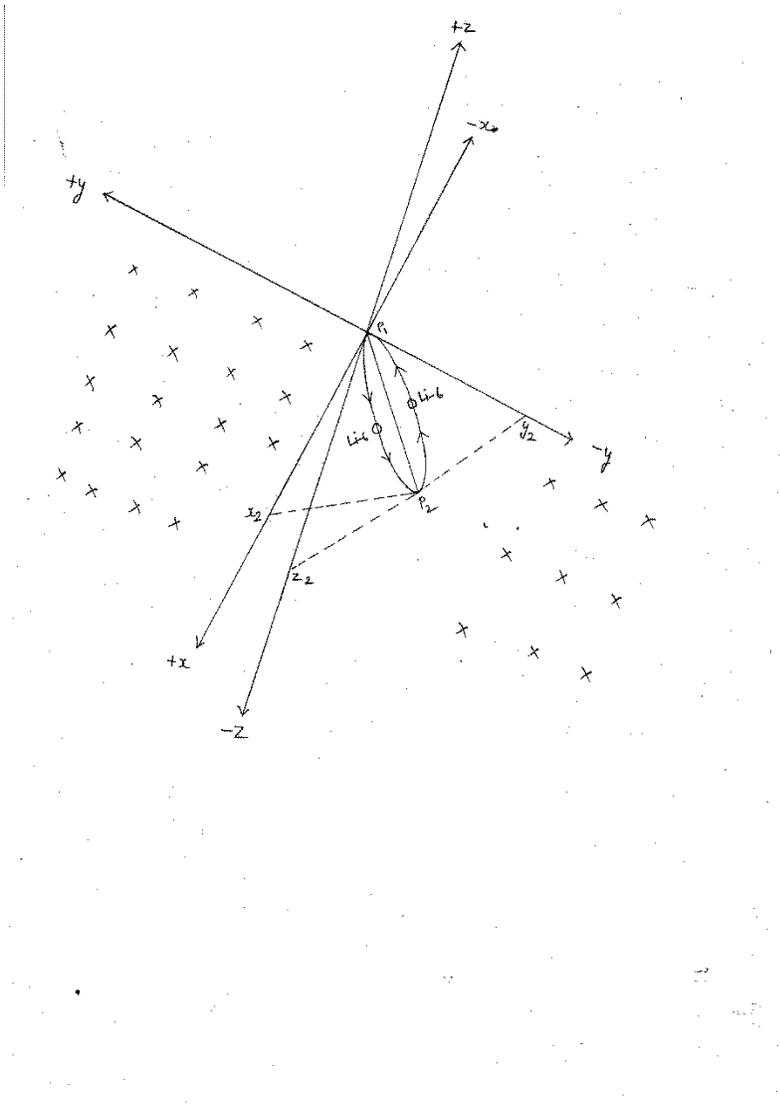
$$\cos \gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 1.3114 \times (-0.4473) \text{ m}$$

$$z_2 - z_1 = -0.5865 \text{ m}$$

$$z_2 = -0.5865 \text{ m} \quad [\because z_1 = 0]$$



The cartesian coordinates of the point $p_1(x_1, y_1, z_1)$ and $p_2(x_2, y_2, z_2)$ located on the circumference of the circle obtained by the lithium -6 nucleus are as above shown .

The line is the diameter of the circle .

P_1P_2

Conclusion :-

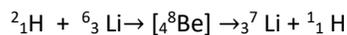
The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-6 nucleus are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit followed by the lithium-6 nucleus lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the lithium-6 nucleus to undergo to a circular orbit of radius of 0.6557 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.0158 \text{ m}, -0.5863 \text{ m}, -0.5865 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

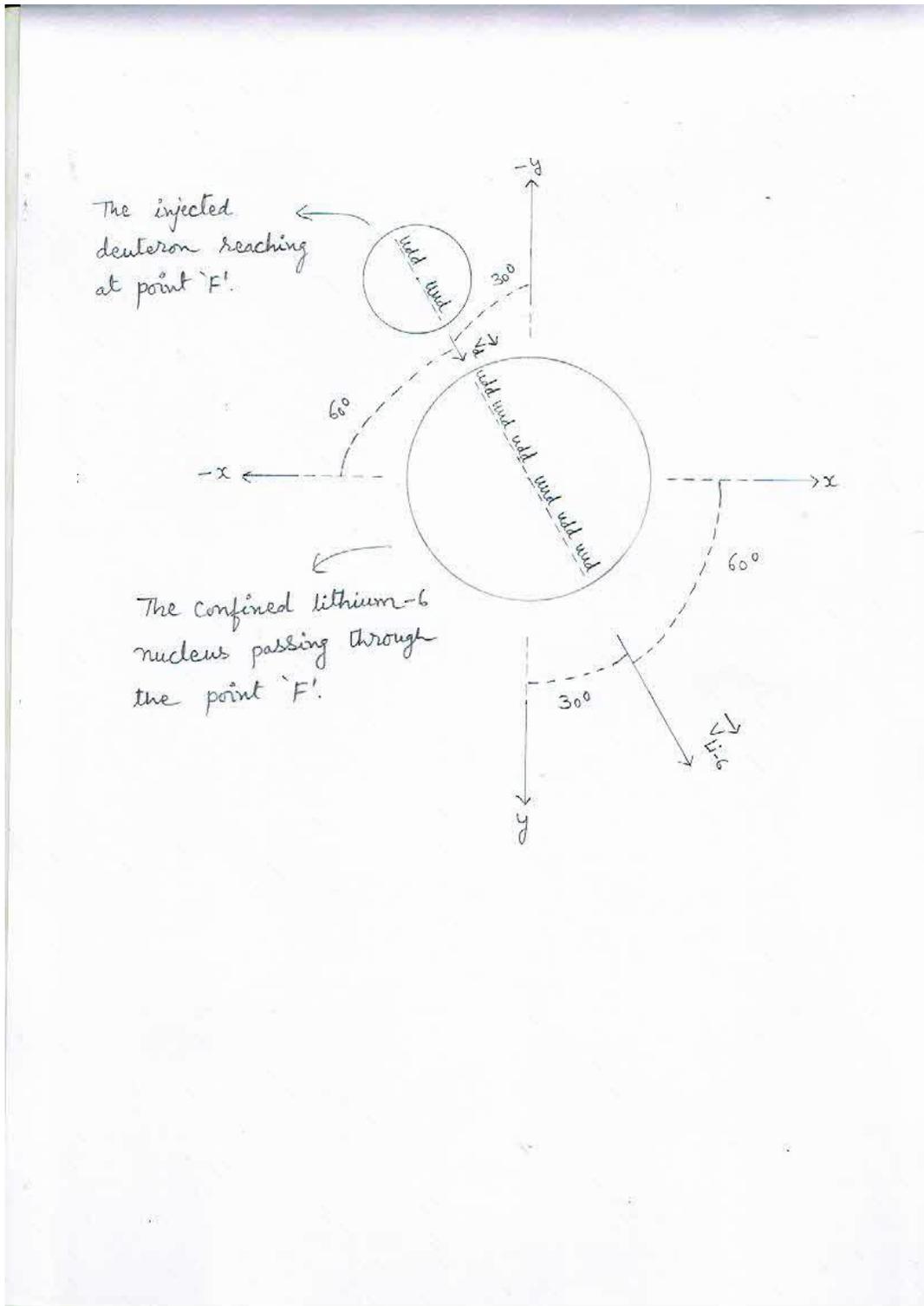
For fusion reaction



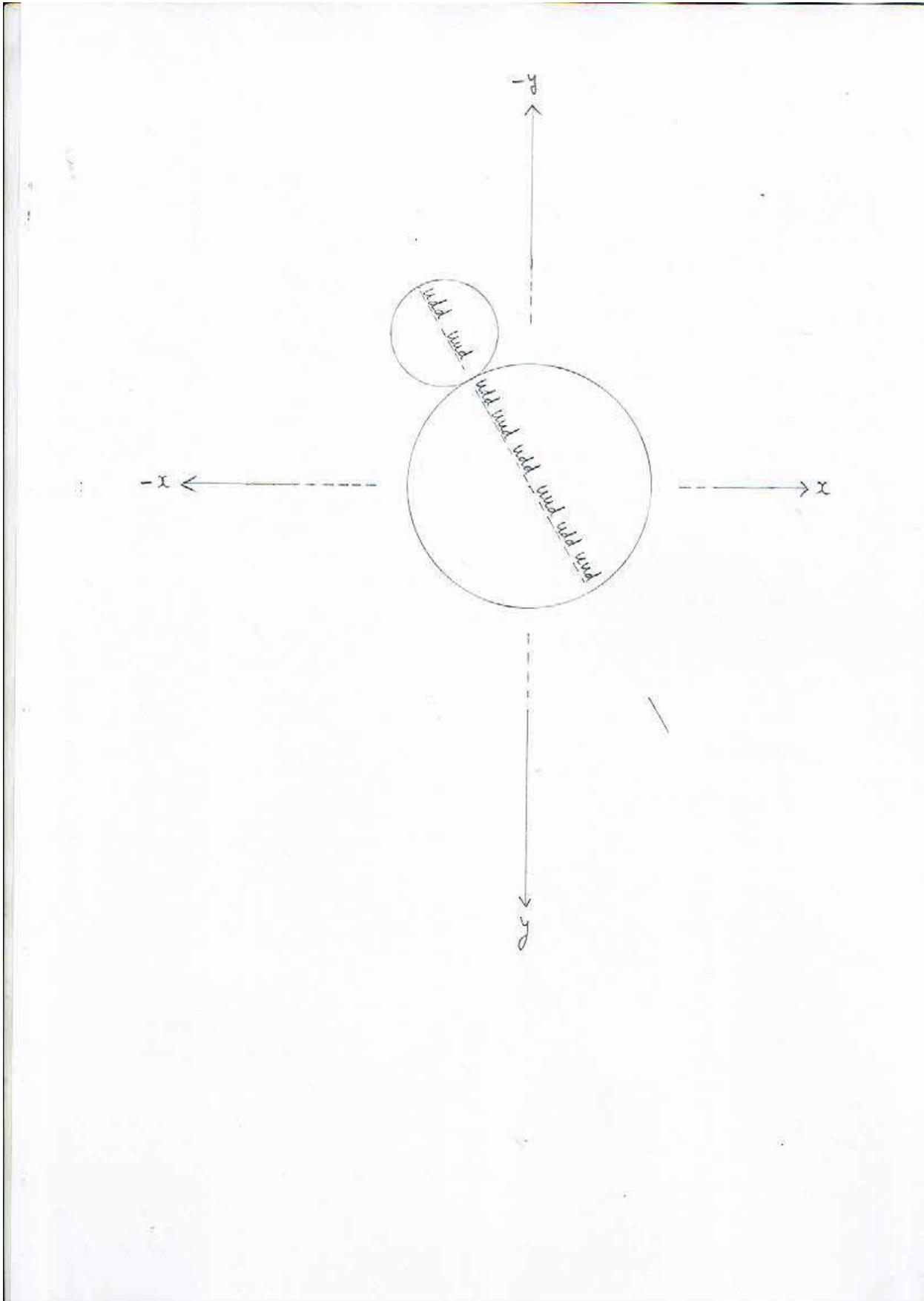
The interaction of nuclei :-

The injected deuteron reaches at point F, and interacts [experiences a repulsive force due to the confined lithium-6] with the confined lithium-6 passing through the point F. the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join – the injected deuteron dissimilarly joins with the confined lithium-6.

Interaction of nuclei (1)



Interaction of nuclei (2)

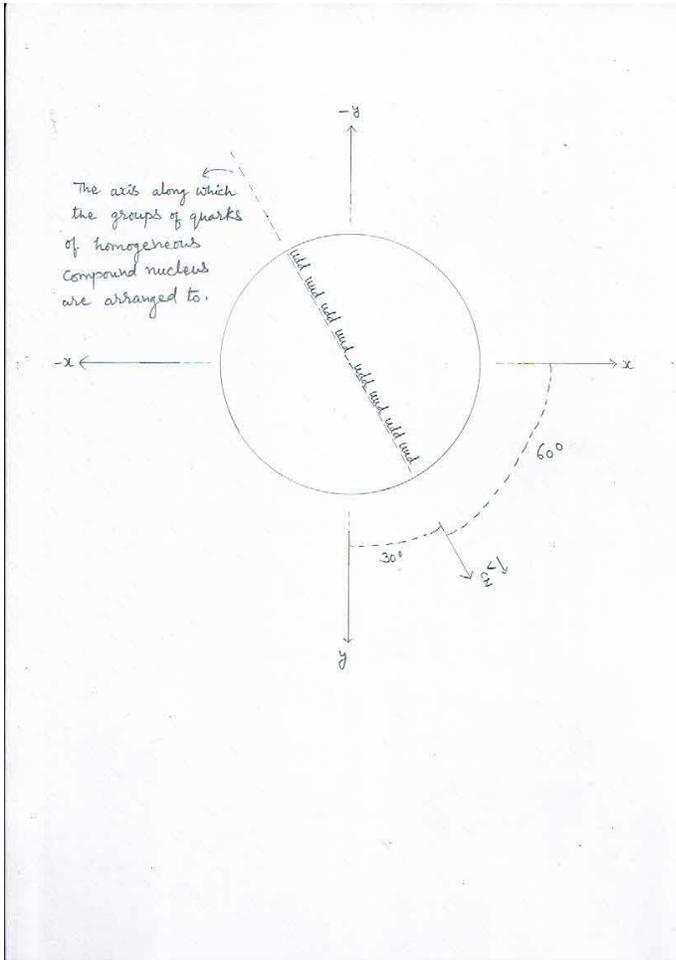


.Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron and the lithium-6 nucleus) behave like a liquid and form a homogeneous compound nucleus . having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 8 groups of quarks surrounded by the gluons.

The homogenous compound nucleus



where,

$$\alpha = 60 \text{ degrees}$$

$$\beta = 30 \text{ degrees}$$

3 . Formation of lobes within into the homogeneous compound nucleus or the homogenous compound nucleus into the heterogenous compound nucleus : -

transformation of the

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the lithium-7) than the reactant one (the lithium-6) includes the other three (nearby located) groups of quarks with their surrounding gluons and rearrange to form the 'A' lobe of the heterogeneous compound nucleus.

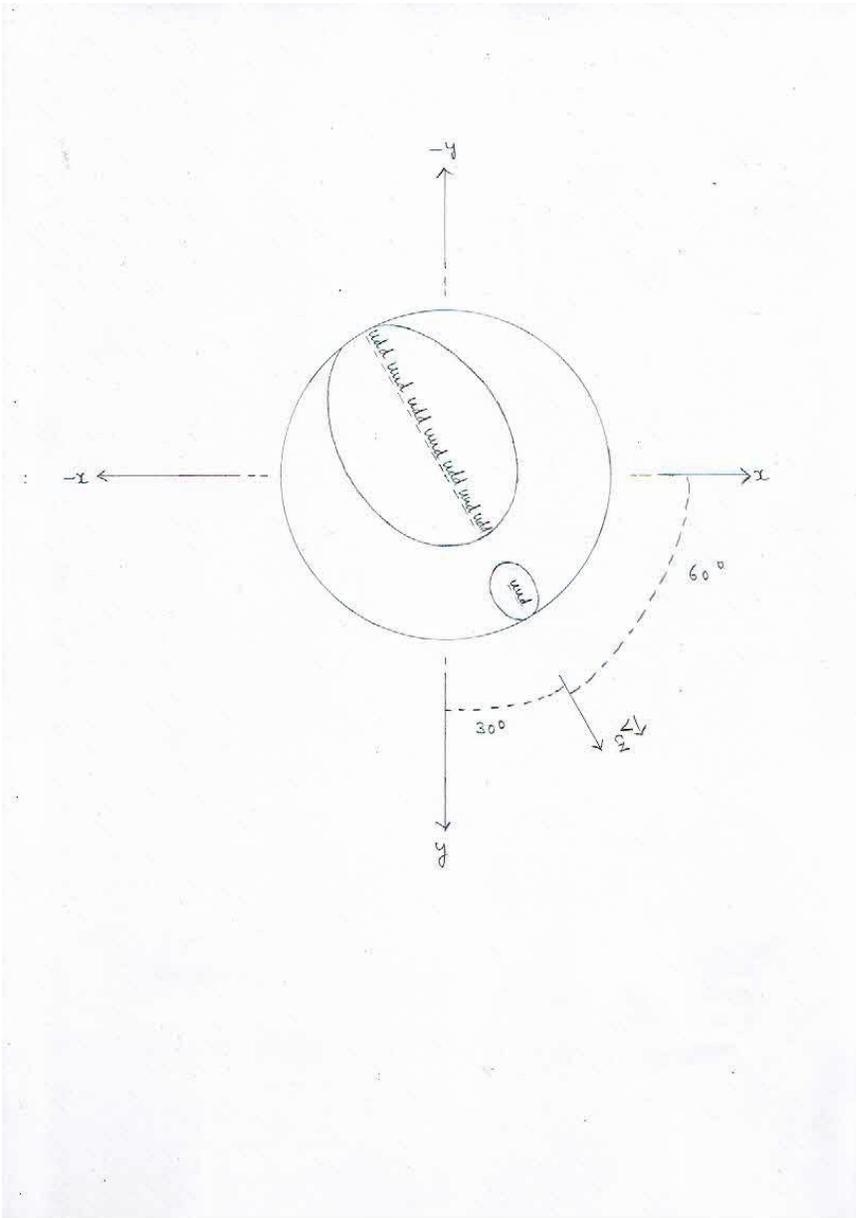
While, the remaining groups of quarks to become a stable nucleus (the proton) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe 'A'] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus.

Thus, due to formation of two dissimilar lobes within into the homogeneous compound nucleus, the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the lithium-7 nucleus and the smaller nucleus is the proton.

The greater nucleus is the lobe 'A' and the smaller nucleus is the lobe 'B' while the remaining space represent the remaining gluons.



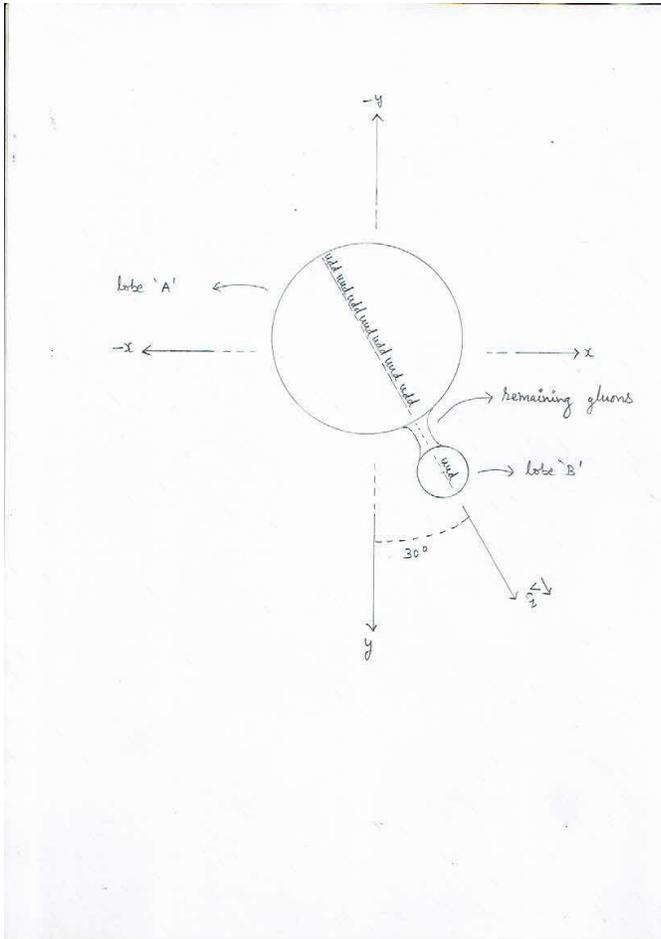
Formaton of lobes

4..Final stage of the heterogeneous compound nucleus : -

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

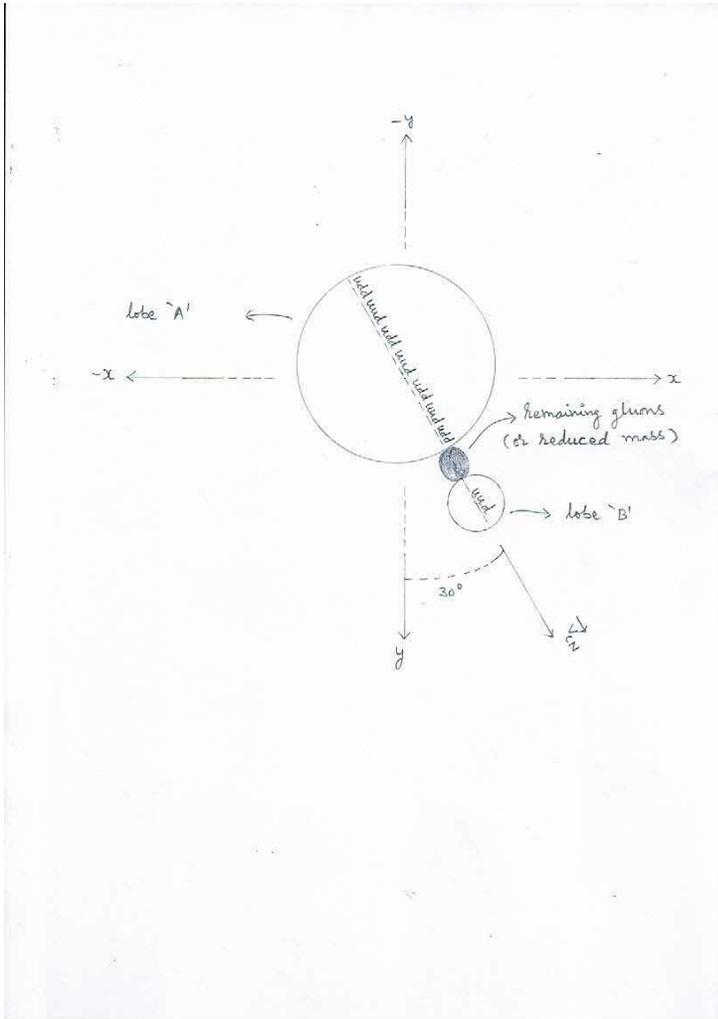
So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogenous compound nucleus

For $\alpha = 60$ degrees

$\beta = 30$ degrees



Final stage of the heterogenous compound nucleus

where, $\alpha = 60$ degrees

$\beta = 30$ degrees

Formation of compound nucleus :

As the deuteron of n^{th} bunch reaches at point F , it fuses with the confined lithium-6 to form a compound nucleus .

1. Just before fusion, to overcome the electrostatic repulsive force exerted by the lithium-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves its energy equal to 45.5598 keV.

so, just before fusion,

the kinetic energy of n^{th} deuteron is –

$$E_b = 153.6 \left[\text{keV} - 45.5598 \text{ keV} \right]$$

$$= 108.0402 \text{ keV}$$

$$= 0.1080402 \text{ MeV}$$

2. Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron, the lithium-6 loses (radiates its energy in the form of electromagnetic waves its energy equal to 136.0700 keV.

so, just before fusion,

the kinetic energy of lithium-6 is –

$$E_b = 388.2043 \text{ keV} - 136.0700 \text{ keV}$$

$$= 252.1343 \text{ keV}$$

$$= 0.2521343 \text{ MeV}$$

Kinetic energy of the compound nucleus :-

$$\text{K.E.} = [E_b \text{ of deuteron}] + [E_b \text{ of lithium-6}]$$

$$= [108.0402 \text{ KeV}] + [252.1343 \text{ KeV}]$$

$$= 360.1745 \text{ KeV.}$$

$$= 0.3601745 \text{ MeV}$$

Mass of the compound nucleus

$$M = m_d + m_{\text{Li-6}}$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}]$$

$$= 13.3287 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3601745 \text{ MeV}$$

$$V_{\text{CN}} = \left[\frac{2 \times 0.3601745 \times 1.6 \times 10^{-13}}{13.3287 \times 10^{-27} \text{ kg}} \right]^{1/2} \text{ m/s}$$

$$V_{CN} = \left(\frac{1.1525584 \times 10^{-13} \text{ m/s}}{13.3287 \times 10^{-27}} \right)^{1/2}$$

$$V_{CN} = [0.08647192899 \times 10^{14}]^{1/2} \text{ m/s}$$

$$V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$\begin{aligned} \vec{V}_x &= V_{CN} \cos \alpha \\ &= 0.2940 \times 10^7 \times 0.5 \quad \text{m/s} \\ &= 0.1470 \times 10^7 \quad \text{m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_y &= V_{CN} \cos \beta \\ &= 0.2940 \times 10^7 \times 0.866 \quad \text{m/s} \\ &= \mathbf{0.2546} \text{ m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_z &= V_{CN} \cos \gamma \\ &= 0.2940 \times 10^7 \times 0 \quad \text{m/s} \\ &= 0 \quad \text{m/s} \end{aligned}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus, due to its instability, splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – lithium-7, the proton, and the reduced mass (Δm).

Out of them, the two particles (the lithium-7 and proton) are stable while the third one (reduced mass) is unstable.

According to the law of inertia, each particle that is produced due to splitting of the compound nucleus, has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}).

So, for conservation of momentum

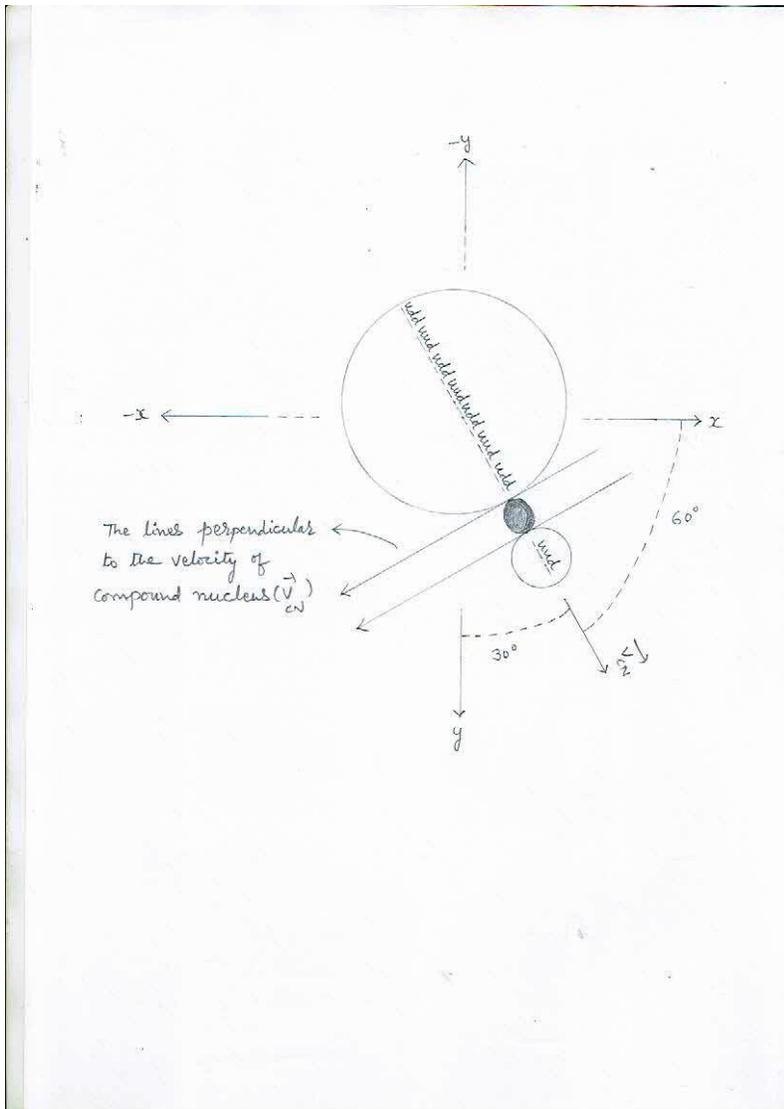
$$M\vec{V}_{cn} = (m_{Li-7} + \Delta m + m_p)\vec{V}_{cn}$$

Where ,

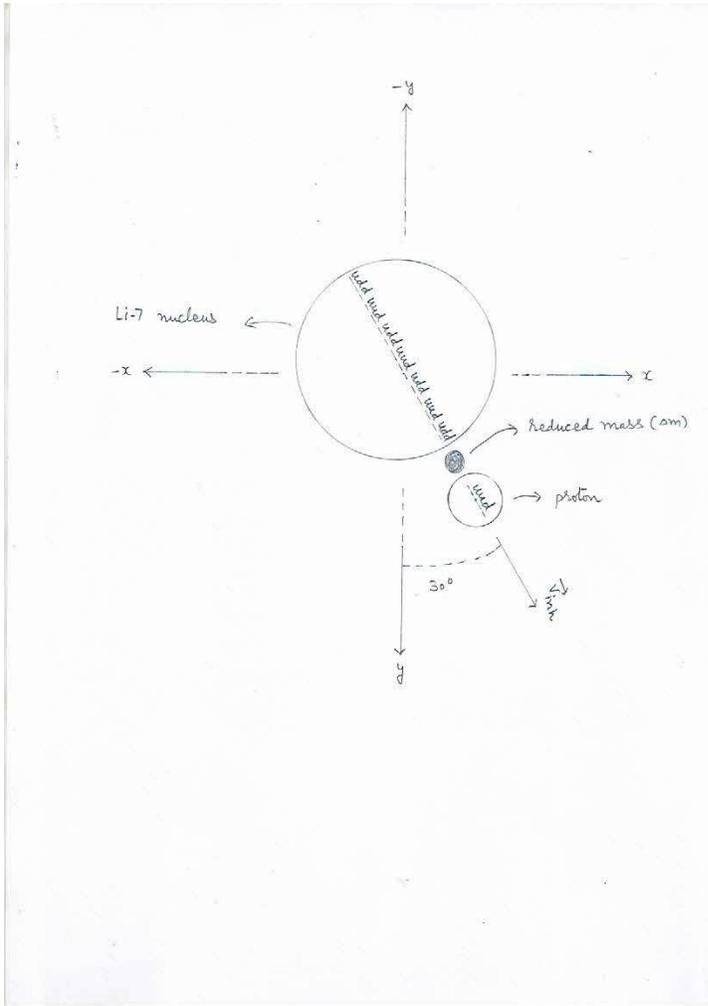
M	= mass of the compound nucleus
\vec{V}_{cn}	= velocity of the compound nucleus
M_{Li-7}	= mass of the lithium-7 nucleus
Δm	= reduced mass
m_p	= mass of the proton

The splitting of the heterogeneous compound nucleus

The heterogeneous compound nucleus to show the lines perpendicular to the \vec{V}_{cn}



The splitting of the heterogenous compound nucleus



Inherited velocity of the particles (s) :-

Each particle that is produced due to splitting of compound nucleus has an inherited velocity (\vec{V}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}).

I. Inherited velocity of the particle lithium -7

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle lithium -7

$$1 \quad \vec{V}_{Vx} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2 \quad \vec{V}_{Vy} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3 \quad \vec{V}_{Vz} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

II. Inherited velocity of the proton

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the proton

$$1 \quad \vec{V}_{Vx} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2 \quad \vec{V}_{Vy} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3 \quad \vec{V}_{Vz} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

iii Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{Li-6}] - [m_{Li-7} + m_p]$$

$$\Delta m = [2.01355 + 6.01347708] - [7.01435884 + 1.007276] \text{ amu}$$

$$\Delta m = [8.02702708] - [8.02163484] \text{ amu}$$

$$\Delta m = 0.00539224 \text{ amu}$$

$$\Delta m = 0.00539224 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm) .

$$E_{inh} = \frac{1}{2} \Delta m V_{CN}^2$$

$$\Delta m = 0.00539224 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{CN}^2 = 0.08647192899 \times 10^{14}$$

$$E_{inh} = \frac{1}{2} \times 0.00539224 \times 1.6605 \times 10^{-27} \times 0.08647192899 \times 10^{14} \text{ J}$$

$$E_{inh} = 0.0003871268 \times 10^{-13} \text{ J}$$

$$E_{inh} = 0.000241 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.00539224 \times 931 \text{ Mev}$$

$$E_R = 5.020175 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{inh} + E_R$$

$$E_T = [0.000241 + 5.020175] \text{ Mev}$$

$$E_T = 5.020416 \text{ Mev}$$

Increased in the energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses. so, the increased energy (E_{inc}) of the particles :-

1.. For lithium-7

$$E_{inc} = \frac{m_p}{m_p + m_{Li-7}} \times E_T$$

$$E_{inc} = \frac{1.007276 \text{ amu}}{[1.007276 + 7.01435884] \text{ amu}} \times 5.020416 \text{ Mev}$$

$$E_{inc} = \frac{1.007276}{8.02163484} \times 5.020416 \text{ Mev}$$

$$E_{inc} = 0.12556991437 \times 5.020416 \text{ Mev}$$

$$E_{inc} = 0.630413 \text{ Mev}$$

2..increased energy of the proton

$$E_{inc} = [E_T] - [\text{increased energy of the Li-7}]$$

$$E_{inc} = [5.020416] - [0.630413] \text{ Mev}$$

$$E_{inc} = 4.390003 \text{ Mev}$$

6..Increased velocity of the particles .

(1) For proton

$$E_{inc} = \frac{1}{2} m_p v_{inc}^2$$

$$\begin{aligned} v_{inc} &= [2 \times E_{inc} / m_p]^{1/2} \\ &= \left[\frac{2 \times 4.390003 \times 1.6 \times 10^{-13} \text{ J}}{1.6726 \times 10^{-27} \text{ kg}} \right]^{1/2} \text{ m/s} \\ &= \left[\frac{14.0480096 \times 10^{-13}}{1.6726 \times 10^{-27}} \right]^{1/2} \text{ m/s} \\ &= [8.39890565586 \times 10^{14}]^{1/2} \text{ m/s} \\ &= 2.8980 \times 10^7 \text{ m/s} \end{aligned}$$

(2) For lithium-7

$$\begin{aligned} v_{inc} &= [2 \times E_{inc} / m_{He-4}]^{1/2} \\ &= \left[\frac{2 \times 0.630413 \times 1.6 \times 10^{-13} \text{ J}}{11.6473 \times 10^{-27} \text{ kg}} \right]^{1/2} \\ &= \left[\frac{2.0173216 \times 10^{-13}}{11.6473 \times 10^{-27}} \right]^{1/2} \text{ m/s} \end{aligned}$$

$$\begin{aligned}
 &= [0.17320079331 \times 10^{14}]^{1/2} \text{ m/s} \\
 &= 0.4161 \times 10^7 \text{ m/s}
 \end{aligned}$$

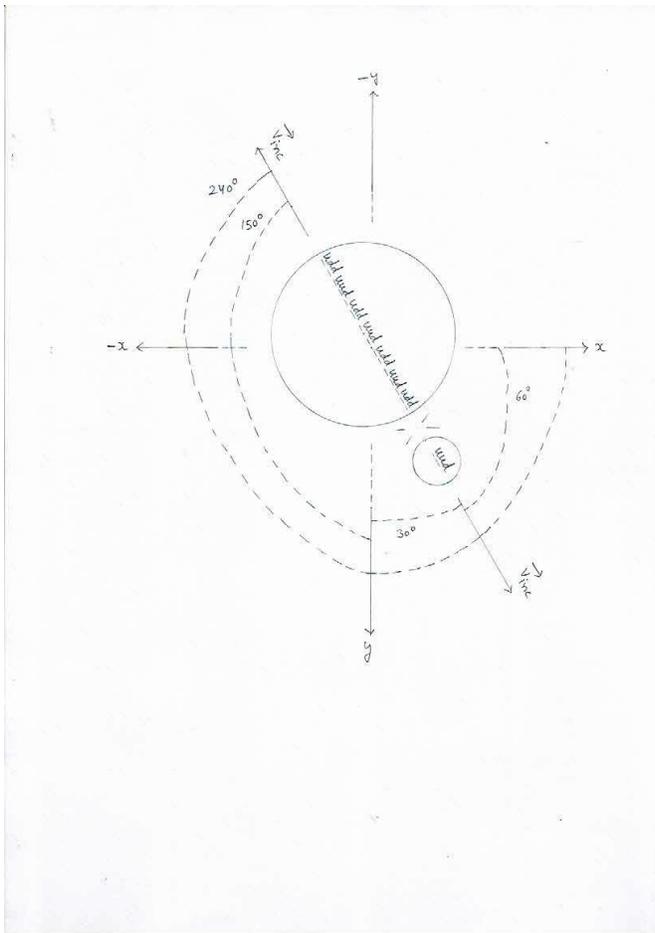
7 Angle of propulsion

- 1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum.

2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus (\vec{V}_{CN}) .]

- 3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .
 so, the proton is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .
 While the lithium-7 is propelled making 240° angle with x-axis , 150° angle with y-axis and 90° angle with z-axis .

propulsion of the particles



Components of the increased velocity (V_{inc}) of the particles.

(i) For lithium-7

$$1 \rightarrow_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 0.4161 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos (240) = -0.5$$

$$\rightarrow_{V_x} = 0.4161 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.2080 \times 10^7 \text{ m/s}$$

$$2 \rightarrow_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos (150) = -0.866$$

$$\rightarrow_{V_y} = 0.4161 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.3603 \times 10^7 \text{ m/s}$$

$$3 \rightarrow_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\rightarrow_{V_z} = 0.4161 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

(II) For proton

$$1 \rightarrow_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.8980 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\rightarrow_{V_x} = 2.8980 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 1.4490 \times 10^7 \text{ m/s}$$

$$2 \rightarrow_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos (30) = 0.866$$

$$\rightarrow_{V_y} = 2.8980 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 2.5096 \times 10^7 \text{ m/s}$$

$$3 \rightarrow_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos (90) = 0$$

$$\rightarrow_{V_z} = 2.8980 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9.. Components of the finalvelocity (\vec{V}_f)of the particles

IFor lithion-7

According to -	Inherited Velocity(\vec{V}_{inh})	Increased Velocity(\vec{V}_{inc})	Finalvelocity (\vec{V}_f) $=(\vec{V}_{inh} + \vec{V}_{inc})$
X – axis	$\vec{v}_x = 0.1470 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.2080 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.061 \times 10^7 \text{ m/s}$
y – axis	$\vec{v}_y = 0.2546 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.3603 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.1057 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..Forproton

According to -	Inherited Velocity(\vec{V}_{inh})	Increased Velocity(\vec{V}_{inc})	Final velocity (\vec{V}_f) $=(\vec{V}_{inh} + \vec{V}_{inc})$

X-axis	$\vec{v}_x = 0.1470$ $\times 10^7 \text{ m/s}$	$\vec{v}_x = 1.4490$ $\times 10^7 \text{ m/s}$	$\vec{v}_x = 1.5960$ $\times 10^7 \text{ m/s}$
y-axis	$\vec{v}_y = 0.2546$ $\times 10^7 \text{ m/s}$	$\vec{v}_y = 2.5096$ $\times 10^7 \text{ m/s}$	$\vec{v}_y = 2.7642$ $\times 10^7 \text{ m/s}$
z-axis	$\vec{v}_z = 0$ m/s	$\vec{v}_z = 0$ m/s	$\vec{v}_z = 0$ m/s

10.. Final velocity (vf) of the lithium-7

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.061 \times 10^7 \text{ m/s}$$

$$V_y = 0.1057 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.061 \times 10^7)^2 + (0.1057 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.003721 \times 10^{14}) + (0.01117249 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.01489349 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.1220 \times 10^7 \text{ m/s}$$

Final kinetic energy of the lithium-7

$$E = \frac{1}{2} m_{\text{Li-7}} V_f^2$$

$$E = \frac{1}{2} \times 11.6473 \times 10^{-27} \times 0.01489349 \times 10^{14} \text{ J}$$

$$= 0.08673447303 \times 10^{-13} \text{ J}$$

$$= 0.054209 \text{ MeV}$$

$$m_{\text{Li-7}} V_f^2 = 11.6473 \times 10^{-27} \times 0.01489349 \times 10^{14} \text{ J}$$

$$= 0.1734 \times 10^{-13} \text{ J}$$

10.. Final velocity (v_f) of the proton

$$V_f^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 1.5960 \times 10^7 \text{ m/s}$$

$$V_y = 2.7642 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (1.5960 \times 10^7)^2 + (2.7642 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (2.547216 \times 10^{14}) + (7.64080164 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 10.18801764 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 3.1918 \times 10^7 \text{ m/s}$$

Final kinetic energy of the proton

$$E = \frac{1}{2} m_p V_f^2$$

$$V_f^2 = 10.18801764 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$E = \frac{1}{2} \times 1.6726 \times 10^{-27} \times 10.18801764 \times 10^{14} \text{ J}$$

$$= 8.5202391523 \times 10^{-13} \text{ J}$$

$$= 5.3251 \text{ Mev}$$

$$M_p V_f^2 = 1.6726 \times 10^{-27} \times 10.18801764 \times 10^{14} \text{ J}$$

$$= 17.0404 \times 10^{-13} \text{ J}$$

Forces acting on the lithium-7 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.061 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 3 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 3 \times 1.6 \times 10^{-19} \times 0.061 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.2930 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

so,

$$\vec{F}_y = 0.2930 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 3 \times 1.6 \times 10^{-19} \times 0.061 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.2931 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (+) Z-axis,

so,

$$\vec{F}_z = 0.2931 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = -0.1057 \times 10^7 \quad \text{m/s}$$

$$\vec{B}_z = 1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

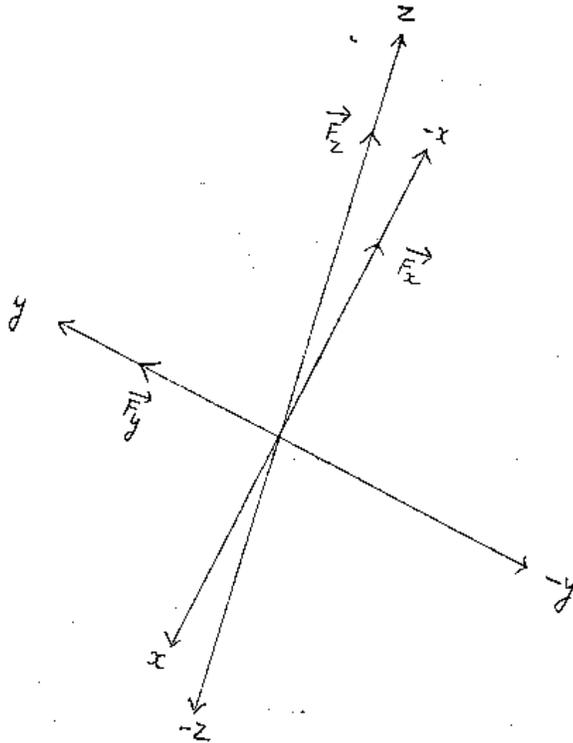
$$F_x = 3 \times 1.6 \times 10^{-19} \times 0.1057 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 0.5078 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x-axis,

$$\text{so, } \vec{F}_x = -0.5078 \times 10^{-13} \text{ N}$$

Forces acting on the lithion-7



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 0.5078 \times 10^{-13} \text{ N}$$

$$F_y = 0.2930$$

$$F_z = 0.2931 \times 10^{-13} \text{ N}$$

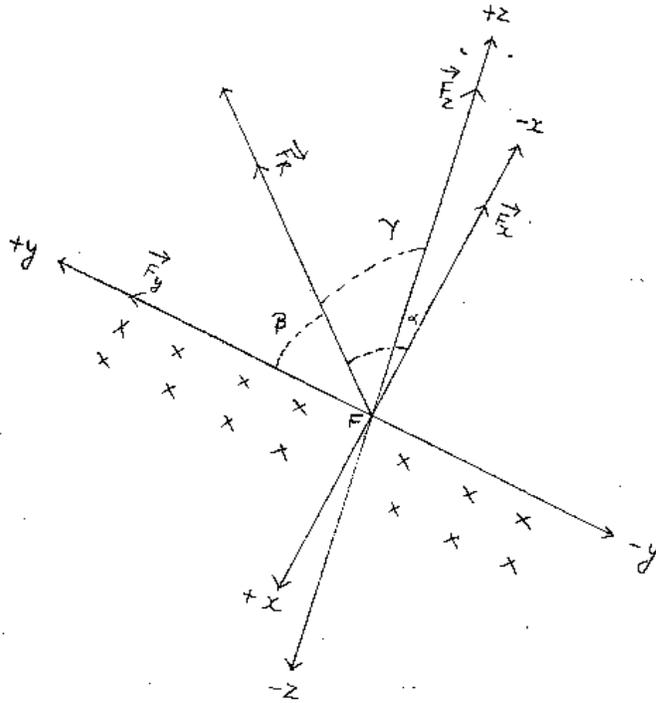
$$F_R^2 = (0.5078 \times 10^{-13})^2 + (0.2930 \times 10^{-13})^2 + (0.2931)^2 \text{ N}^2$$

$$F_R^2 = (0.25786084 \times 10^{-26}) + (0.085849 \times 10^{-26}) + (0.08590761) \text{ N}^2$$

$$F_R^2 = 0.42961745 \times 10^{-26} \text{ N}^2$$

$$F_R = 0.6554 \times 10^{-13} \text{ N}$$

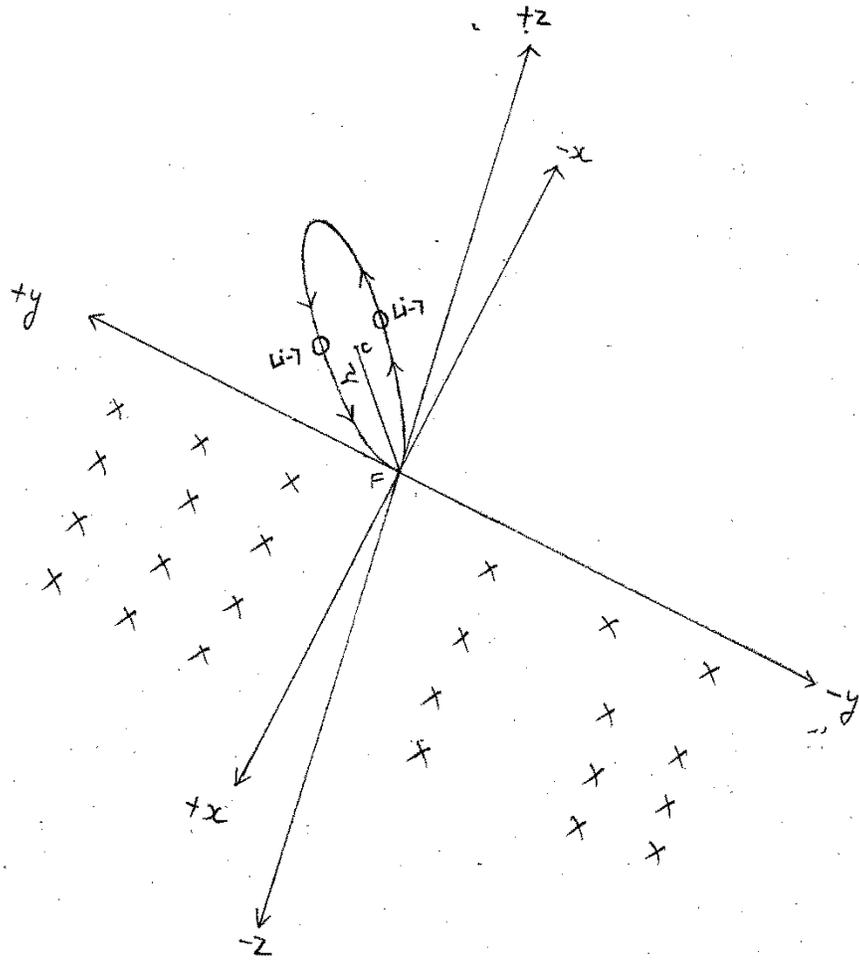
Resultant force acting on the lithium-7



Radius of the circular orbit to be followed by the lithium-7 :

$$r = mv^2 / F_R$$
$$mv^2 = 0.1734 \times 10^{-13} \text{ J}$$
$$F_r = 0.6554 \times 10^{-13} \text{ N}$$
$$r = \frac{0.1734 \times 10^{-13} \text{ J}}{0.6554 \times 10^{-13} \text{ N}}$$

$$r = 0.2645 \text{ m}$$



The circular orbit to be followed by the lithion ⁻⁷ lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

The plane of the circular orbit to be followed by the lithion ⁻⁷ makes angles with positive x, y and z-axes as follows :-

1 with x-axis

$$\cos \alpha = \frac{F_{R \cos \alpha}}{F_r} = \frac{F_x}{F_r}$$

$$F_x = -0.5078 \times 10^{-13} \text{ N}$$

$$F_r = 0.6554 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7747$$

$$\alpha = 219.22 \text{ degree } [\because \cos(219.22) = -0.7747]$$

2 with y-axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{F_y}{F_r}$$

$$F_y = 0.2930 \times 10^{-13} \text{ N}$$

$$F_r = 0.6554 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4470$$

$$\beta = \text{degree } [\because \cos(\) =]$$

3 with z-axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{F_z}{F_r}$$

$$F_z = 0.2931 \times 10^{-13} \text{ N}$$

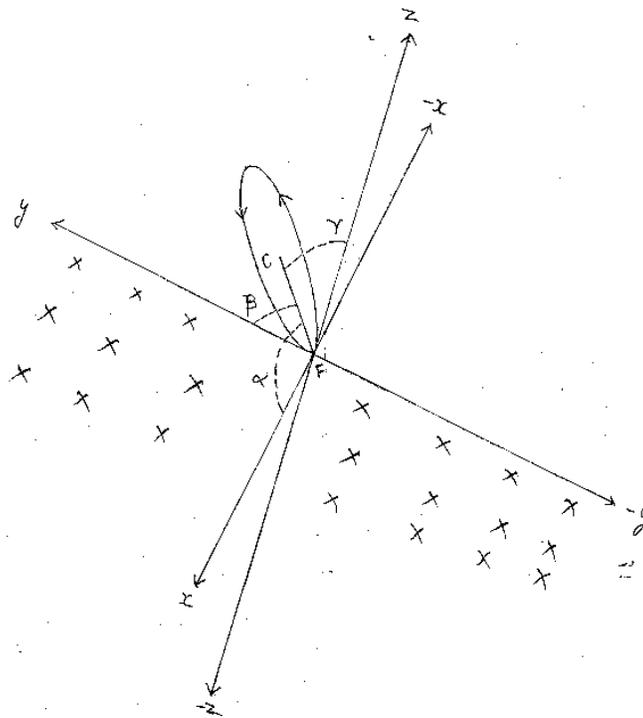
$$F_r = 0.6554 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4472$$

$$\gamma = 63.43 \text{ degree}$$

Plane of the circular orbit to be followed by the lithium -7 nucleus makes angles with positive x, y, and z axes are as follows :-



Where,

$$\alpha = 219.22 \text{ degree}$$

$$\beta = \text{degree}$$

$$\gamma = 63.43 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the lithium-7.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$= 2 \times 0.2645 \text{ m}$$

$$= 0.529 \text{ m}$$

$$d = 2 \times r$$

$$\cos \alpha = -0.7747$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 0.529 \times (-0.7747) \quad \text{m}$$

$$x_2 - x_1 = -0.4098 \text{ m}$$

$$x_2 = -0.4098 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

d

$$\cos \beta = 0.4470$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 0.529 \times 0.4470 \text{ m}$$

$$y_2 - y_1 = 0.2364 \text{ m}$$

$$y_2 = 0.2364 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

d

$$\cos \gamma = 0.4472$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 0.529 \times 0.4472 \text{ m}$$

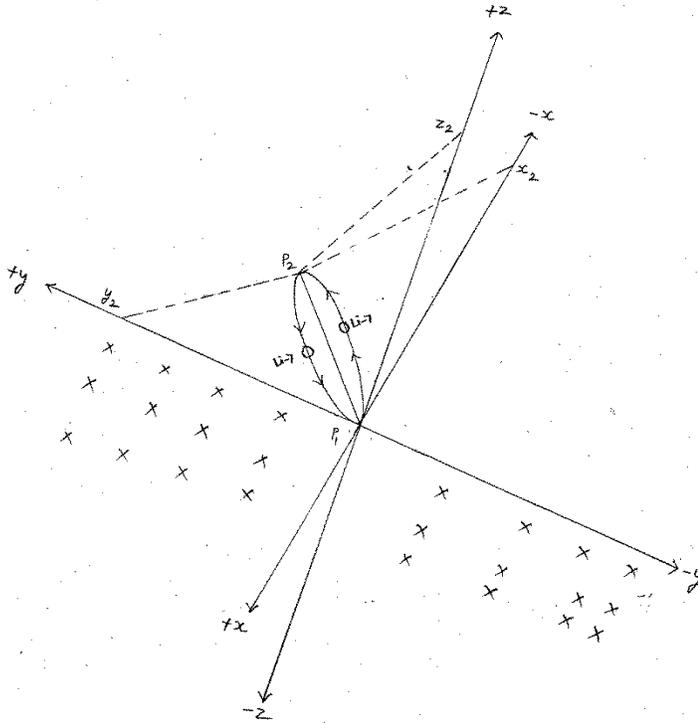
$$z_2 - z_1 = 0.2365 \text{ m}$$

$$z_2 = 0.2365 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the lithion -7 are as shown below.

The line ____ is the diameter of the circle .

P_1P_2



Conclusion :-

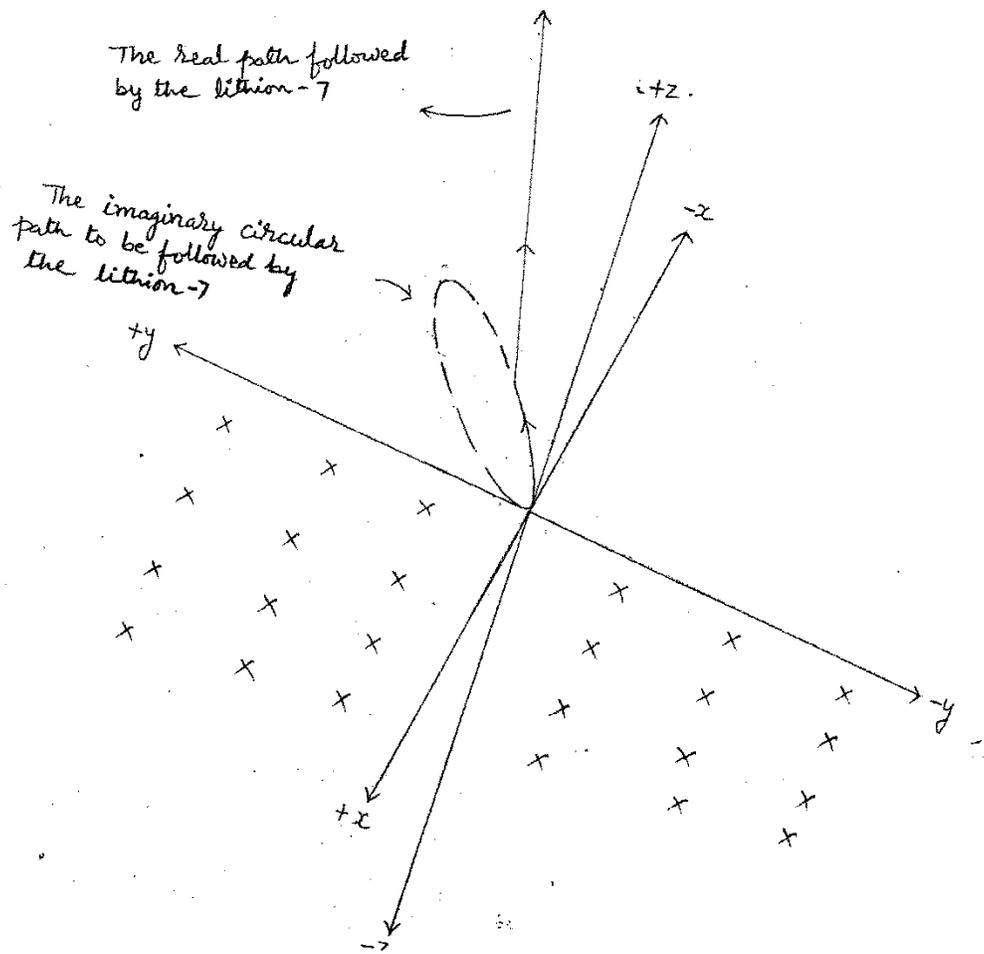
The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-7 nucleus are along **-x, +y and +z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-7 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the lithium-7 nucleus to undergo to a circular orbit of radius 0.2645 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.4098 \text{ m}, 0.2364 \text{ m}, 0.2365 \text{ m})$ where the magnetic fields are not applied.

So, It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the lithium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. so, inspite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

So the lithium-7 nucleus is not confined.



Forces acting on the proton

$$1 \ F_y = q V_x B_z \sin \theta$$

$$\vec{v}_x = 1.5960 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_y &= 1.6 \times 10^{-19} \times 1.5960 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 2.5561 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = -2.5561 \times 10^{-13} \text{ N}$$

$$2 \ F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_z &= 1.6 \times 10^{-19} \times 1.5960 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N} \\ &= 2.5569 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = -2.5569 \times 10^{-13} \text{ N}$$

$$3 \ F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = 2.7642 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

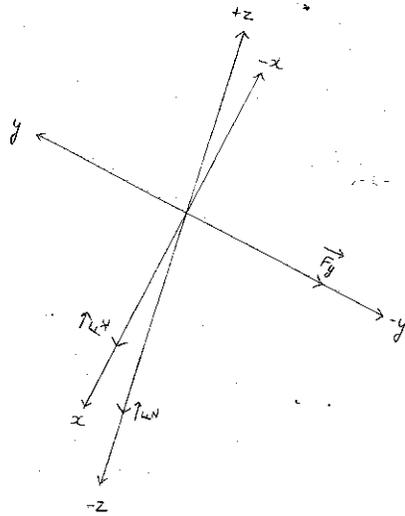
$$\begin{aligned} F_x &= 1.6 \times 10^{-19} \times 2.7642 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 4.4271 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x axis,

so,

$$\vec{F}_x = 4.4271 \times 10^{-13} \text{ N}$$

The forces acting on the proton



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 4.4271 \times 10^{-13} \text{ N}$$

$$F_y = 2.5561 \times 10^{-13} \text{ N}$$

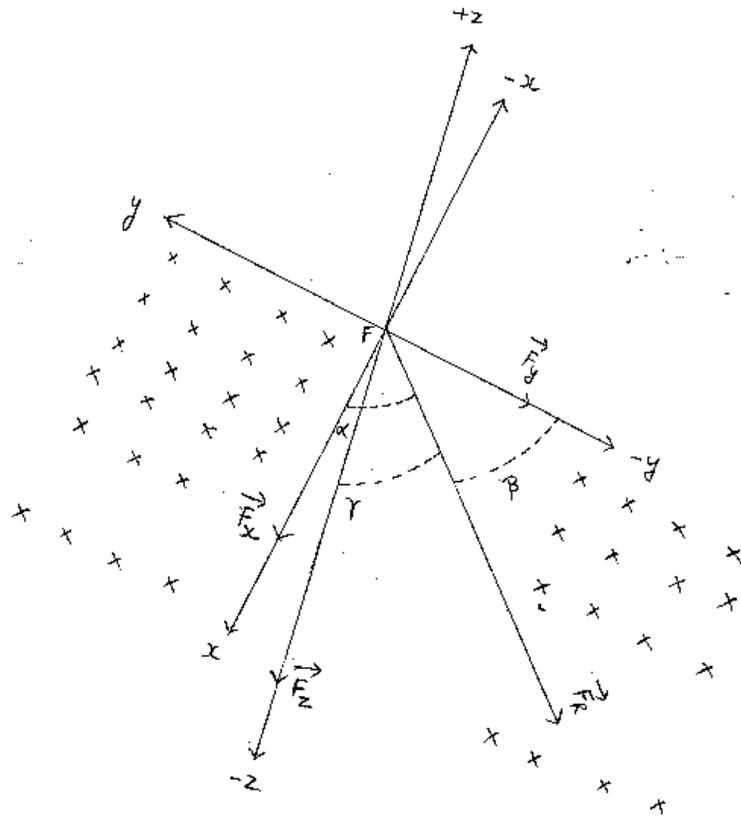
$$F_z = 2.5569 \times 10^{-13} \text{ N}$$

$$F_R^2 = (4.4271 \times 10^{-13})^2 + (2.5561 \times 10^{-13})^2 + (2.5569 \times 10^{-13})^2 \quad \text{N}^2$$

$$F_R^2 = (19.59921441 \times 10^{-26}) + (6.53364721 \times 10^{-26}) + (6.53773761 \times 10^{-26}) \text{N}^2$$

$$F_R^2 = 32.67059923 \times 10^{-26} \quad \text{N}^2$$

$$F_R = 5.7158 \times 10^{-13} \quad \text{N}$$



Radius of the circular orbit to be followed by the proton :

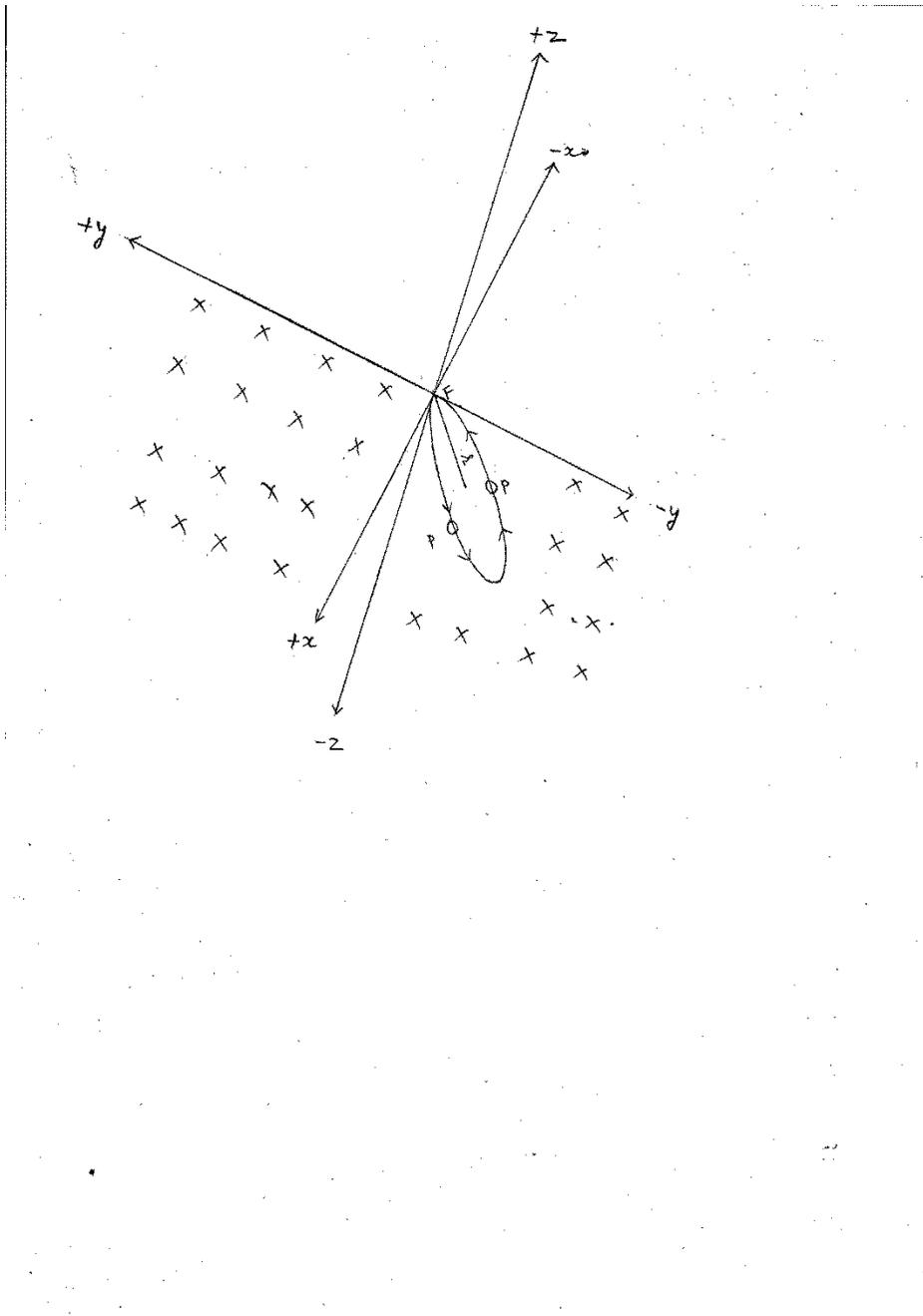
$$r = mv^2 / F_R$$

$$mv^2 = 17.0404 \times 10^{-13} \text{ J}$$

$$F_r = 5.7158 \times 10^{-13} \text{ N}$$

$$r = \frac{17.0404 \times 10^{-13} \text{ J}}{5.7158 \times 10^{-13} \text{ N}}$$

$$r = 2.9812 \text{ m}$$



The circular orbit to be followed by the proton lies in the plane made up of positive x-axis, negative y-axis and the negative z-axis.

C = center of the circle to be followed by the proton.

The plane of the circular orbit to be followed by the proton makes angles with positive x, y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_x}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = 4.4271 \times 10^{-13} \text{ N}$$

$$F_r = 5.7158 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos (39.24) = 0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_y}{F_r} = \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = -2.5561 \times 10^{-13} \text{ N}$$

$$F_r = 5.7158 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4471$$

$$\beta = 243.44 \text{ degree } [\because \cos (243.44) = -0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_z}{F_r} = \frac{F_z}{F_r}$$

$$\frac{F_z}{F_r} = -2.5569 \times 10^{-13} \text{ N}$$

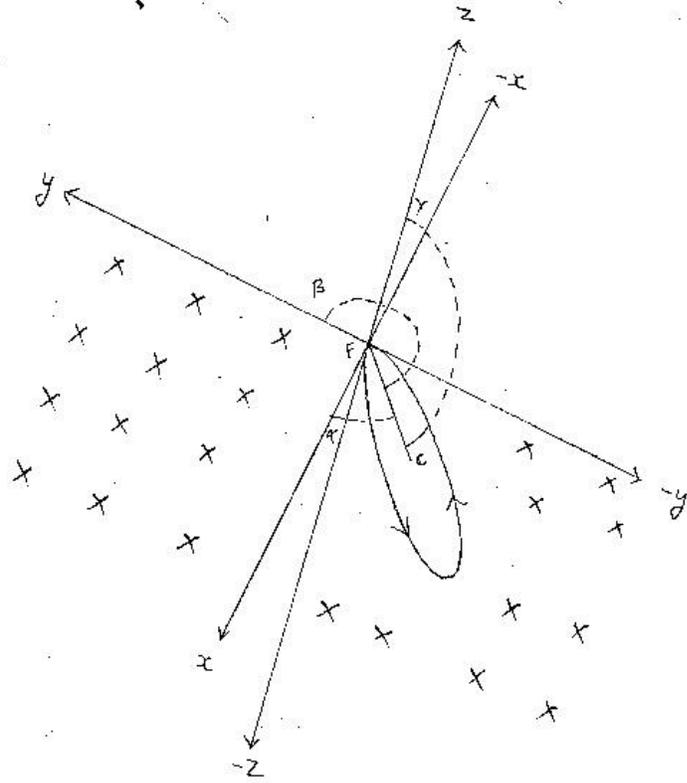
$$F_r = 5.7158 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.425 \text{ degree}$$

The plane of the circular orbit to be followed by the proton makes angles with positive x, y, and z axes as follows :-



Where,
 $\alpha = 39.24$ degree

$$\beta = 243.44 \text{ degree}$$

$$Y = 243.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the proton .

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$= 2 \times 2.9812 \text{ m}$$

$$d = 2 \times r$$

$$= 5.9624 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 5.9624 \times 0.7745 \text{ m}$$

$$x_2 - x_1 = 4.6178 \text{ m}$$

$$x_2 = 4.6178 \text{ m} [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$d$$

$$\cos \beta = -0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 5.9624 \times (-0.4471) \text{ m}$$

$$y_2 - y_1 = -2.6657 \text{ m}$$

$$y_2 = -2.6657 \text{ m} [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$d$$

$$\cos \gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 5.9624 \times (-0.4473) \text{ m}$$

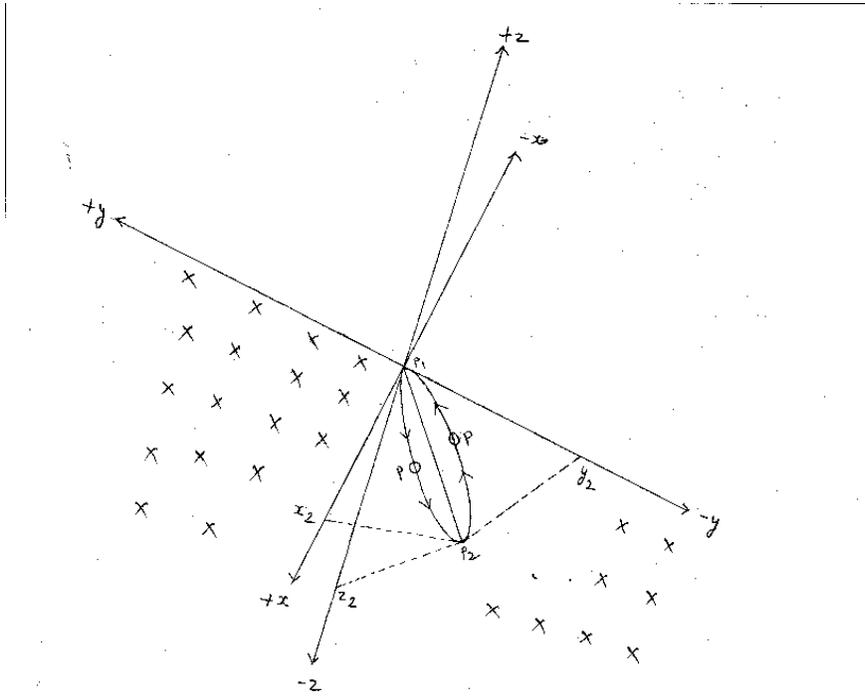
$$z_2 - z_1 = -2.6669 \text{ m}$$

$$z_2 = -2.6669 \text{ m} [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circle to be followed by the proton are as shown above.

The line P_1P_2 is the diameter of the circle .



Conclusion :-

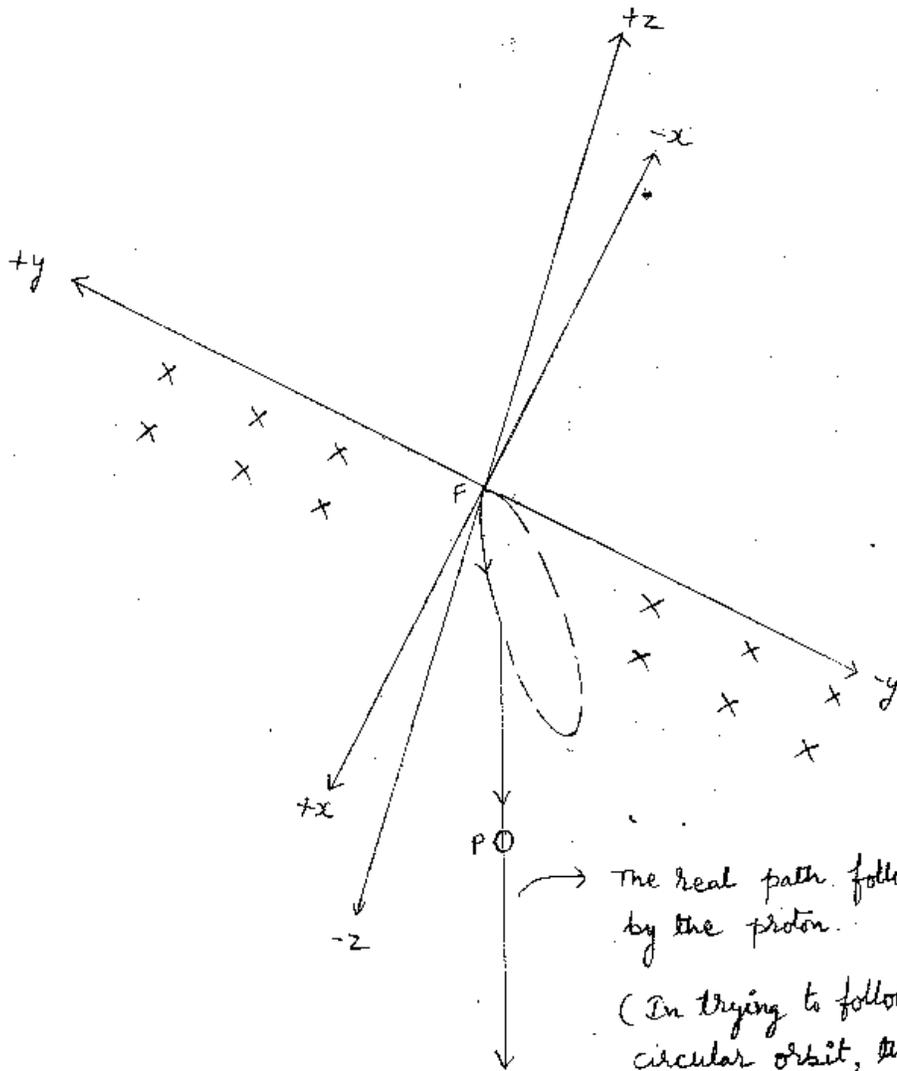
The directions components $\left[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z \right]$ of the resultant force $\left(\vec{F}_r \right)$ that are acting on the proton are along $+x$, $-y$ and $-z$ axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 2.9812 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(4.6178 \text{ m}, -2.6657 \text{ m}, -2.6669 \text{ m})$. in trying to complete its circle, due to lack of space, it strikes to the base wall of the tokamak.

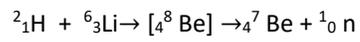
Hence the proton is not confined.



The real path followed by the proton.

(In trying to follow the circular orbit, the produced proton strike to base wall of the tokamak. so, it can not complete the circle.)

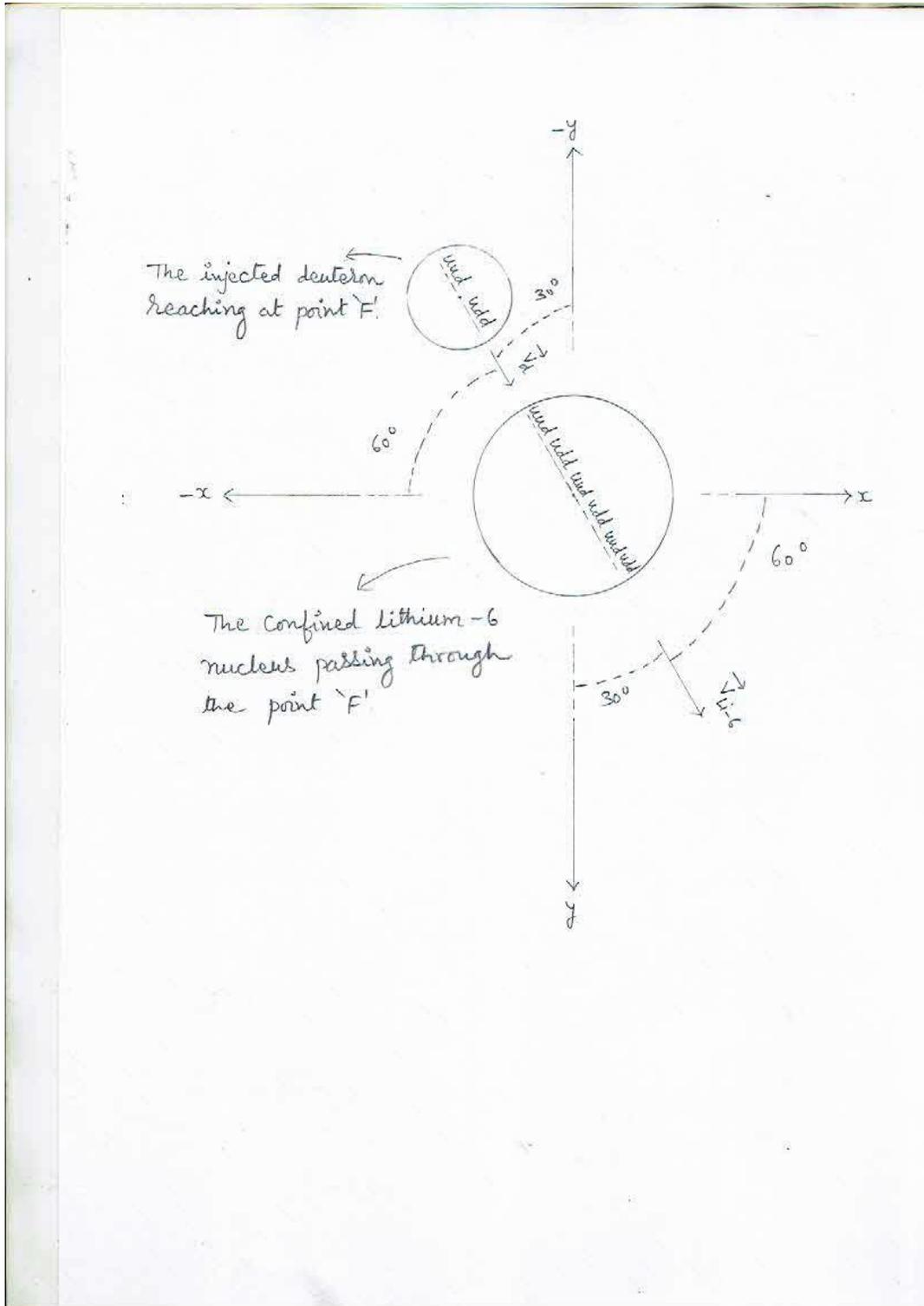
For fusion reaction



The interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined lithium-6] with the confined lithium-6 passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined lithium-6.

Interaction of nuclei (1)



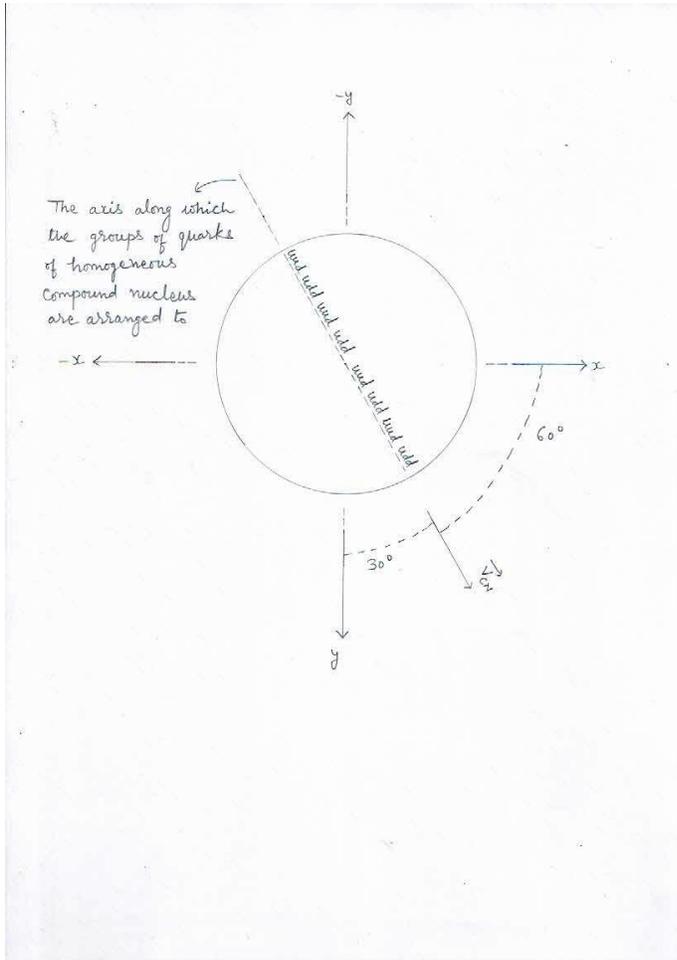
Interaction of nuclei (2)

2. Formation of the homogeneous compound nucleus :-

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron and the lithium-6 nucleus) behave like a liquid and form a homogeneous compound nucleus . having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 8 groups of quarks surrounded by the gluons.

The homogenous compound nucleus



where,

$$\alpha = 60 \text{ degrees}$$

$$\beta = 30 \text{ degrees}$$

3. Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the beryllium - 7) than the reactant one (the lithium-6) includes the other seven (nearby located) groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

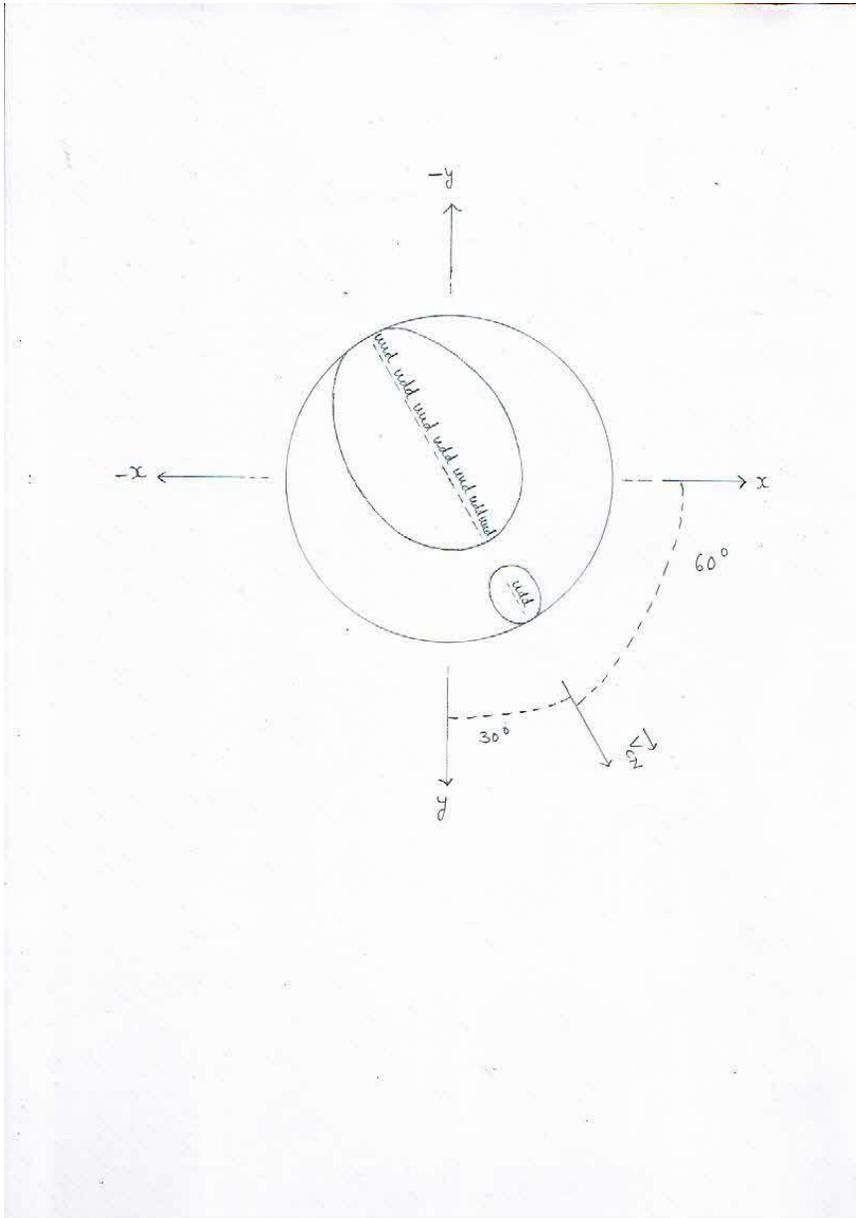
While , the remaining groups of quarks to become a stable nucleus (the neutron) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe ' A '] and rearrange to form the ' B ' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two dissimilar lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the beryllium – 7 nucleus and the smaller nucleus is the neutron.

The greater nucleus is the lobe ' A ' and the smaller nucleus is the lobe ' B ' while the remaining space represent the remaining gluons .



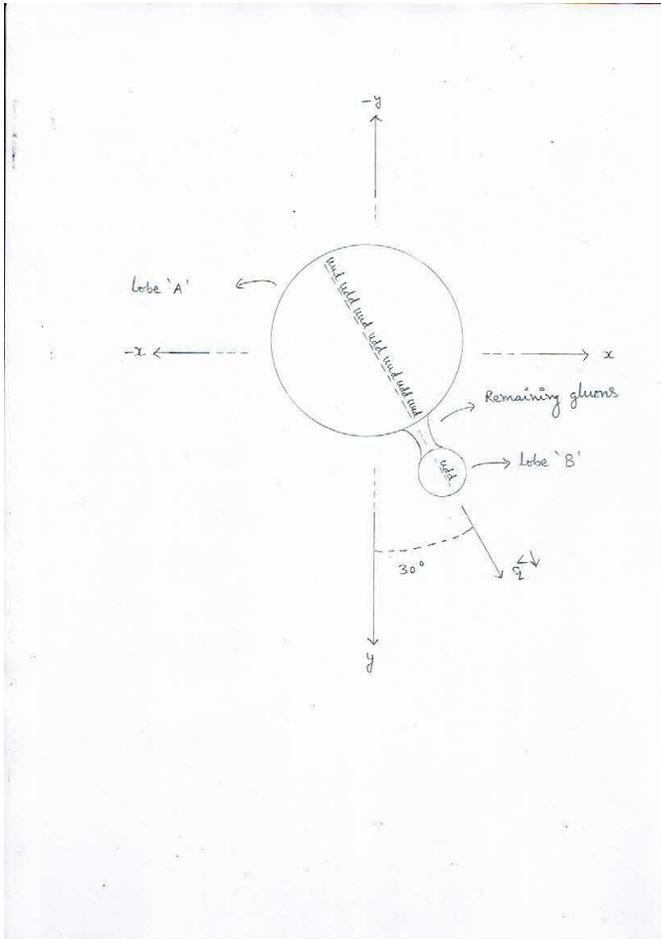
Formaton of lobes

4..Final stage of the heterogeneous compound nucleus :-

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

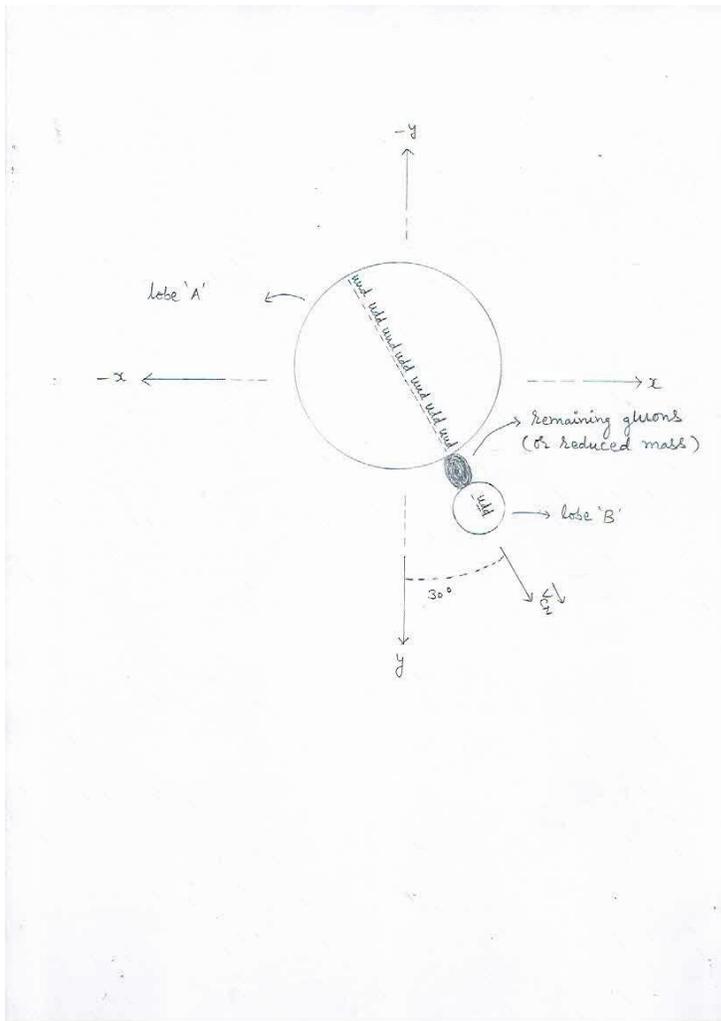
So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogenous compound nucleus

For $\alpha = 60$ degrees

$\beta = 30$ degrees



Final stage of the heterogenous compound nucleus

where, $\alpha = 60$ degree

$\beta = 30$ degree

Formation of compound nucleus :

As the deuteron of n^{th} bunch reaches at point F , it fuses with the confined lithium-6 to form a compound nucleus .

1. Just before fusion, to overcome the electrostatic repulsive force exerted by the lithium-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves its energy equal to 45.5598 keV.

so, just before fusion,

the kinetic energy of n^{th} deuteron is –

$$E_b = 153.6 \text{ keV} - 45.5598 \text{ keV}$$

$$= 108.0402 \text{ keV}$$

$$= 0.1080402 \text{ MeV}$$

2. Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron, the lithium-6 loses (radiates its energy in the form of electromagnetic waves its energy equal to 136.0700 keV.

so, just before fusion,

the kinetic energy of lithium-6 is –

$$E_b = 388.2043 \text{ keV} - 136.0700 \text{ keV}$$

$$= 252.1343 \text{ keV}$$

$$= 0.2521343 \text{ MeV}$$

Kinetic energy of the compound nucleus :-

$$\text{K.E.} = [E_b \text{ of deuteron}] + [E_b \text{ of lithium-6}]$$

$$= [108.0402 \text{ KeV}] + [252.1343 \text{ KeV}]$$

$$= 360.1745 \text{ KeV.}$$

$$= 0.3601745 \text{ MeV}$$

Mass of the compound nucleus

$$M = m_d + m_{\text{Li-6}}$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}]$$

$$= 13.3287 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3601745 \text{ MeV}$$

$$V_{\text{CN}} = \left(\frac{[2 \times 0.3601745 \times 1.6 \times 10^{-13}]}{13.3287 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}} \quad \text{m/s}$$

$$V_{CN} = \left(\frac{1.1525584 \times 10^{-13} \text{ m/s}}{13.3287 \times 10^{-27}} \right)^{1/2}$$

$$V_{CN} = [0.08647192899 \times 10^{14}]^{1/2} \text{ m/s}$$

$$V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$\begin{aligned} \vec{V}_x &= V_{CN} \cos \alpha \\ &= 0.2940 \times 10^7 \times 0.5 \quad \text{m/s} \\ &= 0.1470 \times 10^7 \quad \text{m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_y &= V_{CN} \cos \beta \\ &= 0.2940 \times 10^7 \times 0.866 \quad \text{m/s} \\ &= \mathbf{0.2546} \text{ m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_z &= V_{CN} \cos \gamma \\ &= 0.2940 \times 10^7 \times 0 \quad \text{m/s} \\ &= 0 \quad \text{m/s} \end{aligned}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus , due to its instability , splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – **beryllium – 7**, the neutron and the reduced mass (Δm) .

Out of them , the two particles (the **beryllium – 7** and neutron) are stable while the third one (reduced mass) is unstable .

According to the law of inertia, each particle that is produced due to splitting of the compound nucleus, has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}) .

So, for conservation of momentum

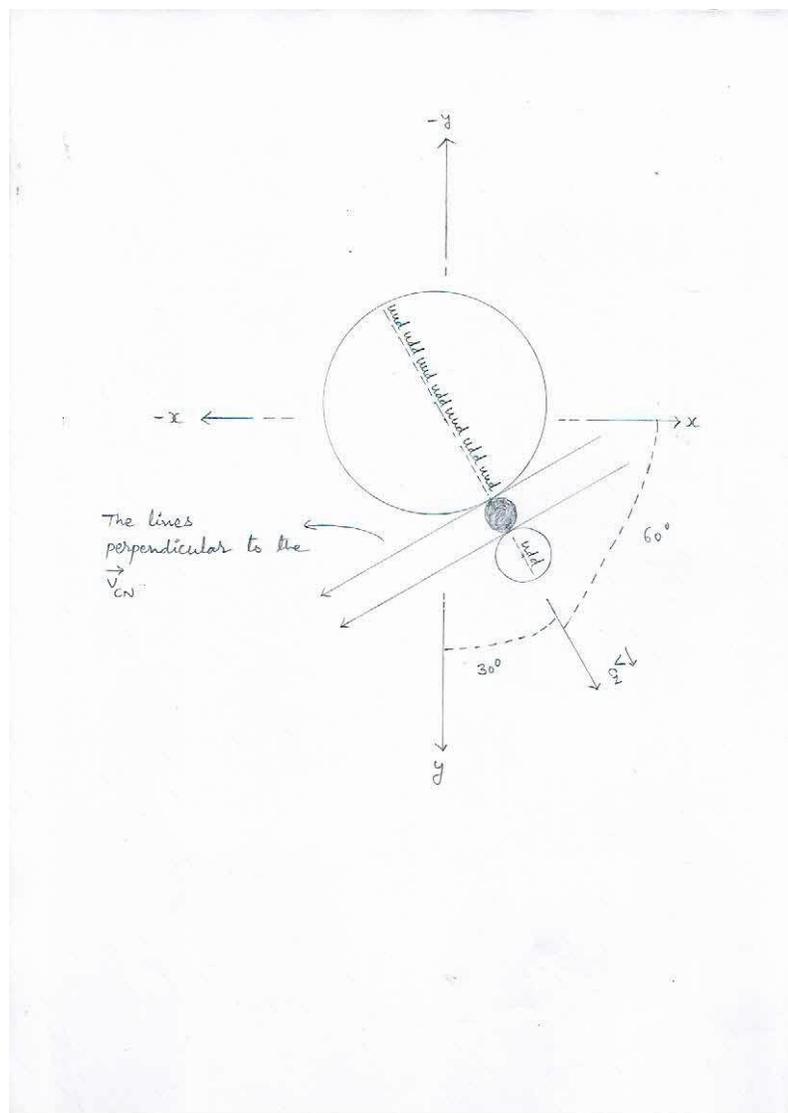
$$M\vec{V}_{cn} = (m_{Be-7} + \Delta m + m_n)\vec{V}_{cn}$$

Where ,

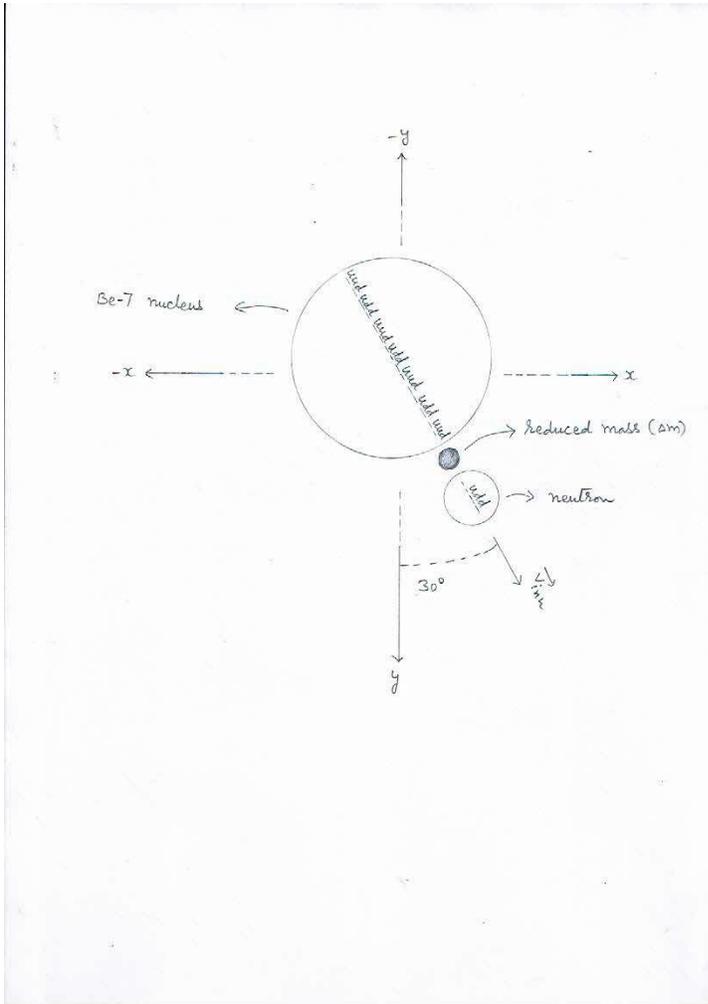
M	= mass of the compound nucleus
\vec{V}_{cn}	= velocity of the compound nucleus
m_{Be-7}	= mass of the beryllium – 7 nucleus
Δm	= reduced mass
m_n	= mass of the neutron

The splitting of the heterogeneous compound nucleus

The heterogeneous compound nucleus to show the lines perpendicular to the \vec{V}_{cn}



The splitting of the heterogeneous compound nucleus



Inherited velocity of the particles (s) :-

Each particle has inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{v}_{cn}).

(I). Inherited velocity of the particle ${}^4_7\text{Be}$

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle beryllium -7

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

II. Inherited velocity of the neutron

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the neutron

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(iii) Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{Li-6}] - [m_{Be-7} + m_n]$$

$$\Delta m = [2.01355 + 6.01347708] - [7.01473555 + 1.00866] \text{ amu}$$

$$\Delta m = [8.02702708] - [8.02339555] \text{ amu}$$

$$\Delta m = 0.00363153 \text{ amu}$$

$$\Delta m = 0.00363153 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm).

$$E_{inh} = \frac{1}{2} \Delta m V_{CN}^2$$

$$\Delta m = 0.00363153 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{\text{CN}}^2 = 0.08647192899 \times 10^{14}$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.00363153 \times 1.6605 \times 10^{-27} \times 0.08647192899 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00026071959 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.000162 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta mc^2$$

$$E_R = 0.00363153 \times 931 \text{ Mev}$$

$$E_R = 3.380954 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{\text{inh}} + E_R$$

$$E_T = [0.000162 + 3.380954] \text{ Mev}$$

$$E_T = 3.381116 \text{ Mev}$$

Increased in the energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses . so,the increased energy (E_{inc}) of the particles are :-

1.. For **beryllium – 7**

$$E_{inc} = \frac{m_n}{m_n + m_{Be-7}} \times E_T$$

$$E_{inc} = \frac{1.00866}{[1.00866 + 7.01473555]} \text{ amu} \times 3.381116 \text{ Mev}$$

$$E_{inc} = \frac{1.00866}{8.02339555} \times 3.381116 \text{ Mev}$$

8.02339555

$$E_{inc} = 0.12571485398 \times 3.381116 \text{ Mev}$$

$$E_{inc} = 0.425056 \text{ Mev}$$

2..increased energy of the neutron

$$E_{inc} = [E_T] - [\text{increased energy of the Be-7}]$$

$$E_{inc} = [3.381116] - [0.425056] \text{ Mev}$$

$$E_{inc} = 2.95606 \text{ Mev}$$

6..Increased velocity of the particles .

(1) For neutron

$$E_{inc} = \frac{1}{2} m_n v_{inc}^2$$

$$v_{inc} = [2 \times E_{inc} / m_n]^{1/2}$$

$$= \frac{2 \times 2.95606 \times 1.6 \times 10^{-13} \text{ J}}{1.6749 \times 10^{-27} \text{ kg}}^{1/2} \text{ m/s}$$

$$\left(\frac{9.459392 \times 10^{-13}}{1.6749 \times 10^{-27}} \right)^{1/2} \text{ m/s}$$

$$= [5.64773538718 \times 10^{14}]^{1/2} \text{ m/s}$$

$$= 2.3764 \times 10^7 \text{ m/s}$$

For beryllium-7

$$v_{inc} = [2 \times E_{inc} / m_{Be-7}]^{1/2}$$

$$= \frac{2 \times 0.425056 \times 1.6 \times 10^{-13} \text{ J}}{11.6479 \times 10^{-27} \text{ kg}}^{1/2} \text{ m/s}$$

$$= \left(\frac{1.3601792 \times 10^{-13}}{11.6479 \times 10^{-27}} \right)^{1/2} \text{ m/s}$$

$$= [0.1167746289 \times 10^{14}]^{1/2} \text{ m/s}$$

$$= 0.3417 \times 10^7 \text{ m/s}$$

7 Angle of propulsion

1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum.

2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus(\vec{V}_{CN}) .]

3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

so, the neutron is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .
While the **beryllium-7** is propelled making 240° angle with x-axis , 150° angle with y-axis and 90° angle with z-axis .

$$\vec{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 0.3417 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(240) = -0.5$$

$$\vec{1}_{V_x} = 0.3417 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.1708 \times 10^7 \text{ m/s}$$

$$\vec{2}_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(150) = -0.866$$

$$\vec{2}_{V_y} = 0.3417 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.2959 \times 10^7 \text{ m/s}$$

$$\vec{3}_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\vec{3}_{V_z} = 0.3417 \times 10^7 \times 0$$

$$= 0 \text{ m/s}$$

For neutron

$$\vec{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.3764 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\vec{1}_{V_x} = 2.3764 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 1.1882 \times 10^7 \text{ m/s}$$

$$\vec{2}_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(30) = 0.866$$

$$\vec{2}_{V_y} = 2.3764 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 2.0579 \times 10^7 \text{ m/s}$$

$$\vec{3}_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos(90) = 0$$

$$\vec{3}_{V_z} = 2.3764 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9.. Components of the final velocity(V_f) of the particles

For beryllium-7

According to-	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) $=(\vec{v}_{inh} + \vec{v}_{inc})$
X-axis	$\vec{v}_x = 0.1470$ $\times 10^7 \text{ m/s}$	$\vec{v}_x = -0.1708$ $\times 10^7 \text{ m/s}$	$\vec{v}_x = -0.0238$ $\times 10^7 \text{ m/s}$
y-axis	$\vec{v}_y = 0.2546 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.2959 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.0413 \times 10^7 \text{ m/s}$
z-axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..For neutron

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) $=(\vec{v}_{inh} + \vec{v}_{inc})$
X-axis	$\vec{v}_x = 0.1470$ $\times 10^7 \text{ m/s}$	$\vec{v}_x = 1.1882$ $\times 10^7 \text{ m/s}$	$\vec{v}_x = 1.3352$ $\times 10^7 \text{ m/s}$
y-axis	$\vec{v}_y = 0.2546$ $\times 10^7 \text{ m/s}$	$\vec{v}_y = 2.0579$ $\times 10^7 \text{ m/s}$	$\vec{v}_y = 2.3125$ $\times 10^7 \text{ m/s}$
z-axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final velocity (v_f) of the beryllium-7

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.0238 \times 10^7 \text{ m/s}$$

$$V_y = 0.0413 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.0238 \times 10^7)^2 + (0.0413 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.00056644 \times 10^{14}) + (0.00170569 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.00227213 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.0476 \times 10^7 \text{ m/s}$$

Final kinetic energy of the beryllium-7

$$E = \frac{1}{2} m_{\text{Be-7}} V_f^2$$

$$E = \frac{1}{2} \times 11.6479 \times 10^{-27} \times 0.00227213 \times 10^{14} \text{ J}$$

$$= 0.01323277151 \times 10^{-13} \text{ J}$$

$$= 0.008270 \text{ Mev}$$

$$m_{\text{Be-7}} V_f^2 = 11.6479 \times 10^{-27} \times 0.00227213 \times 10^{14} \text{ J}$$

$$= 0.0264 \times 10^{-13} \text{ J}$$

Forces acting on the **beryllium-7** nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.0238 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 4 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 4 \times 1.6 \times 10^{-19} \times 0.0238 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.1524 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

so,

$$\vec{F}_y = 0.1524 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 4 \times 1.6 \times 10^{-19} \times 0.0238 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.1525 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (+) Z-axis,

so,

$$\vec{F}_z = 0.1525 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = -0.0413 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = 1.001 \times 10^{-1} \text{ Tesla}$$

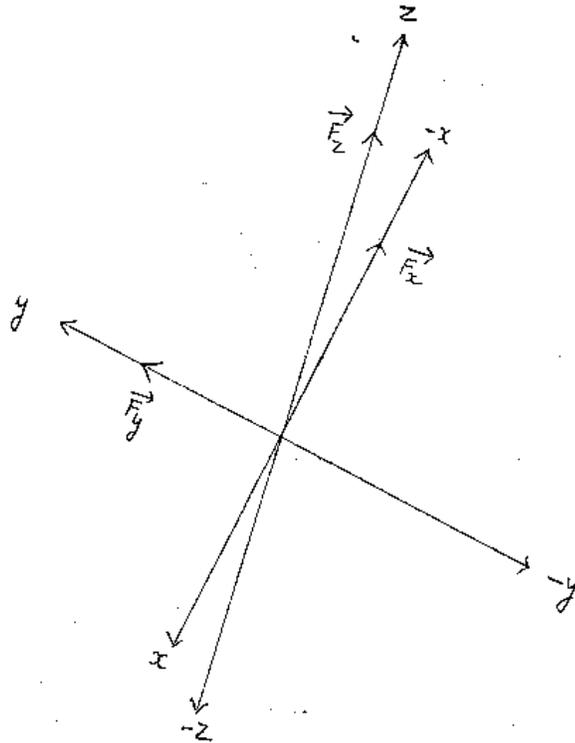
$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_x &= 4 \times 1.6 \times 10^{-19} \times 0.0413 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 0.2645 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x axis,

$$\text{so, } \vec{F}_x = -0.2645 \times 10^{-13} \text{ N}$$

Forces acting on the beryllium-7



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 0.2645 \times 10^{-13} \text{ N}$$

$$F_y = 0.1524$$

$$F_z = 0.1525 \times 10^{-13} \text{ N}$$

$$F_R^2 = (0.2645 \times 10^{-13})^2 + (0.1524 \times 10^{-13})^2 + (0.1525)^2 \text{ N}^2$$

$$F_R^2 = (0.06996025 \times 10^{-26}) + (0.02322576 \times 10^{-26}) + (0.02325625) \text{ N}^2$$

$$F_R^2 = 0.11644226 \times 10^{-26} \text{ N}^2$$

$$F_R = 0.3412 \times 10^{-13} \text{ N}$$

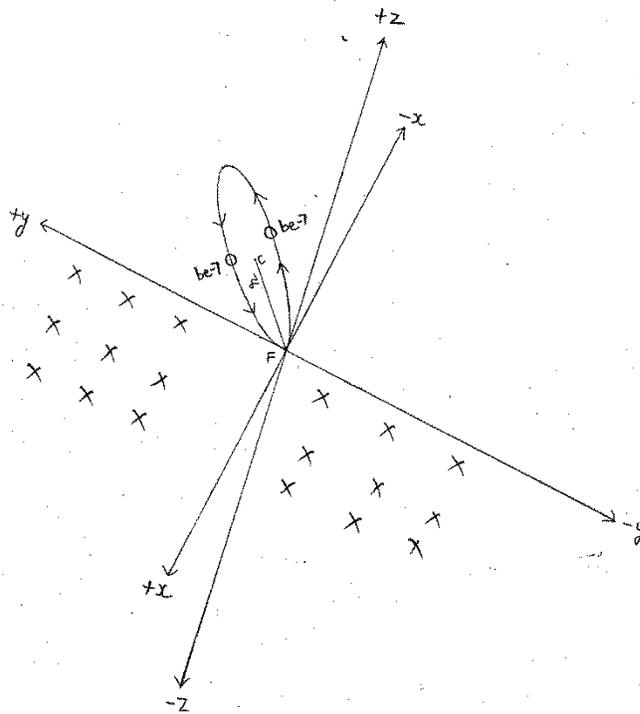
Resultant force acting on the beryllium -7

$$\begin{aligned}r &= mv^2 / F_R \\mv^2 &= 0.0264 \times 10^{-13} \text{ J} \\F_r &= 0.3412 \times 10^{-13} \text{ N} \\0.0264 \times 10^{-13} \text{ J} \\r &= \frac{\quad}{0.3412 \times 10^{-13} \text{ N}}\end{aligned}$$

$$r = 0.0773 \text{ m}$$

The circular orbit to be followed by the beryllium -7 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

C = center of the circular orbit to be followed by the beryllium -7.



The plane of the circular orbit to be followed by the beryllium -7 nucleus makes angles with positive x, y and z-axes as follows :-

1 with x-axis

$$\cos \alpha = \frac{F_r \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\vec{F}_x = -0.2645 \times 10^{-13} \text{ N}$$

$$F_r = 0.3412 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7752$$

$$\alpha = 219.17 \text{ degree } [\because \cos(219.17) = -0.7752]$$

2 with y- axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{F_y}{F_r}$$

$$\vec{F}_y = 0.1524 \times 10^{-13} \text{ N}$$

$$F_r = 0.3412 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4466$$

$$\beta = 63.47 \text{ degree } [\because \cos(63.47) = 0.4466]$$

3 with z- axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{F_z}{F_r}$$

$$\vec{F}_z = 0.1525 \times 10^{-13} \text{ N}$$

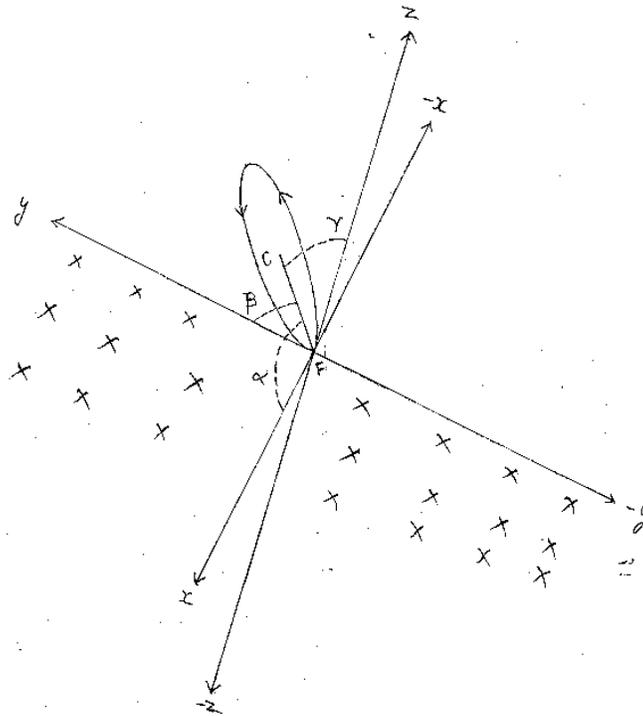
$$F_r = 0.3412 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4469$$

$$\gamma = 63.45 \text{ degree}$$

The plane of the circular orbit to be followed by the beryllium -7 nucleus makes angles with positive x, y, and z axes as follows :-



Where,

$$\alpha = 219.17 \text{ degree}$$

$$\beta = 63.47 \text{ degree}$$

$$\gamma = 63.45 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium -7.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 0.0773 \text{ m}$$

$$= 0.1546 \text{ m}$$

$$\cos \alpha = -0.7752$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 0.1546 \times (-0.7752) \text{ m}$$

$$x_2 - x_1 = -0.1198 \text{ m}$$

$$x_2 = -0.1198 \text{ m} [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$d$$

$$\cos \beta = 0.4466$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 0.1546 \times 0.4466 \text{ m}$$

$$y_2 - y_1 = 0.0690 \text{ m}$$

$$y_2 = 0.0690 \text{ m} [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$d$$

$$\cos \gamma = 0.4469$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 0.1546 \times 0.4469 \text{ m}$$

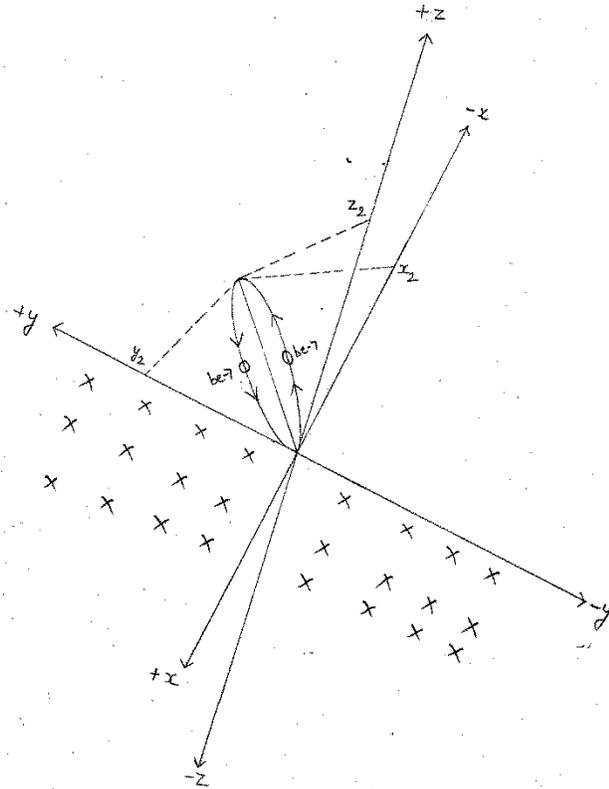
$$z_2 - z_1 = 0.0690 \text{ m}$$

$$z_2 = 0.0690 \text{ m} [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium-7 are as shown below.

The line ___ is the diameter of the circle .

P_1P_2



Conclusion :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the beryllium-7 nucleus are along **-x, +y and +z** axes respectively .

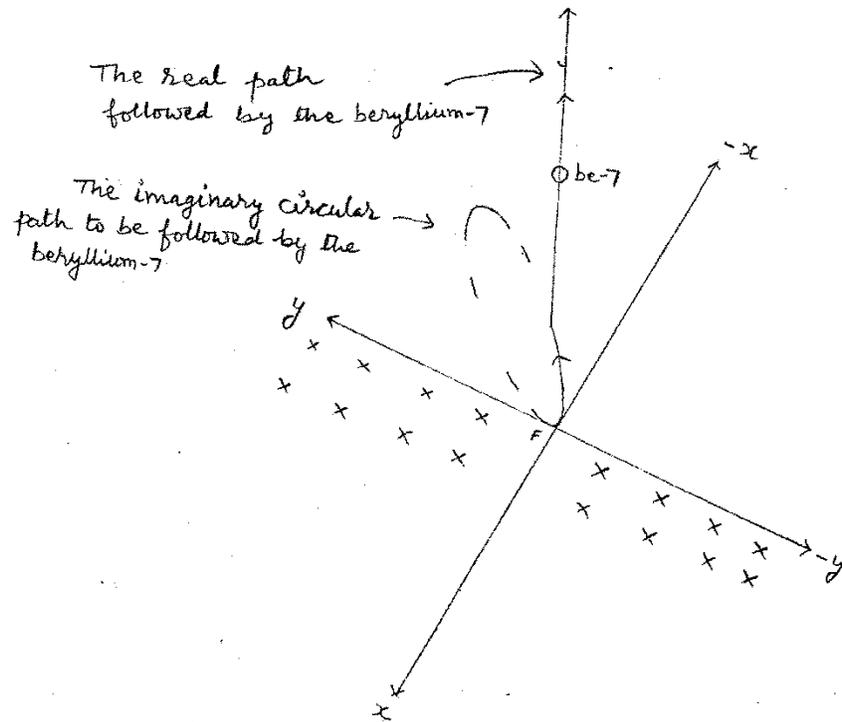
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the beryllium-7 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-7 nucleus to undergo to a circular orbit of radius 0.0773 m .

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.1198 \text{ m}, 0.0690 \text{ m}, 0.0690 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the beryllium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , in spite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

Hence the beryllium-7 nucleus is not confined.



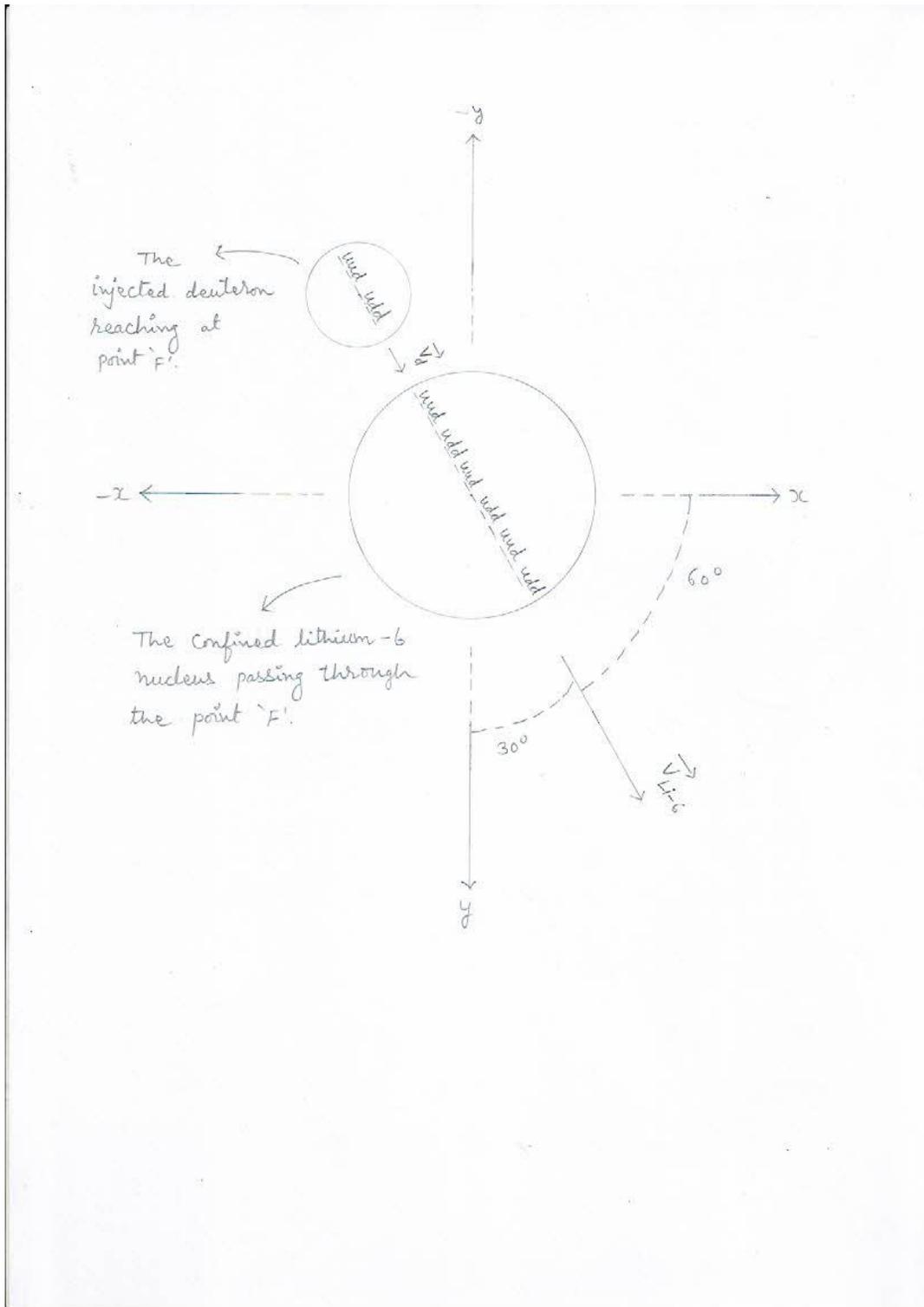
For fusion reaction



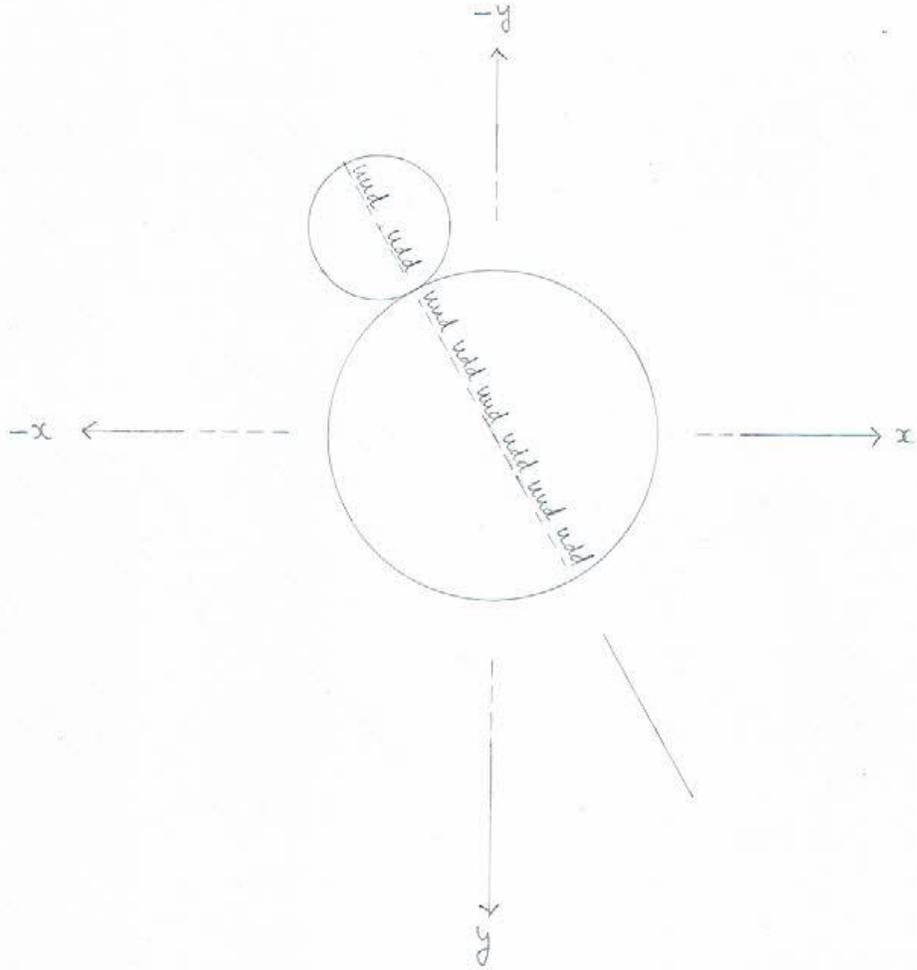
The interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined lithion-6] with the confined lithion-6 passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined lithion-6.

Interaction of nuclei (1)



Interaction of nuclei (2)

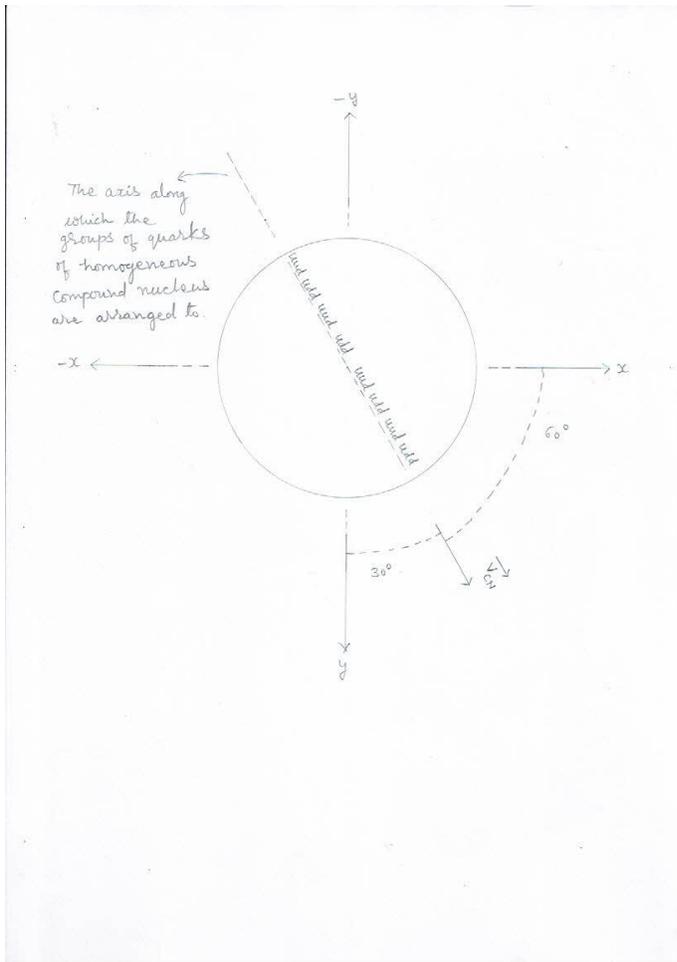


2. Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron and the lithium-6 nucleus) behave like a liquid and form a homogeneous compound nucleus . having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 8 groups of quarks surrounded by the gluons.

The homogenous compound nucleus



where,

$$\alpha = 60 \text{ degrees}$$

$$\beta = 30 \text{ degrees}$$

3. Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogenous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the just lower nucleus (the hellion-4) than the reactant one (the lithion-6) includes the other three (nearby located) groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

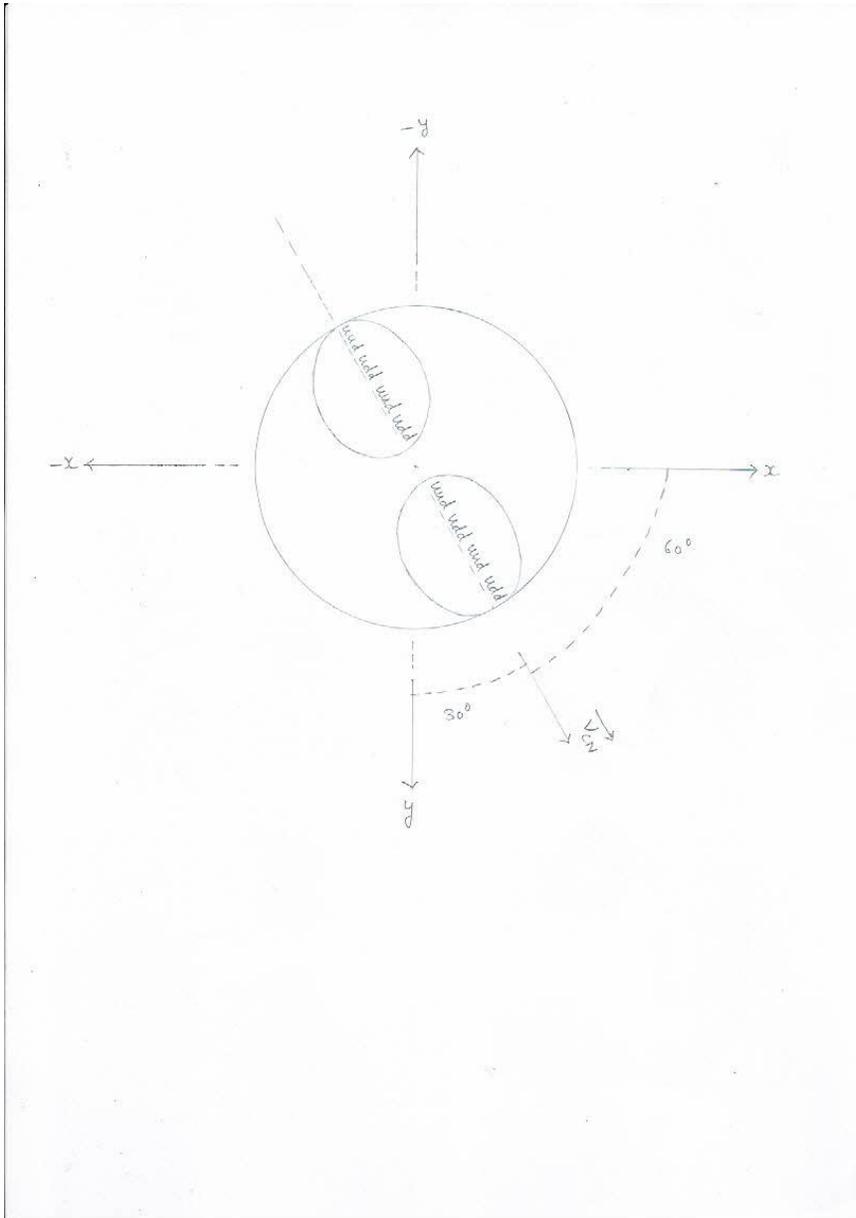
While , the remaining groups of quarks to become a stable nucleus (the hellion-4) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe ' A '] and rearrange to form the ' B ' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two dissimilar lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the one nucleus is the hellion-4 nucleus and the other nucleus is the hellion-4.

The one nucleus is the lobe ' A ' and the other nucleus is the lobe ' B ' while the remaining space represent the remaining gluons .



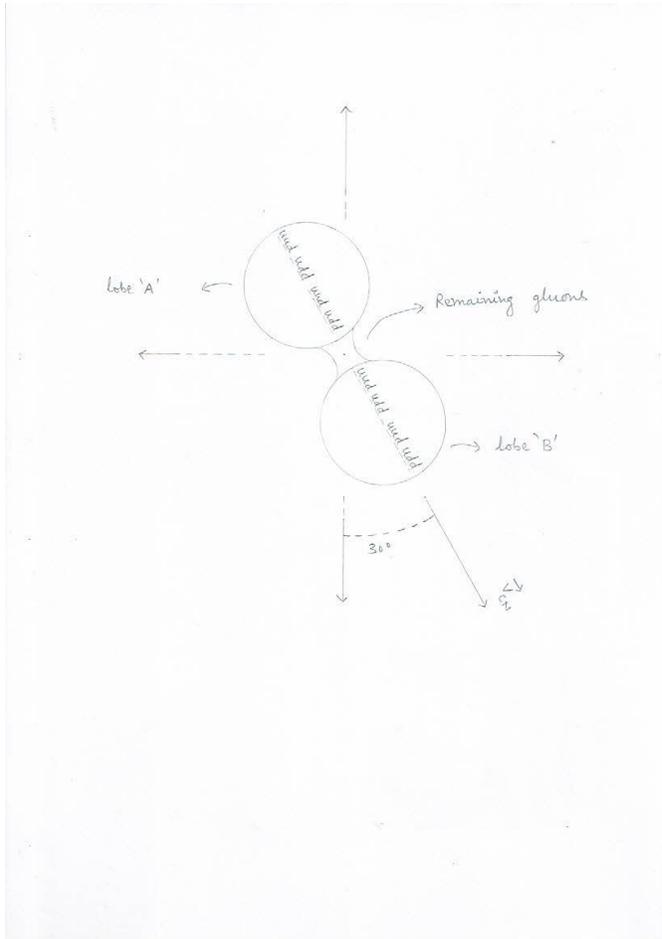
Formaton of lobes

4..Final stage of the heterogeneous compound nucleus :-

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

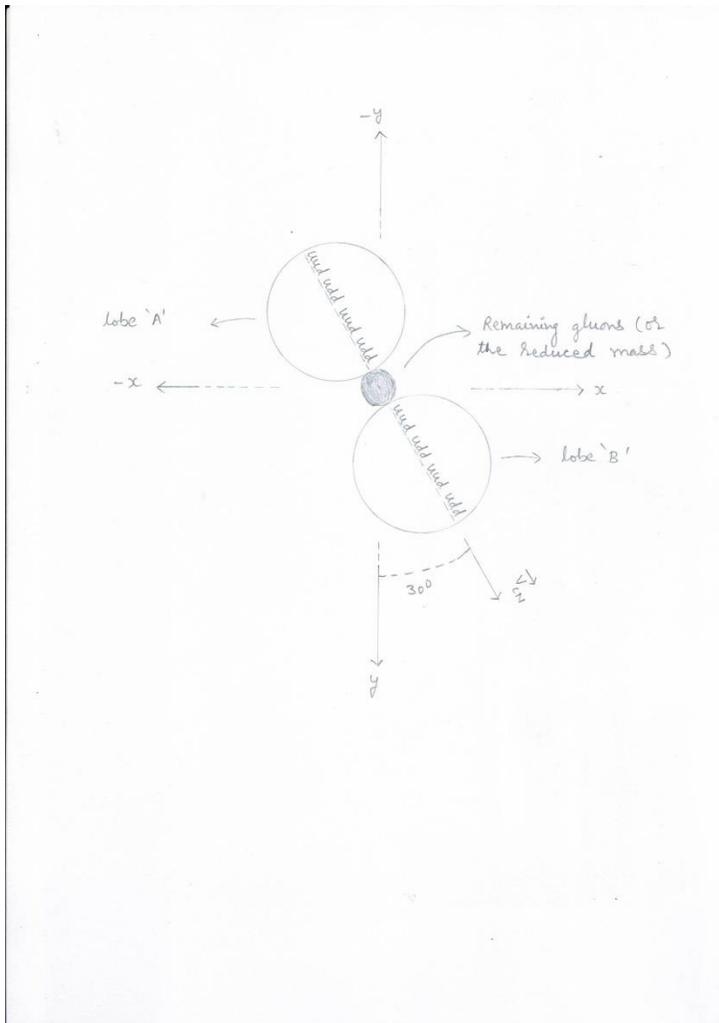
So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogenous compound nucleus

For $\alpha = 60$ degree

$\beta = 30$ degree



Final stage of the heterogeneous compound nucleus

where, $\alpha = 60$ degree

$\beta = 30$ degree

Formation of compound nucleus :

As the deuteron (of n^{th} bunch reaches at point F) it fuses with the confined lithium-6 to form a compound nucleus .

1. Just before fusion, to overcome the electrostatic repulsive force exerted by the lithium-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves its energy equal to 45.5598 kev.

so, just before fusion,

the kinetic energy of n^{th} deuteron is –

$$E_b = 153.6 \text{ kev} - 45.5598 \text{ kev}$$

$$= 108.0402 \text{ kev}$$

$$= 0.1080402 \text{ Mev}$$

2. Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron, the lithium-6 loses (radiates its energy in the form of electromagnetic waves its energy equal to 136.0700kev.

so, just before fusion,

the kinetic energy of lithium-6 is –

$$E_b = 388.2043 \text{ kev} - 136.0700 \text{ kev}$$

$$= 252.1343 \text{ kev}$$

$$= 0.2521343 \text{ Mev}$$

Kinetic energy of the compound nucleus :-

$$\text{K.E.} = [E_b \text{ of deuteron}] + [E_b \text{ of lithium-6}]$$

$$= [108.0402 \text{ Kev}] + [252.1343 \text{ Kev}]$$

$$= 360.1745 \text{ Kev.}$$

$$= 0.3601745 \text{ Mev}$$

Mass of the compound nucleus

$$M = m_d + m_{\text{Li-6}}$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}]$$

$$= 13.3287 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3601745 \text{ Mev}$$

$$V_{\text{CN}} = \left[\frac{2 \times 0.3601745 \times 1.6 \times 10^{-13}}{13.3287 \times 10^{-27} \text{ kg}} \right]^{\frac{1}{2}} \text{ m/s}$$

$$V_{\text{CN}} = \left[1.1525584 \times 10^{-13} \right]^{\frac{1}{2}} \text{ m/s}$$

$$13.3287 \times 10^{-27}$$

$$V_{CN} = [0.08647192899 \times 10^{14}]^{\frac{1}{2}} \text{ m/s}$$

$$V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$\begin{aligned} \vec{V}_X &= V_{CN} \cos \alpha \\ &= 0.2940 \times 10^7 \times 0.5 \quad \text{m/s} \\ &= 0.1470 \times 10^7 \quad \text{m/s} \end{aligned}$$

$$\vec{V}_y = V_{CN} \cos \beta$$

$$\begin{aligned} &= 0.2940 \times 10^7 \times 0.866 \quad \text{m/s} \\ &= \mathbf{0.2546} \text{ m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_z &= V_{CN} \cos \gamma \\ &= 0.2940 \times 10^7 \times 0 \quad \text{m/s} \\ &= 0 \quad \text{m/s} \end{aligned}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus, due to its instability, splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – helium-4, the helium-4 and the reduced mass (Δm).

Out of them , the two particles (the helion-4, and helion-4) are stable while the third one (reduced mass) isunstable .

According to the law of inertia , each particle that is produced due to splitting of the compound nucleus , hasan inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus(\vec{V}_{cn}) .

So, for conservation of momentum

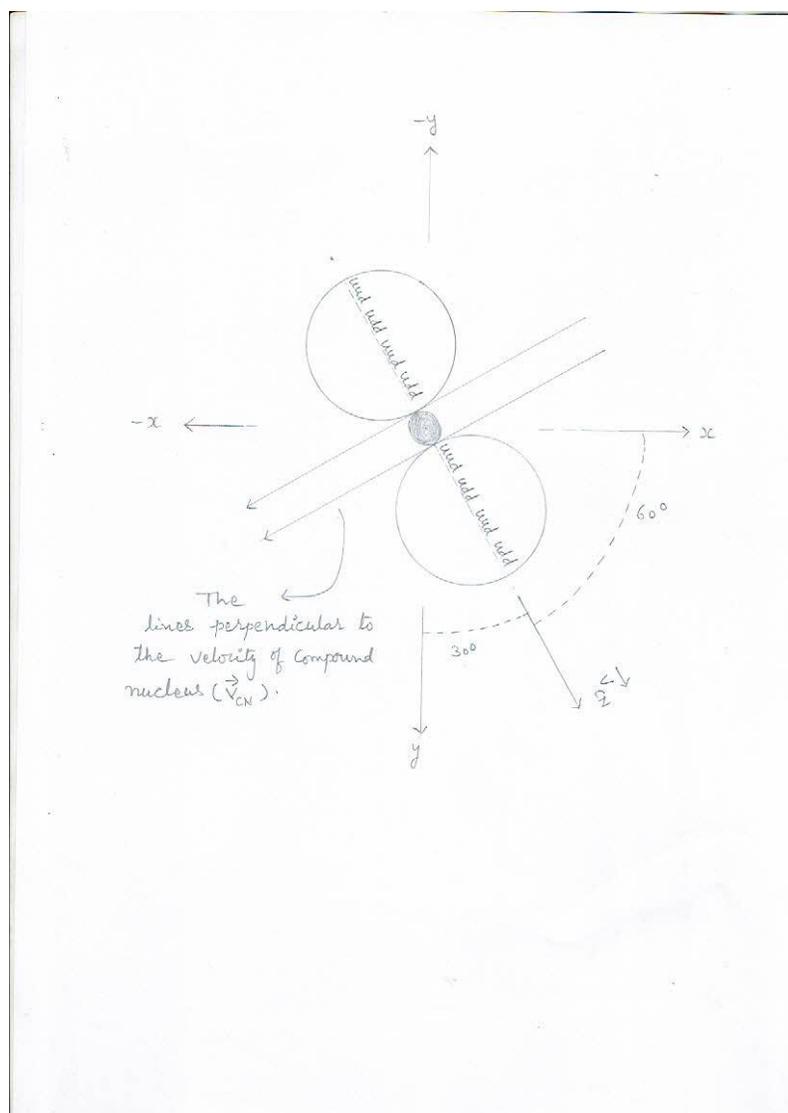
$$M\vec{V}_{cn} = (m_{He-4} + \Delta m + m_{He-4})\vec{V}_{cn}$$

Where ,

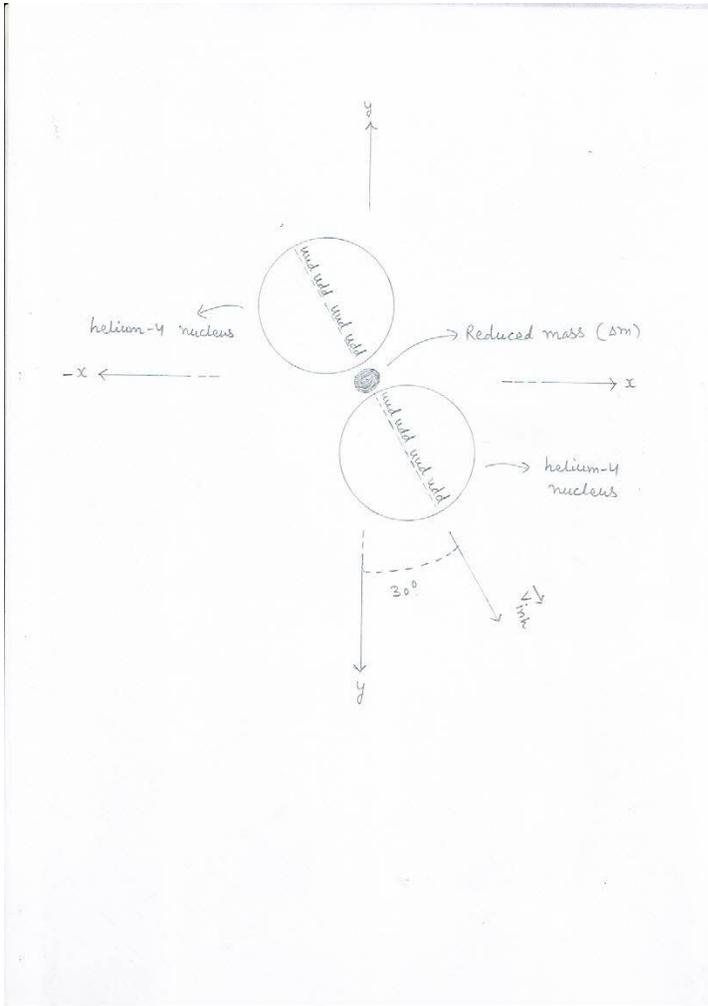
M	= massof the compound nucleus
\vec{V}_{cn}	= velocity of the compound nucleus
m_{He-4}	= mass of thehellion-4 nucleus
Δm	= reduced mass

The splitting of the heterogenous compound nucleus

The heterogenous compound nucleus to show the lines perpendicular tothe \vec{V}_{cn}



The splitting of the heterogeneous compound nucleus



Inherited velocity of the particles (s) : -

Each particles has inherited velocity ($\frac{\vec{v}}{v_{inh}}$) equal to the velocity of the compound nucleus ($\frac{\vec{v}}{v_{cn}}$). There, due to splitting, two helium -4 nuclei are produced.

(I). Inherited velocity of the each helium -4 nucleus

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the each helium -4 nucleus

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(ii) Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{Li-6}] - [m_{He-4} + m_{He-4}]$$

$$= [m_d + m_{Li-6}] - 2[m_{He-4}]$$

$$\Delta m = [2.01355 + 6.01347708] - 2[4.0015] \text{ amu}$$

$$\Delta m = [8.02702708] - [8.003] \text{ amu}$$

$$\Delta m = 0.02402708 \text{ amu}$$

$$\Delta m = 0.02402708 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm).

$$E_{inh} = \frac{1}{2} \Delta m V_{CN}^2$$

$$\Delta m = 0.02402708 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{\text{CN}}^2 = 0.08647192899 \times 10^{14}$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.02402708 \times 1.6605 \times 10^{-27} \times 0.08647192899 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00172498382 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.001078 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta mc^2$$

$$E_R = 0.02402708 \times 931 \text{ Mev}$$

$$E_R = 22.369211 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{\text{inh}} + E_R$$

$$E_T = [0.001078 + 22.369211] \text{ Mev}$$

$$E_T = 22.370289 \text{ Mev}$$

Increased in the energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses . so,the increased energy (E_{inc}) of the particles are :-

1.Increased kinetic energy of each helium-4 nucleus

$$E_{inc} = \frac{m_{He-4}}{m_{He-4} + m_{He-4}} \times E_T$$

$$E_{inc} = E_T/2$$

$$E_{inc} = 22.370289 / 2 \quad \text{Mev}$$

$$E_{inc} = 11.185144 \quad \text{Mev}$$

6..Increased velocity of each of the helium-4 nucleus .

(1) For helium-4 nucleus

$$E_{inc} = \frac{1}{2} m_{He-4} V_{inc}^2$$

$$V_{inc} = \left[2 \times E_{inc} / m_{He-4} \right]^{1/2}$$

$$= \left(\frac{2 \times 11.185144 \times 1.6 \times 10^{-13} \text{ J}}{6.64449 \times 10^{-27} \text{ kg}} \right)^{1/2} \text{ m/s}$$

$$= \left(\frac{35.7924608 \times 10^{-13}}{6.64449 \times 10^{-27}} \right)^{1/2} \text{ m/s}$$

$$\begin{aligned}
 & 6.64449 \times 10^{-27} \\
 & = [5.38678827118 \times 10^{14}]^{1/2} \text{ m/s} \\
 & = 2.3209 \times 10^7 \text{ m/s}
 \end{aligned}$$

7 Angle of propulsion

- 1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum.

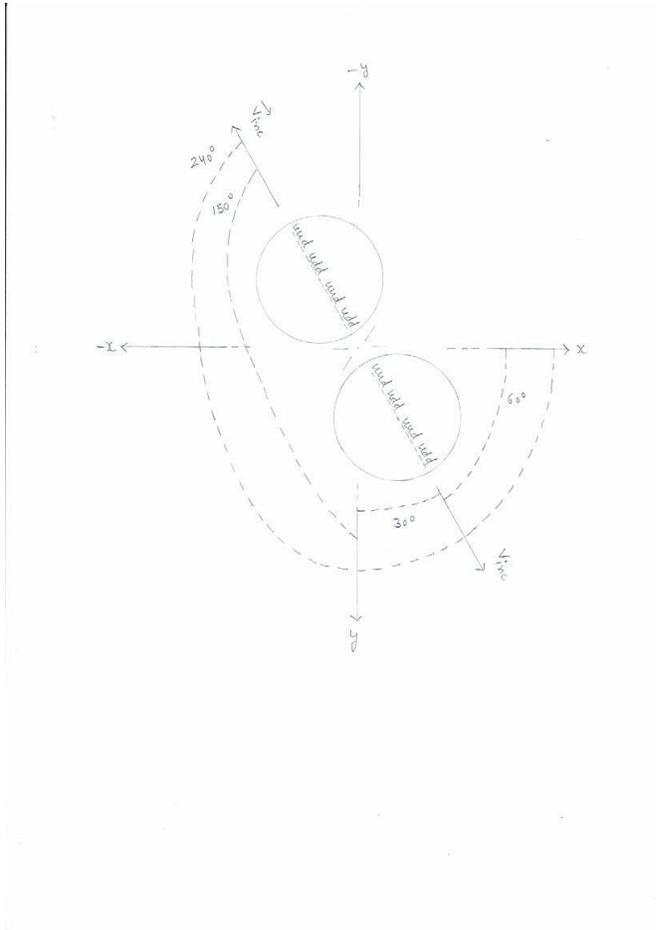
2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus($\overrightarrow{V_{CN}}$) .]

- 3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

so, the one helium-4 is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

While the other helium-4 is propelled making 240° angle with x-axis , 150° angle with y-axis and 90° angle with z-axis .

Propulsion of the particles



Components of the increased velocity (V_{inc}) of the particles.

(i) For left hand side propelled helion-4

$$1 \rightarrow_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.3209 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(240) = -0.5$$

$$\rightarrow_{V_x} = 2.3209 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -1.1604 \times 10^7 \text{ m/s}$$

$$2 \rightarrow_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(150) = -0.866$$

$$\rightarrow_{V_y} = 2.3209 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -2.0098 \times 10^7 \text{ m/s}$$

$$3 \rightarrow_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\rightarrow_{V_z} = 2.3209 \times 10^7 \times 0$$

$$= 0 \text{ m/s}$$

For right hand side propelled helion-4

$$1 \rightarrow_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.3209 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\rightarrow_{V_x} = 2.3209 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 1.1604 \times 10^7 \text{ m/s}$$

$$2 \rightarrow_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(30) = 0.866$$

$$\rightarrow_{V_y} = 2.3209 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 2.0098 \times 10^7 \text{ m/s}$$

$$3 \rightarrow_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos(90) = 0$$

$$\rightarrow_{V_z} = 2.3209 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9.. Componentsof the final velocity(Vf)oftheparticles

1 For right hand side propelled helion-4

According to -	Inherited Velocity(\vec{V}_{inh})	Increased Velocity(\vec{V}_{inc})	Final velocity (\vec{V}_f)= $(\vec{V}_{inh})+(\vec{V}_{inc})$
X – axis	$\vec{v}_x = 0.1470 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.1604 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.3074 \times 10^7 \text{ m/s}$
y –axis	$\vec{v}_y = 0.2546 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.0098 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.2644 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2.. Forleft hand side propelled helion-4

According to -	Inherited Velocity(\vec{V}_{inh})	Increased Velocity(\vec{V}_{inc})	Finalvelocity (\vec{V}_f)= $(\vec{V}_{inh})+(\vec{V}_{inc})$
X – axis	$\vec{v}_x = 0.1470 \times 10^7 \text{ m/s}$	$\vec{v}_x = -1.1604 \times 10^7 \text{ m/s}$	$\vec{v}_x = -1.0134 \times 10^7 \text{ m/s}$
y –axis	$\vec{v}_y = 0.2546 \times 10^7 \text{ m/s}$	$\vec{v}_y = -2.0098 \times 10^7 \text{ m/s}$	$\vec{v}_y = -1.7552 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10..Final velocity (vf) of For right hand side propelled helion-4

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 1.3074 \times 10^7 \text{ m/s}$$

$$V_y = 2.2644 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (1.3074 \times 10^7)^2 + (2.2644 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (1.70929476 \times 10^{14}) + (5.12750736 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 6.83680212 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 2.6147 \times 10^7 \text{ m/s}$$

Final kinetic energy of right hand side propelled helion-4

$$E = \frac{1}{2} m_{\text{He-4}} V_f^2$$

$$E = \frac{1}{2} \times 6.64449 \times 10^{-27} \times 6.83680212 \times 10^{14} \text{ J}$$

$$= 22.7135316591 \times 10^{-13} \text{ J}$$

$$= 14.1959 \text{ Mev}$$

$$m_{\text{He-4}} V_f^2 = 6.64449 \times 10^{-27} \times 6.83680212 \times 10^{14} \text{ J}$$

$$= 45.4270 \times 10^{-13} \text{ J}$$

10.. Final velocity (v_f) of left hand side propelled helion-4

$$V_f^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 1.0134 \times 10^7 \text{ m/s}$$

$$V_y = 1.7552 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (1.0134 \times 10^7)^2 + (1.7552 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (1.02697956 \times 10^{14}) + (3.08072704 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 4.1077066 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 2.0267 \times 10^7 \text{ m/s}$$

Final kinetic energy of left hand side propelled helion-4

$$E = \frac{1}{2} m_{\text{He-4}} V_f^2$$

$$V_f^2 = 4.1077066 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$E = \frac{1}{2} \times 6.64449 \times 10^{-27} \times 4.1077066 \times 10^{14} \text{ J}$$

$$= 13.6468077133 \times 10^{-13} \text{ J}$$

$$= 8.5292 \text{ Mev}$$

$$m_{\text{He-4}} V_f^2 = 6.64449 \times 10^{-27} \times 4.1077066 \times 10^{14} \text{ J}$$

$$= 27.2936 \times 10^{-13} \text{ J}$$

Forces acting on the right hand side propelled helion-4

$$1 \ F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = 1.3074 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 2 \times 1.6 \times 10^{-19} \times 1.3074 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 4.1878 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_y is according to (-) y-axis ,

so ,

$$\vec{F}_y = -4.1878 \times 10^{-13} \text{ N}$$

$$2 \ F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 2 \times 1.6 \times 10^{-19} \times 1.3074 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N}$$

$$= 4.1891 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_z is according to (-) Z- axis ,

so ,

$$\vec{F}_z = -4.1891 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = 2.2644 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = 1.001 \times 10^{-1} \text{ Tesla}$$

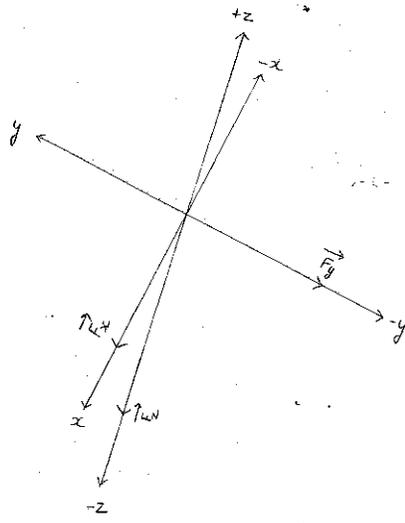
$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_x &= 2 \times 1.6 \times 10^{-19} \times 2.2644 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 7.2533 \times 10^{-13} \text{ N} \end{aligned}$$

From the right hand palm rule , the direction of the force \vec{F}_x is according to (+) x axis ,

$$\text{so } \vec{F}_x = 7.2533 \times 10^{-13} \text{ N}$$

The forces acting on the right hand side propelled helium – 4 nucleus



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 7.2533 \times 10^{-13} \text{ N}$$

$$F_y = 4.1878 \times 10^{-13} \text{ N}$$

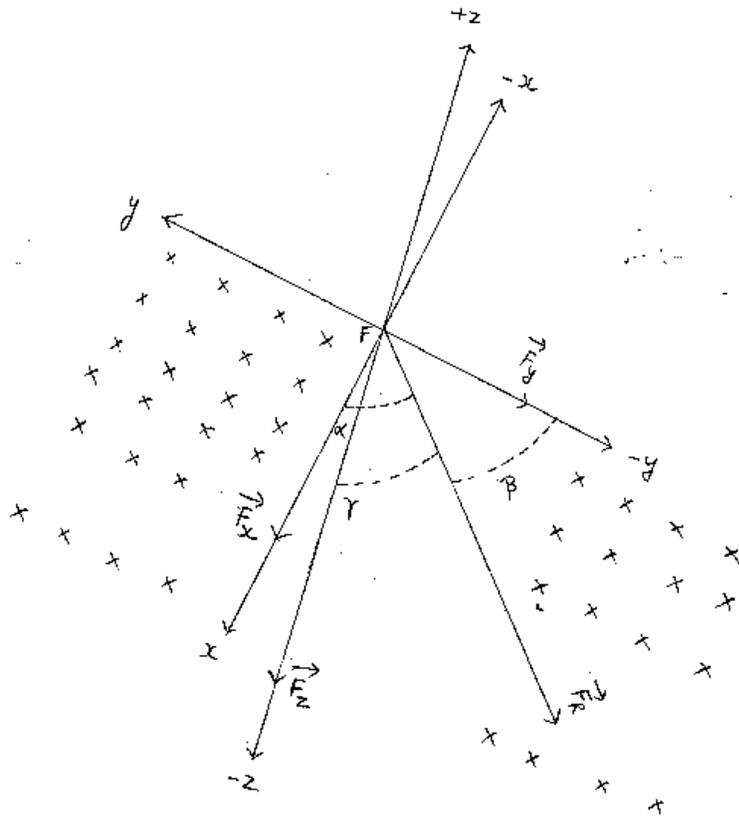
$$F_z = 4.1891 \times 10^{-13}$$

$$F_R^2 = (7.2533 \times 10^{-13})^2 + (4.1878 \times 10^{-13})^2 + (4.1891 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (52.6103 \times 10^{-26}) + (17.53766884 \times 10^{-26}) + (17.54855881 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 87.69652765 \times 10^{-26} \text{ N}^2$$

$$F_R = 9.3646 \times 10^{-13} \text{ N}$$



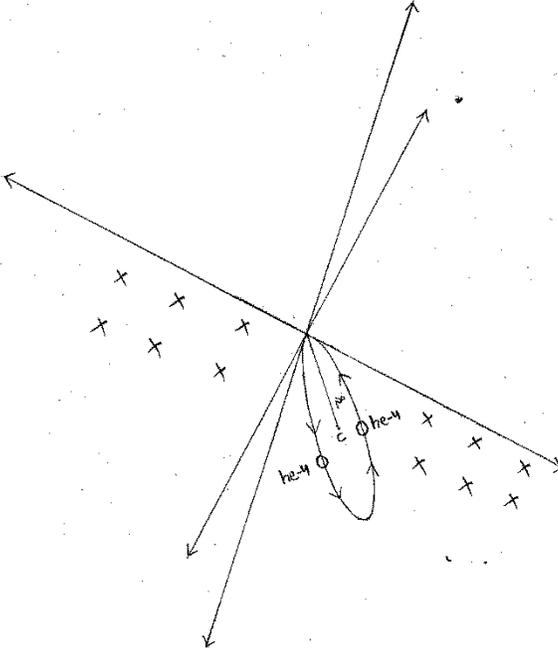
Radius of the circular orbit to be followed by the right hand side propelled helion-4 :

$$\begin{aligned}
 r &= mv^2 / F_R \\
 mv^2 &= 45.4270 \times 10^{-13} \quad \text{J} \\
 F_r &= 9.3646 \times 10^{-13} \quad \text{N} \\
 r &= \frac{45.4270 \times 10^{-13} \text{J}}{9.3646 \times 10^{-13} \quad \text{N}}
 \end{aligned}$$

$$r = 4.8509 \quad \text{m}$$

The circular orbit to be followed by the right hand side propelled helion -4 nucleus lies in the plane made up of positive x-axis, negative y-axis and the negative z-axis.

He-4 = center of the circular orbit to be followed by the right hand side propelled helion -4 nucleus.



The plane of the circular orbit to be followed by the right hand side propelled helion-4 makes angles with positive x, y and z-axes as follows :-

1 with x-axis

$$\cos \alpha = \frac{F_{R \cos \alpha}}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = 7.2533 \times 10^{-13} \text{ N}$$

$$F_r = 9.3646 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos(39.24) = 0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = -4.1878 \times 10^{-13} \text{ N}$$

$$F_r = 9.3646 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4471$$

$$\beta = 243.44 \text{ degree } [\because \cos(243.44) = -0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{\vec{F}_z}{F_r}$$

$$\vec{F}_z = -4.1891 \times 10^{-13} \text{ N}$$

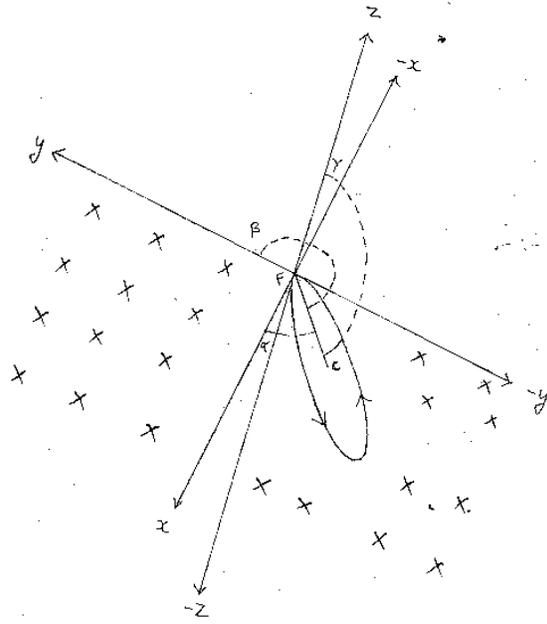
$$F_r = 9.3646 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.425 \text{ degree}$$

The plane of the circular orbit to be followed by the right hand side propelled helion -4 makes angles with positive x, y, and z axes as follows :-



Where,

$$\alpha = 39.24 \text{ degree}$$

$$\beta = 243.44 \text{ degree}$$

$$\gamma = 243.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the right hand side propelled hellion-4 .

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 4.8509 \text{ m}$$

$$= 9.7018 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 9.7018 \times 0.7745 \text{ m}$$

$$x_2 - x_1 = 7.5140 \text{ m}$$

$$x_2 = 7.5140 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$d$$

$$\cos \beta = -0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 9.7018 \times (-0.4471) \text{ m}$$

$$y_2 - y_1 = -4.3376 \text{ m}$$

$$y_2 = -4.3376 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$d$$

$$\cos \gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 9.7018 \times (-0.4473) \text{ m}$$

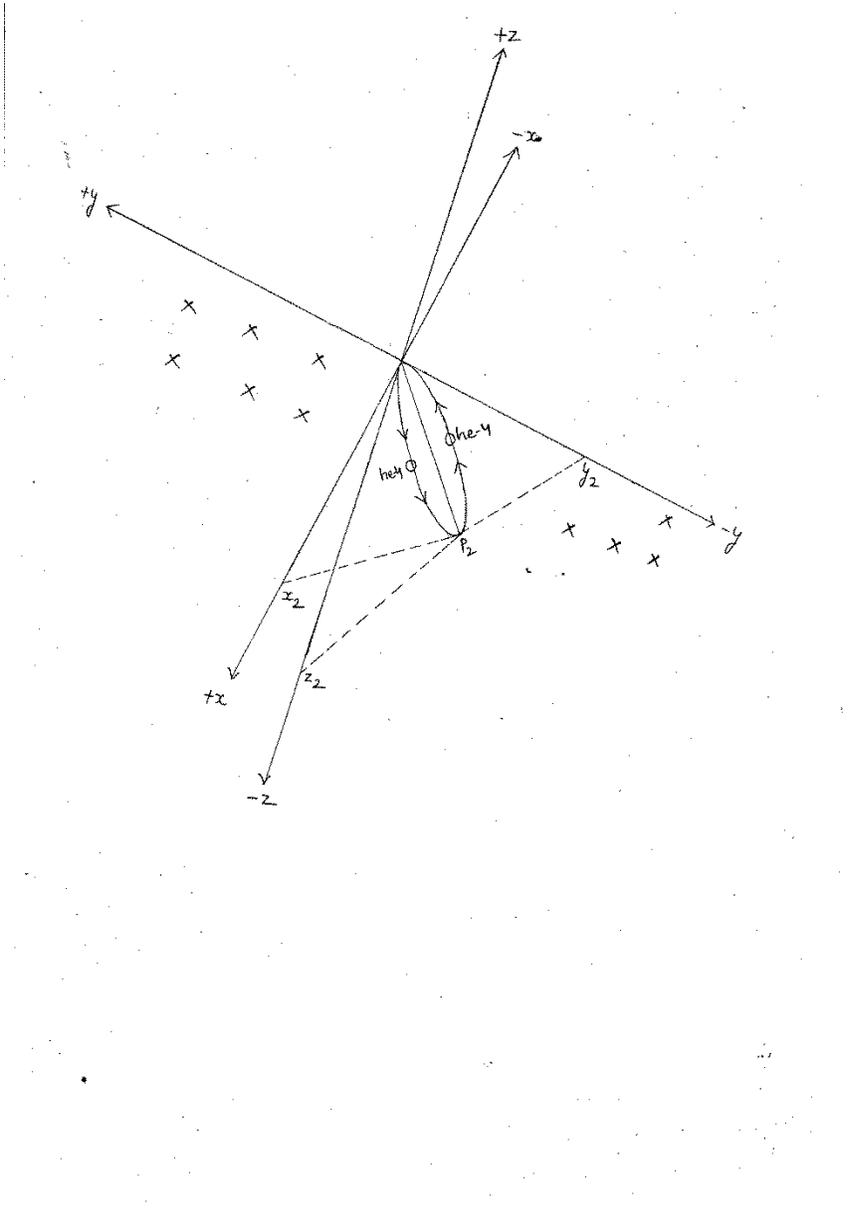
$$z_2 - z_1 = -4.3396 \text{ m}$$

$$z_2 = -4.3396 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the right hand side propelled helion-4 are as shown below.

The line is the diameter of the circle .

P_1P_2



Conclusion :-

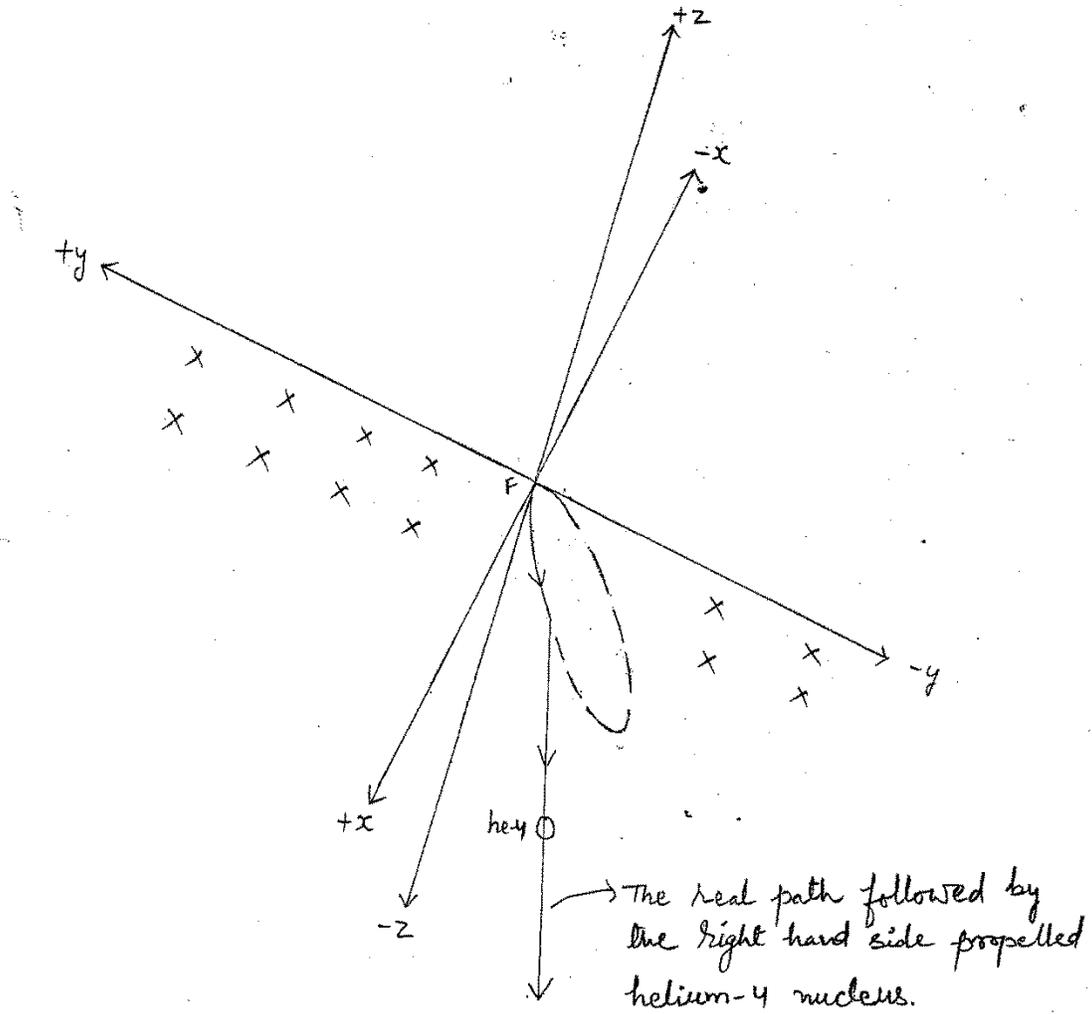
The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the right hand side propelled helion-4 are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the right hand side propelled helion-4 lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the right hand side propelled helion-4 to undergo a circular orbit of radius 4.8509 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(7.5140 \text{ m}, -4.3376 \text{ m}, -4.3396 \text{ m})$. in trying to complete its circle, due to lack of space, it strikes to the base wall of the tokamak.

Hence the right hand side propelled helion-4 is not confined.



(In trying to follow the circular orbit, the right hand side propelled helium-4 nucleus strike to the base wall of the tokamak. So, it can't complete the circle.)

forces acting on the left hand side propelled hellion-4

$$1 F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -1.0134 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_y &= 2 \times 1.6 \times 10^{-19} \times 1.0134 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 3.2461 \times 10^{-13} \text{ N} \end{aligned}$$

Form the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = 3.2461 \times 10^{-13} \text{ N}$$

$$2 F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_z &= 2 \times 1.6 \times 10^{-19} \times 1.0134 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N} \\ &= 3.2470 \times 10^{-13} \text{ N} \end{aligned}$$

Form the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = 3.2470 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = -1.7552 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

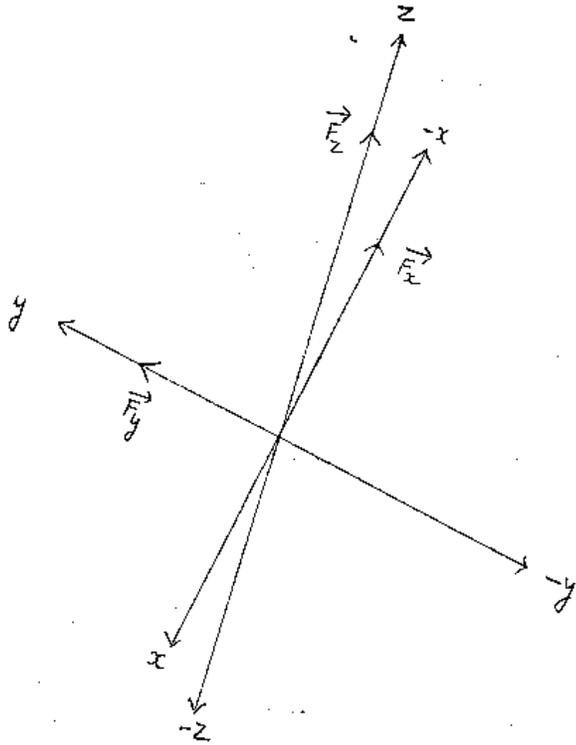
$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_x &= 2 \times 1.6 \times 10^{-19} \times 1.7552 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 5.6222 \times 10^{-13} \text{ N} \end{aligned}$$

Form the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x-axis,

$$\text{so, } \vec{F}_x = -5.6222 \times 10^{-13} \text{ N}$$

Forces acting on the left hand side propelled hellion-4



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 5.6222 \times 10^{-13} \text{ N}$$

$$F_y = 3.2461 \times 10^{-13} \text{ N}$$

$$F_z = 3.2470 \times 10^{-13} \text{ N}$$

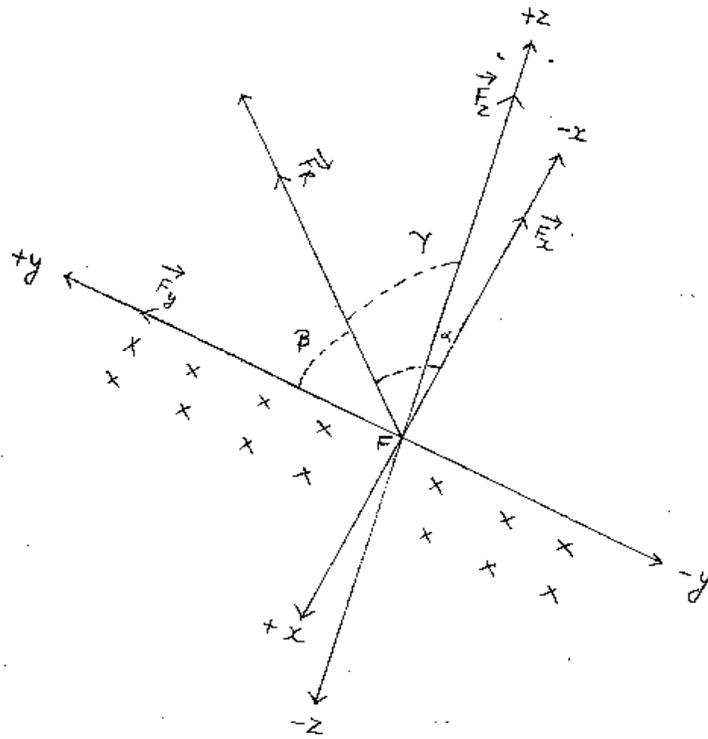
$$F_R^2 = (5.6222 \times 10^{-13})^2 + (3.2461 \times 10^{-13})^2 + (3.2470 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (31.60913284 \times 10^{-26}) + (10.53716521 \times 10^{-26}) + (10.543009 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 52.68930705 \times 10^{-26} \text{ N}^2$$

$$F_R = 7.2587 \times 10^{-13} \text{ N}$$

Resultant force acting on the left hand side propelled helion-4



Radius of the circular orbit to be followed by the left hand side propelled helion-4 :

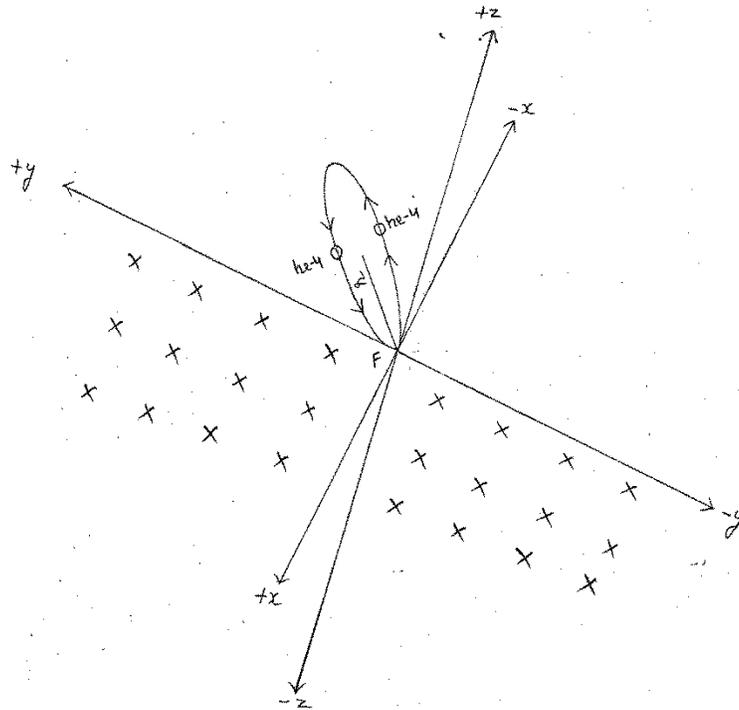
$$r = mv^2 / F_R$$

$$mv^2 = 27.2936 \times 10^{-13} \text{ J}$$

$$F_r = 7.2587 \times 10^{-13} \text{ N}$$

$$r = \frac{27.2936 \times 10^{-13} \text{ J}}{7.2587 \times 10^{-13} \text{ N}}$$

$$r = 3.7601 \text{ m}$$



The circular orbit to be followed by the left hand side propelled helion-4 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

C= center of the circle to be followed by the left hand side propelled helion-4.

The plane of the circular orbit to be followed by the left hand side propelled helium-4 makes angles with positive x, y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_x}{F_r} = \frac{F_x}{F_r}$$

$$F_x = -5.6222 \times 10^{-13} \text{ N}$$

$$F_r = 7.2587 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7745$$

$$\alpha = 219.24 \text{ degree } [\because \cos(219.24) = -0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_y}{F_r} = \frac{F_y}{F_r}$$

$$F_y = 3.2461 \times 10^{-13} \text{ N}$$

$$F_r = 7.2587 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4472$$

$$\beta = 63.43 \text{ degree } [\because \cos(63.43) = 0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_z}{F_r} = \frac{F_z}{F_r}$$

$$F_z = 3.2470 \times 10^{-13} \text{ N}$$

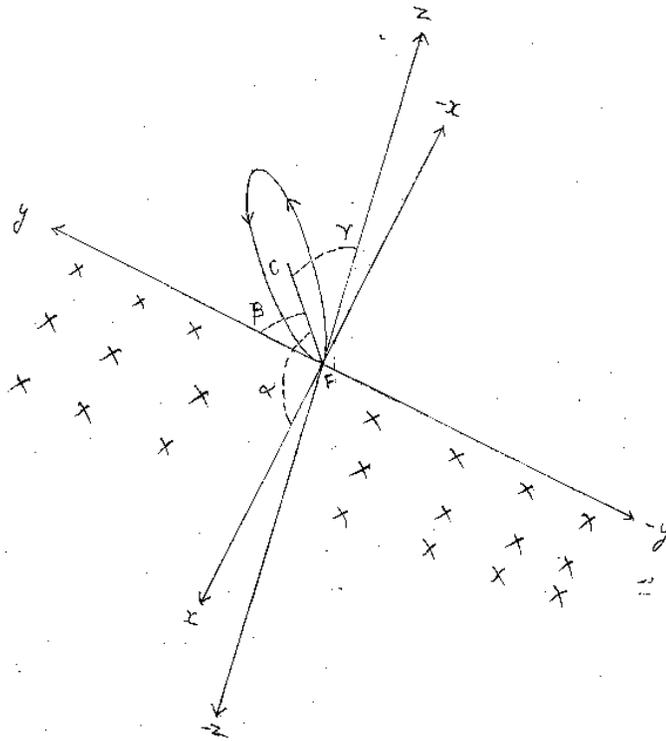
$$F_r = 7.2587 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4473$$

$$\gamma = 63.425 \text{ degree}$$

The plane of the circular orbit to be followed by the left hand side propelled helium -4 makes angles with positive x, y, and z axes as follows :-



Where, $\alpha = 219.24$ degree

$\beta = 63.43$ degree

$Y = 63.425$ degree

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the left hand side propelled hellion-4 .

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 3.7601 \text{ m}$$

$$= 7.5202 \text{ m}$$

$$\cos \alpha = -0.7745$$

$$x_2 - x_1 = d \cos \alpha$$

$$x_2 - x_1 = 7.5202 \times (-0.7745) \text{ m}$$

$$x_2 - x_1 = -5.8243 \text{ m}$$

$$x_2 = -5.8243 \text{ m} [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$d$$

$$\cos \beta = 0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 7.5202 \times 0.4472 \text{ m}$$

$$y_2 - y_1 = 3.3630 \text{ m}$$

$$y_2 = 3.3630 \text{ m} [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$d$$

$$\cos \gamma = 0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 7.5202 \times 0.4473 \text{ m}$$

$$z_2 - z_1 = 3.3637 \text{ m}$$

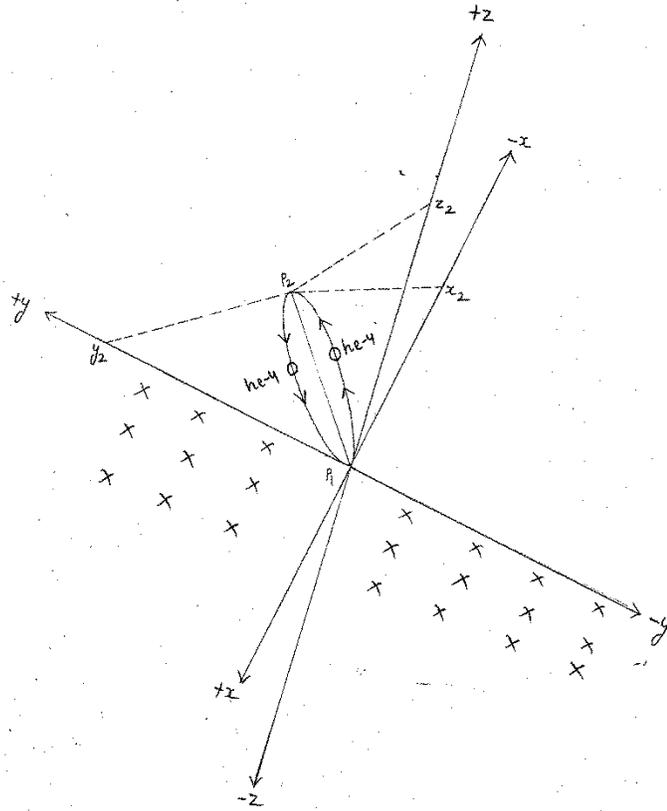
$$z_2 = 3.3637 \text{ m} [\because z_1 = 0]$$

The cartesian coordinates of the points $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$

The cartesian coordinates of the points $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be followed by the left hand side propelled helion -4 are as shown above.

The line ___ is the diameter of the circle .

P1P2



Conclusion :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the left hand side propelled helium-4 nucleus are along **-x, +y and +z** axes respectively .

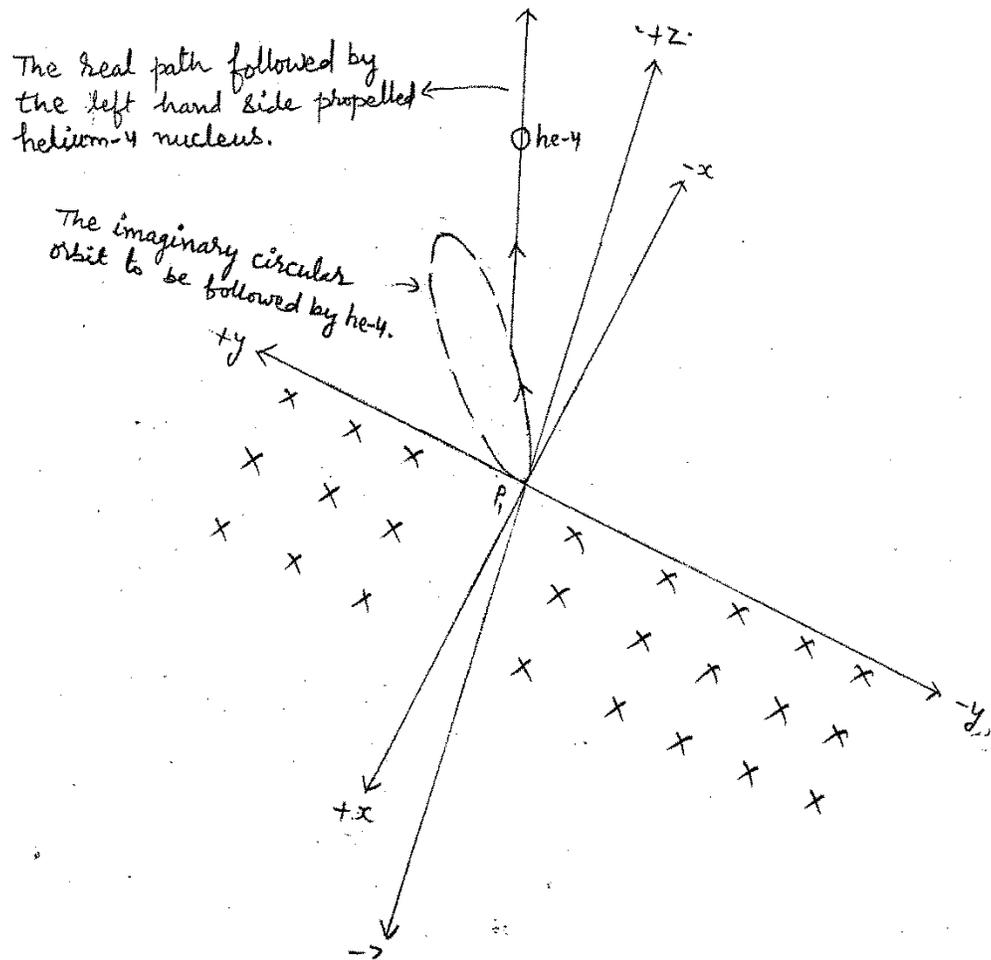
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the left hand side propelled helium-4 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the left hand side propelled helium-4 nucleus to undergo to a circular orbit of radius 3.7601m

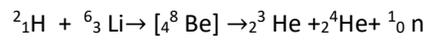
It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-5.8243 \text{ m}, 3.3630 \text{ m}, 3.3637 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the left hand side propelled helium-4 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

So the left hand side propelled helium-4 nucleus is not confined



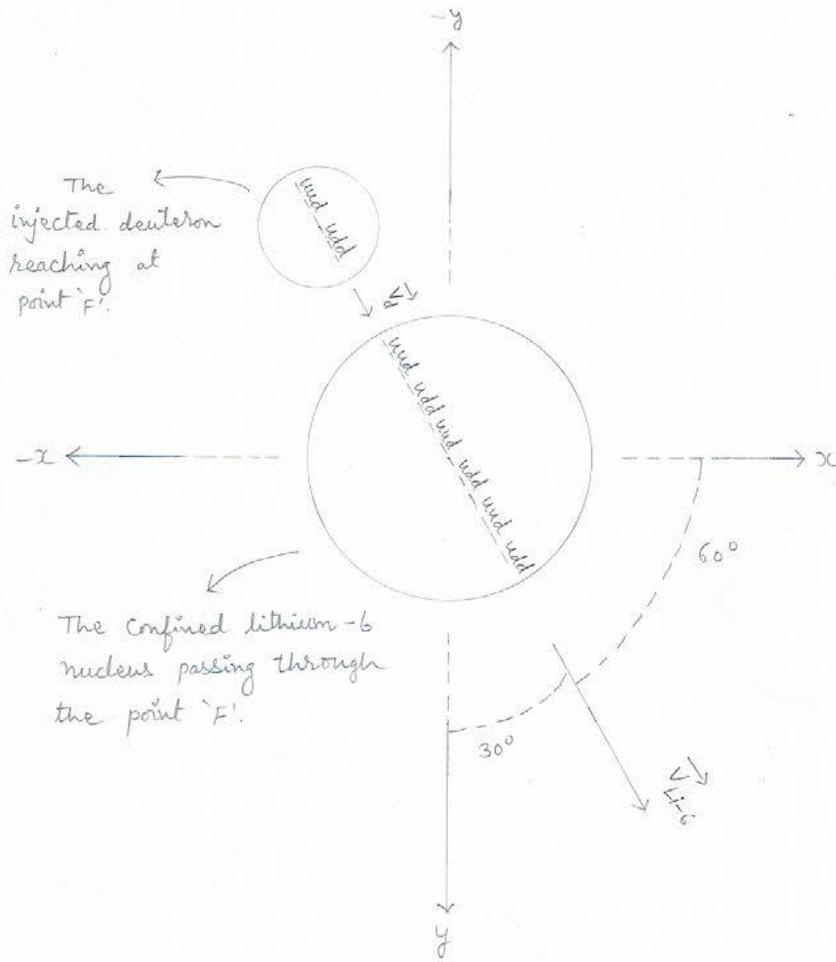
For fusion reaction

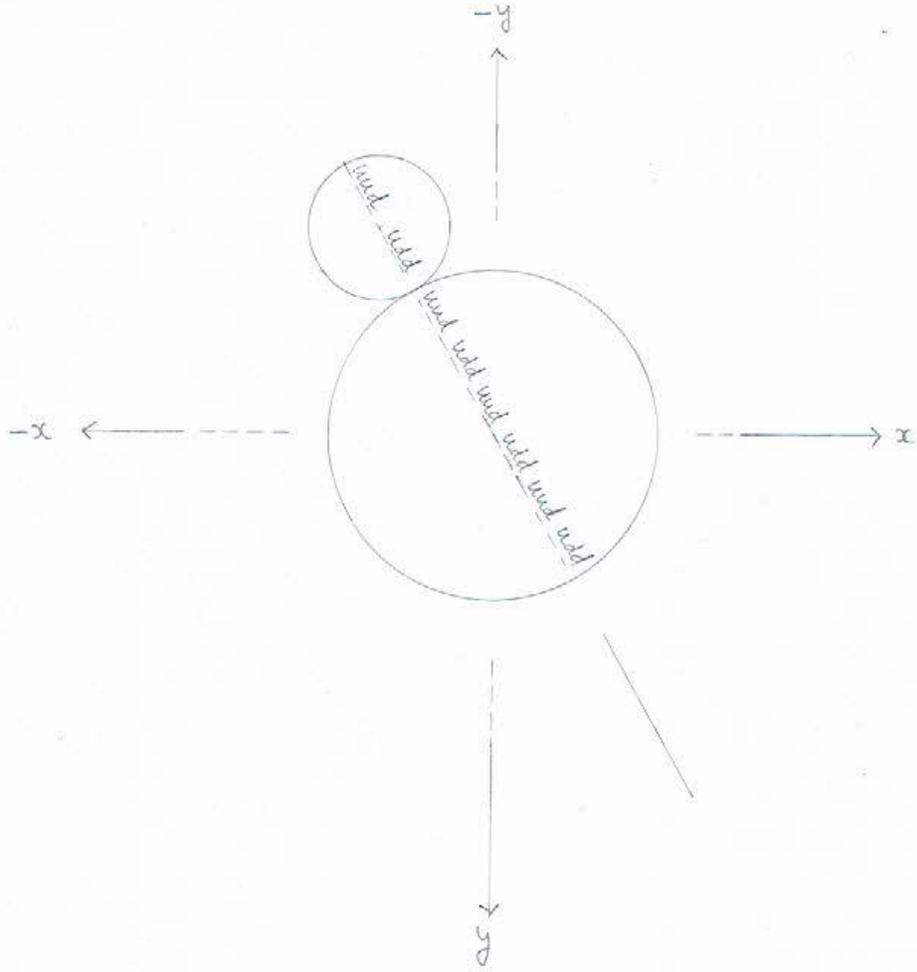


The interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined lithion-6] with the confined lithion-6 passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined lithion-6.

Interaction of nuclei (1)

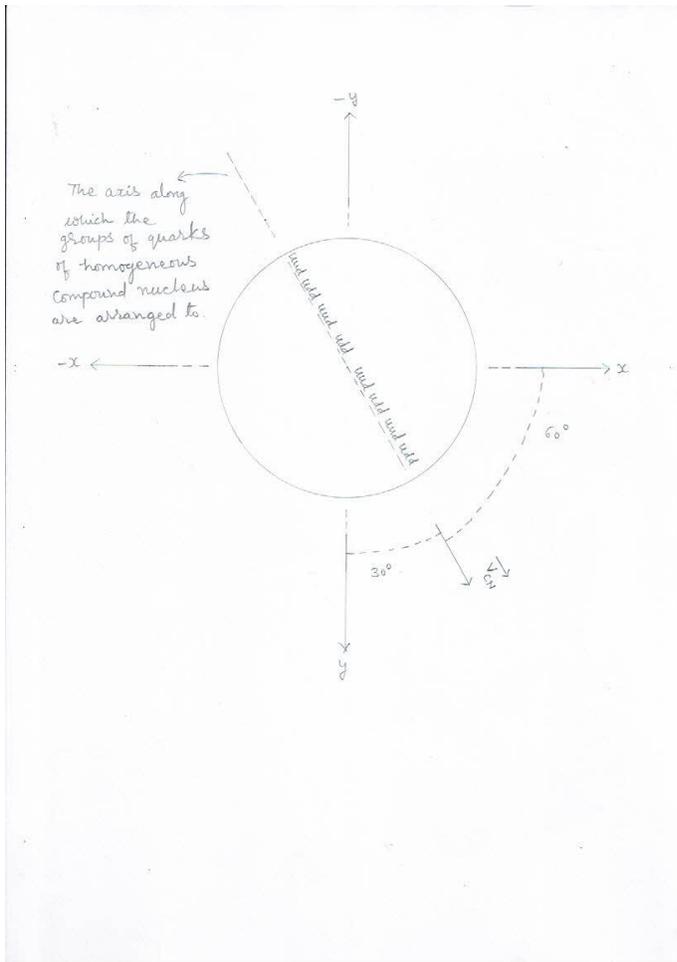




2. Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (deuteron and the lithium-6 nucleus) behave like a liquid and form a homogeneous compound nucleus . having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 8 groups of quarks surrounded by the gluons.



where,

$$\alpha = 60 \text{ degrees}$$

$$\beta = 30 \text{ degrees}$$

3. Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the beryllium - 7) than the reactant one (the lithium-6) includes the other seven (nearby located) groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

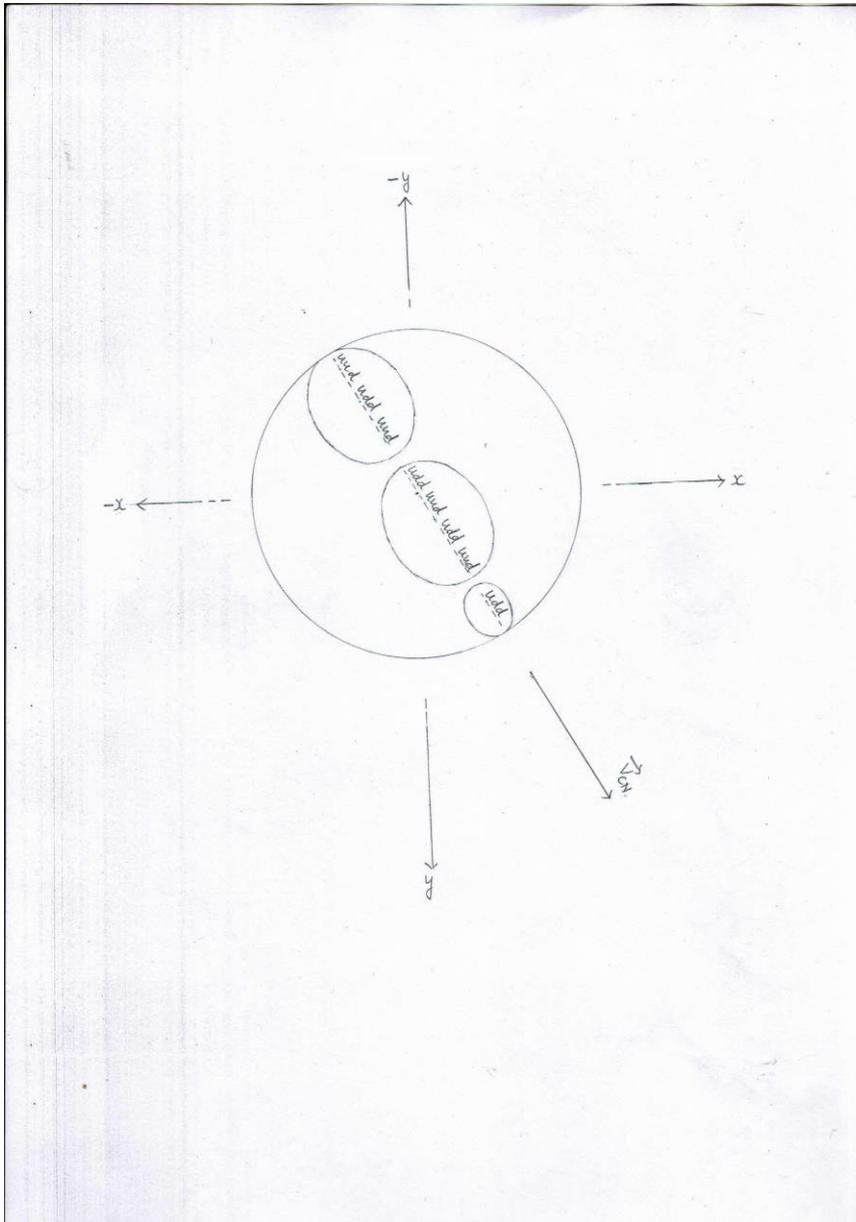
While , the remaining groups of quarks to become a stable nucleus (the neutron) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe ' A '] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two dissimilar lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the beryllium – 7 nucleus and the smaller nucleus is the neutron.

The greater nucleus is the lobe 'A ' and the smaller nucleus is the lobe 'B' while the remainigh space represent the remaining gluons .



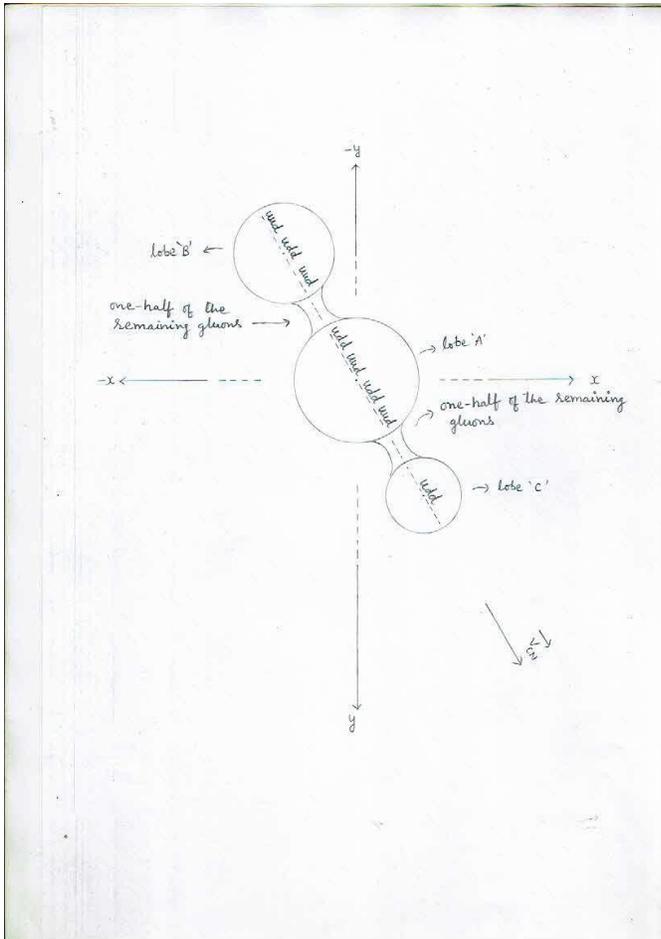
Formaton of lobes

4..Final stage of the heterogeneous compound nucleus : -

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

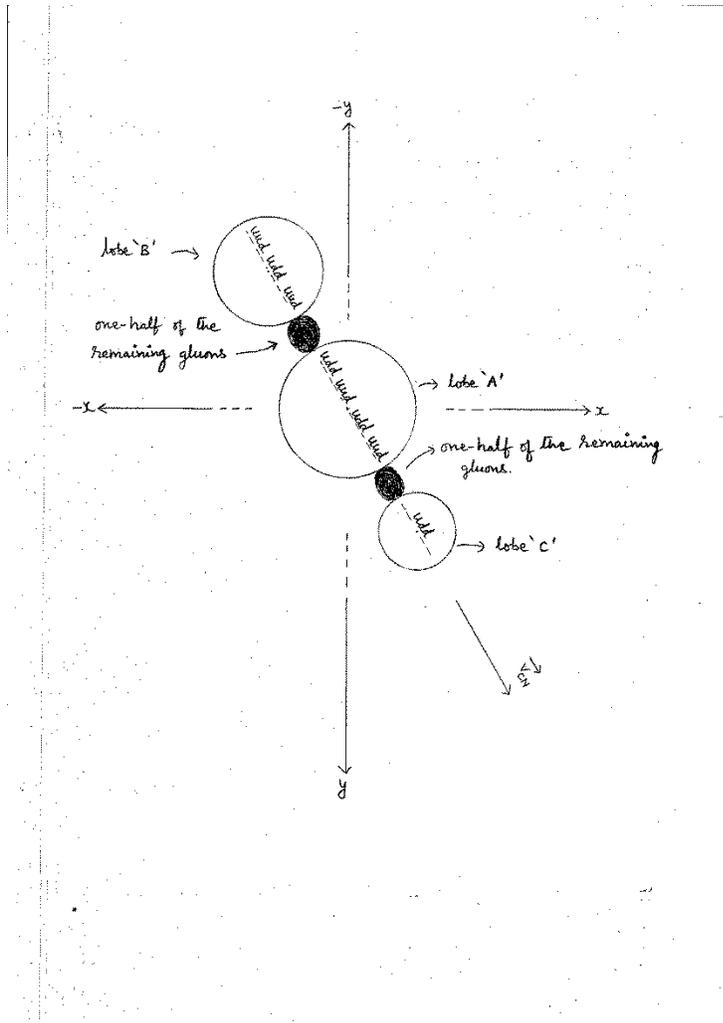
So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogenous compound nucleus

For $\alpha = 60$ degree

$\beta = 30$ degree



Final stage of the heterogenous compound nucleus

where, $\alpha = 60$ degree

$\beta = 30$ degree

Formation of compound nucleus :

As the deuteron of n^{th} bunch reaches at point F , it fuses with the confined lithium-6 to form a compound nucleus .

1. Just before fusion, to overcome the electrostatic repulsive force exerted by the lithium-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves its energy equal to 45.5598 keV.

so, just before fusion,

the kinetic energy of n^{th} deuteron is –

$$E_b = 153.6 \left[\text{keV} - 45.5598 \text{ keV} \right]$$

$$= 108.0402 \text{ keV}$$

$$= 0.1080402 \text{ MeV}$$

2. Just before fusion, to overcome the electrostatic repulsive force exerted by the deuteron, the lithium-6 loses (radiates its energy in the form of electromagnetic waves its energy equal to 136.0700 keV.

so, just before fusion,

the kinetic energy of lithium-6 is –

$$E_b = 388.2043 \text{ keV} - 136.0700 \text{ keV}$$

$$= 252.1343 \text{ keV}$$

$$= 0.2521343 \text{ MeV}$$

Kinetic energy of the compound nucleus :-

$$\text{K.E.} = [E_b \text{ of deuteron}] + [E_b \text{ of lithium-6}]$$

$$= [108.0402 \text{ KeV}] + [252.1343 \text{ KeV}]$$

$$= 360.1745 \text{ KeV.}$$

$$= 0.3601745 \text{ MeV}$$

Mass of the compound nucleus

$$M = m_d + m_{\text{Li-6}}$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}]$$

$$= 13.3287 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3601745 \text{ MeV}$$

$$V_{\text{CN}} = \left(\frac{[2 \times 0.3601745 \times 1.6 \times 10^{-13}]}{13.3287 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}} \quad \text{m/s}$$

$$V_{CN} = \left(\frac{1.1525584 \times 10^{-13} \text{ m/s}}{13.3287 \times 10^{-27}} \right)^{1/2}$$

$$V_{CN} = [0.08647192899 \times 10^{14}]^{1/2} \text{ m/s}$$

$$V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$\begin{aligned} \vec{V}_x &= V_{CN} \cos \alpha \\ &= 0.2940 \times 10^7 \times 0.5 \quad \text{m/s} \\ &= 0.1470 \times 10^7 \quad \text{m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_y &= V_{CN} \cos \beta \\ &= 0.2940 \times 10^7 \times 0.866 \quad \text{m/s} \\ &= \mathbf{0.2546} \text{ m/s} \end{aligned}$$

$$\begin{aligned} \vec{V}_z &= V_{CN} \cos \gamma \\ &= 0.2940 \times 10^7 \times 0 \quad \text{m/s} \\ &= 0 \quad \text{m/s} \end{aligned}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus, due to its instability, splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{CN}) into the three particles – **helium -3**, the **helium -4** and the neutron (Δm).

Out of them , the two particles (the **helium –3** , the **helium –4** and the neutron) are stable while the reduced mass is unstable .

According to the law of inertia ,each particle that is produced due to splitting of the compound nucleus , has an inherited velocity(\vec{v}_{inh}) equal to the velocity of the compound nucleus(\vec{V}_{cn}) .

So, for conservation of momentum

$$M\vec{V}_{cn} = (m_{\text{He-3}} + \Delta m/2 + m_{\text{He-4}} + \Delta m/2 + m_n) \vec{V}_{cn}$$

Where,

M = mass of the compound nucleus

\vec{V}_{cn} = velocity of the compound nucleus

$m_{\text{He-3}}$ = mass of the **helium-3** nucleus

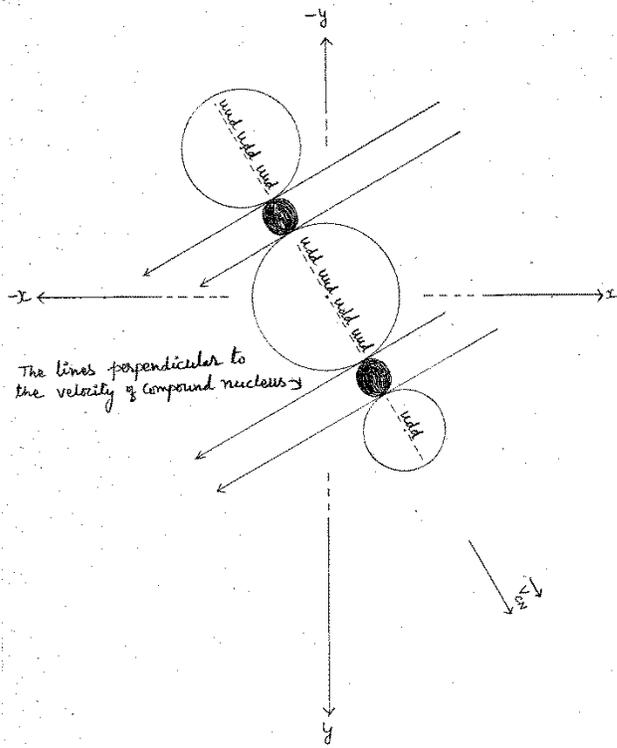
$m_{\text{He-4}}$ = mass of the **helium-4** nucleus

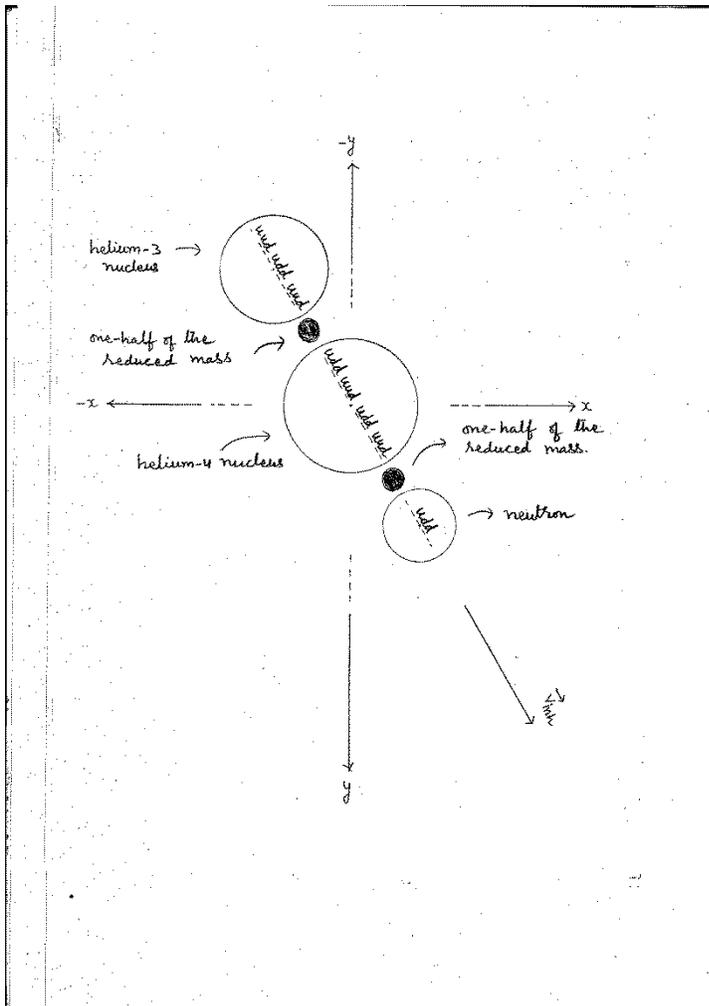
$\Delta m/2$ = one half of the reduced mass

m_n = mass of the neutron

The splitting of the heterogenous compound nucleus

The heterogenous compound nucleus to show the lines perpendicular to the \vec{V}_{cn}





Inherited velocity of the particles (s) :-

Each particle has inherited velocity $(\frac{\rightarrow}{v_{inh}})$ equal to the velocity of the compound nucleus $(\frac{\rightarrow}{v_{cn}})$.

(I). Inherited velocity of the particle ${}^2_3\text{He}$

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle ${}^2_3\text{He}$

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(II) . Inherited velocity of the particle ${}^2_4\text{He}$

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle ${}^2_4\text{He}$

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(III) . Inherited velocity of the neutron

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the neutron

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1470 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2546 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

iii Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2940 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{\text{Li-6}}] - [m_{\text{He-3}} + m_{\text{He-4}} + m_n]$$

$$\Delta m = [2.01355 + 6.01347708] - [3.014932 + 4.0015 + 1.00866] \text{ amu}$$

$$\Delta m = [8.02702708] - [8.025092] \text{ amu}$$

$$\Delta m = 0.00193508 \text{ amu}$$

$$\Delta m = 0.00193508 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm).

$$E_{\text{inh}} = \frac{1}{2} \Delta m V_{\text{CN}}^2$$

$$\Delta m = 0.00193508 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{\text{CN}}^2 = 0.08647192899 \times 10^{14}$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.00193508 \times 1.6605 \times 10^{-27} \times 0.08647192899 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00013892581 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.000086 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.00193508 \times 931 \text{ Mev}$$

$$E_R = 1.801559 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{inh} + E_R$$

$$E_T = [0.000086 + 1.801559] \text{ Mev}$$

$$E_T = 1.801645 \text{ Mev}$$

(I) Increased in the energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses. so, the increased energy (E_{inc}) of the particles are :-

1.. For helium - 3

$$E_{inc} = \frac{m_{He-4}}{m_{He-3} + m_{He-4}} \times E_T/2$$

$$E_{inc} = \frac{4.0015 \text{ amu}}{[3.014932 + 4.0015] \text{ amu}} \times 1.801645 / 2 \text{ Mev}$$

$$E_{inc} = 4.0015 \times 0.900822 \text{ Mev}$$

7.016432

$$E_{inc} = 0.57030410898 \times 0.900822 \text{ Mev}$$

$$E_{inc} = 0.513742 \text{ Mev}$$

2.increased energy of the helium-4

$$E_{inc} = [E_T/2] - [\text{increased energy of the He-3}]$$

$$E_{inc} = [0.900822] - [0.513742] \text{ Mev}$$

$$E_{inc} = 0.38708 \text{ Mev}$$

(II) Increased in the energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses . so,the increased energy (E_{inc}) of the particles are :-

1.. For **helium - 4**

$$E_{inc} = \frac{m_n}{m_n + m_{He-4}} \times E_T/2$$

$$E_{inc} = \frac{1.00866 \text{ amu}}{[1.00866 + 4.0015] \text{ amu}} \times 1.801645 / 2 \text{ Mev}$$

$$E_{inc} = \frac{1.00866}{5.01016} \times 0.900822 \text{ Mev}$$

$$E_{inc} = 0.20132291184 \times 0.900822 \text{ Mev}$$

$$E_{inc} = 0.181356 \text{ Mev}$$

2..increased energy of the neutron

$$E_{inc} = [E_T/2] - [\text{increased energy of the He-4}]$$

$$E_{inc} = [0.900822] - [0.181356] \text{ Mev}$$

$$E_{inc} = 0.719466 \text{ Mev}$$

6..Increased velocity of the particles .

(1) For **neutron**

$$E_{inc} = \frac{1}{2} m_n v_{inc}^2$$

$$\begin{aligned}
 V_{inc} &= [2 \times E_{inc}/m_n]^{1/2} \\
 &= \left(\frac{2 \times 0.719466 \times 1.6 \times 10^{-13} \text{ J}}{1.6749 \times 10^{-27} \text{ kg}} \right)^{1/2} \text{ m/s} \\
 &= \left(\frac{2.3022912 \times 10^{-13}}{1.6749 \times 10^{-27}} \right)^{1/2} \text{ m/s} \\
 &= [1.37458427368 \times 10^{14}]^{1/2} \text{ m/s} \\
 &= 1.1724 \times 10^7 \text{ m/s}
 \end{aligned}$$

For helium-3

$$\begin{aligned}
 V_{inc} &= [2 \times E_{inc} / m_{\text{He-3}}]^{1/2} \\
 &= \left(\frac{2 \times 0.513742 \times 1.6 \times 10^{-13} \text{ J}}{5.00629 \times 10^{-27} \text{ kg}} \right)^{1/2} \text{ m/s} \\
 &= \left(\frac{1.6439744 \times 10^{-13}}{5.00629 \times 10^{-27}} \right)^{1/2} \text{ m/s} \\
 &= [0.32838177572 \times 10^{14}]^{1/2} \text{ m/s} \\
 &= 0.5730 \times 10^7 \text{ m/s}
 \end{aligned}$$

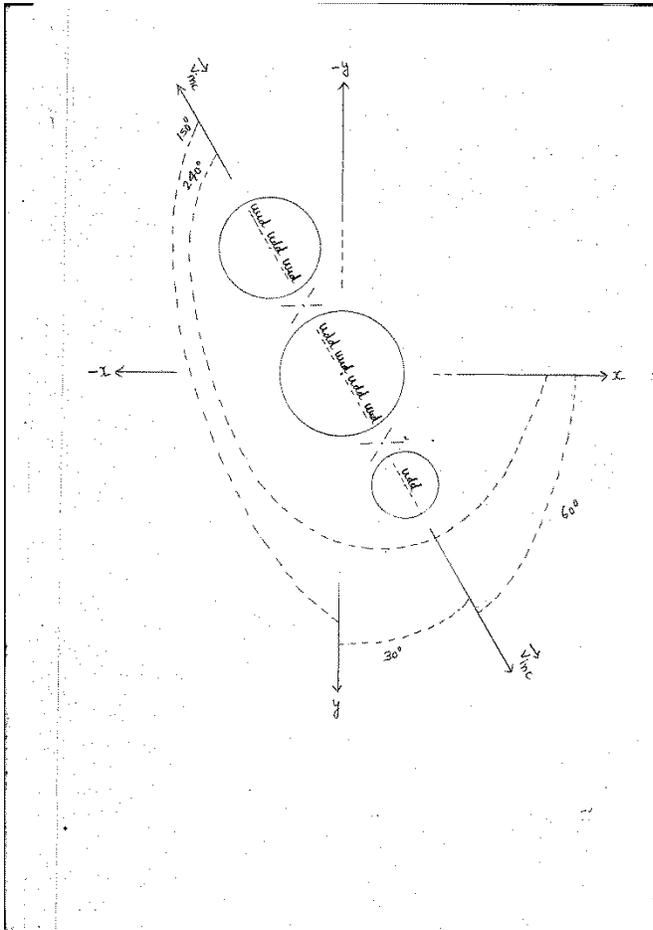
7 Angle of propulsion

- 1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum.

2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus(\vec{V}_{CN}) .]

- 3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .
 so, the neutron is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .
 While the helium -3 nucleus is propelled making 240° angle with x-axis , 150° angle with y-axis and 90° angle with z-axis .

Propulsion of thte particles



Components of the increased velocity (V_{inc}) of the particles.

(i) For helium-3

$$\vec{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 0.5730 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(240) = -0.5$$

$$\vec{1}_{V_x} = 0.5730 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.2865 \times 10^7 \text{ m/s}$$

$$\vec{2}_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(150) = -0.866$$

$$\vec{2}_{V_y} = 0.5730 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.4962 \times 10^7 \text{ m/s}$$

$$\vec{3}_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\vec{3}_{V_z} = 0.5730 \times 10^7 \times 0$$

$$= 0 \text{ m/s}$$

For neutron

$$\vec{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 1.1724 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\vec{1}_{V_x} = 1.1724 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 0.5862 \times 10^7 \text{ m/s}$$

$$\vec{2}_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(30) = 0.866$$

$$\vec{2}_{V_y} = 1.1724 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 1.0152 \times 10^7 \text{ m/s}$$

$$\vec{3}_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos(90) = 0$$

$$\vec{3}_{V_z} = 1.1724 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

Components of the increased momentum of helium-3

$$\vec{1}_{P_x} = m_{\text{He-3}} \vec{1}_{V_x}$$

$$= 5.00629 \times 10^{-27} \times (-0.2865 \times 10^7) \text{ kgm/s}$$

$$= -1.4343 \times 10^{-20} \text{ kgm/s}$$

$$\vec{2}_{P_y} = m_{\text{He-3}} \vec{2}_{V_y}$$

$$= 5.00629 \times 10^{-27} \times (-0.4962 \times 10^7) \text{ kgm/s}$$

$$= - 2.4841 \times 10^{-20} \text{kgm/s}$$

So the Components of the increased momentum of helium-4

$$\vec{p}_x = -(-1.4343 \times 10^{-20})$$

$$= 1.4343 \times 10^{-20}$$

$$\vec{p}_y = -(- 2.4841 \times 10^{-20})$$

$$= 2.4841 \times 10^{-20}$$

Components of the increased momentum of neutron

$$\vec{p}_x = m_n \times \vec{v}_x$$

$$= 1.6749 \times 10^{-27} \times 0.5862 \times 10^7 \text{ kgm/s}$$

$$= 0.9818 \times 10^{-20} \text{kgm/s}$$

$$\vec{p}_y = m_{\text{He-3}} \times \vec{v}_y$$

$$= 1.6749 \times 10^{-27} \times 1.0152 \times 10^7 \text{ kgm/s}$$

$$= 1.7003 \times 10^{-20} \text{ kgm/s}$$

So the Components of the increased momentum of helium-4

$$\vec{P}_x = -(0.9818 \times 10^{-20})$$

$$= -0.9818 \times 10^{-20}$$

$$\vec{P}_y = -(1.7003 \times 10^{-20})$$

$$= -1.7003 \times 10^{-20}$$

9.. Components of the final velocity (\vec{V}_f) of the particles

I For helium-3

According to -	Inherited Velocity (\vec{V}_{inh})	Increased Velocity (\vec{V}_{inc})	Final velocity (\vec{V}_f) $= (\vec{V}_{inh} + \vec{V}_{inc})$
X – axis	$\vec{V}_x = 0.1470 \times 10^7 \text{ m/s}$	$\vec{V}_x = -0.2865 \times 10^7 \text{ m/s}$	$\vec{V}_x = -0.1395 \times 10^7 \text{ m/s}$
y – axis	$\vec{V}_y = 0.2546 \times 10^7 \text{ m/s}$	$\vec{V}_y = -0.4962 \times 10^7 \text{ m/s}$	$\vec{V}_y = -0.2416 \times 10^7 \text{ m/s}$

z -axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$
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2..For neutron

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) = (\vec{v}_{inh}) + (\vec{v}_{inc})
X -axis	$\vec{v}_x = 0.1470 \times 10^7 \text{ m/s}$	$\vec{v}_x = 0.5862 \times 10^7 \text{ m/s}$	$\vec{v}_x = 0.7332 \times 10^7 \text{ m/s}$
y- axis	$\vec{v}_y = 0.2546 \times 10^7 \text{ m/s}$	$\vec{v}_y = 1.0152 \times 10^7 \text{ m/s}$	$\vec{v}_y = 1.2698 \times 10^7 \text{ m/s}$
z -axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final velocity (v_f) of thehelium-3

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.1395 \times 10^7 \text{ m/s}$$

$$V_y = 0.2416 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.1395 \times 10^7)^2 + (0.2416 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.01946025 \times 10^{14}) + (0.05837056 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.07783081 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.2789 \times 10^7 \text{ m/s}$$

Final kineticenergy ofthe helium-3

$$E = \frac{1}{2} m_{\text{He-3}} V_f^2$$

$$E = \frac{1}{2} \times 5.00629 \times 10^{-27} \times 0.07783081 \times 10^{14} \text{ J}$$

$$= 0.19482180289 \times 10^{-13} \text{ J}$$

$$= 0.121763 \text{ Mev}$$

$$m_{\text{He-3}} V_f^2 = 5.00629 \times 10^{-27} \times 0.07783081 \times 10^{14} \text{ J}$$

$$= 0.3896 \times 10^{-13} \text{ J}$$

10..Final velocity (v_f) of the neutron

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.7332 \times 10^7 \text{ m/s}$$

$$V_y = 1.2698 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.7332 \times 10^7)^2 + (1.2698 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.53758224 \times 10^{14}) + (1.61239204 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 2.14997428 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 1.4662 \times 10^7 \text{ m/s}$$

Final kinetic energy of the neutron

$$E = \frac{1}{2} m_n V_f^2$$

$$E = \frac{1}{2} \times 1.6749 \times 10^{-27} \times 2.14997428 \times 10^{14} \text{ J}$$

$$= 1.80049596078 \times 10^{-13} \text{ J}$$

$$= 1.125309 \text{ Mev}$$

Angles made by the final velocity of neutron

$$\cos \alpha = \frac{V_x}{V_f}$$

$$\frac{V_x}{V_f} = 0.7332 \times 10^7 \quad \text{m/s}$$

$$V_f = 1.4662 \times 10^7 \text{ m/s}$$

$$\cos \alpha = 0.7332 \times 10^7 / 1.4662 \times 10^7$$

$$\cos \alpha = 0.5000$$

$$\alpha = 60^\circ$$

$$\cos \beta = \frac{V_y}{V_f}$$

$$\frac{V_y}{V_f} = 1.2698 \times 10^7 \quad \text{m/s}$$

$$V_f = 1.4662 \times 10^7 \quad \text{m/s}$$

$$\cos \beta = 1.2698 \times 10^7 / 1.4662 \times 10^7$$

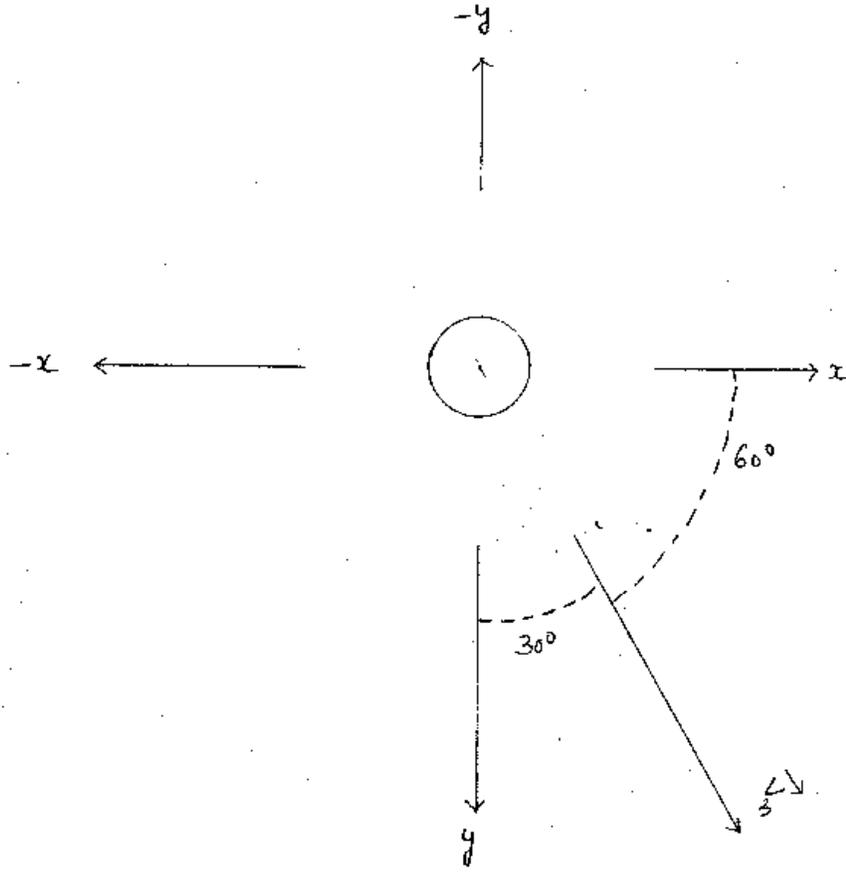
$$\cos \beta = 0.8660$$

$$\beta = 30^\circ$$

$$\cos \gamma = \frac{V_z}{V_f} = 0 / 1.4662 \times 10^7 = 0$$

$$\gamma = 90^\circ$$

The final velocity of neutron makes angles with positive x, y and z axes as follows :-



Forces acting on the helium-3 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.1395 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 2 \times 1.6 \times 10^{-19} \times 0.1395 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.4468 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

$$\text{so,}$$

$$\vec{F}_y = 0.4468 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 2 \times 1.6 \times 10^{-19} \times 0.1395 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.4469 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_z is according to (+) Z-axis,

$$\text{so,}$$

$$\vec{F}_z = 0.4469 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = -0.2416 \times 10^7 \quad \text{m/s}$$

$$\vec{B}_z = 1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

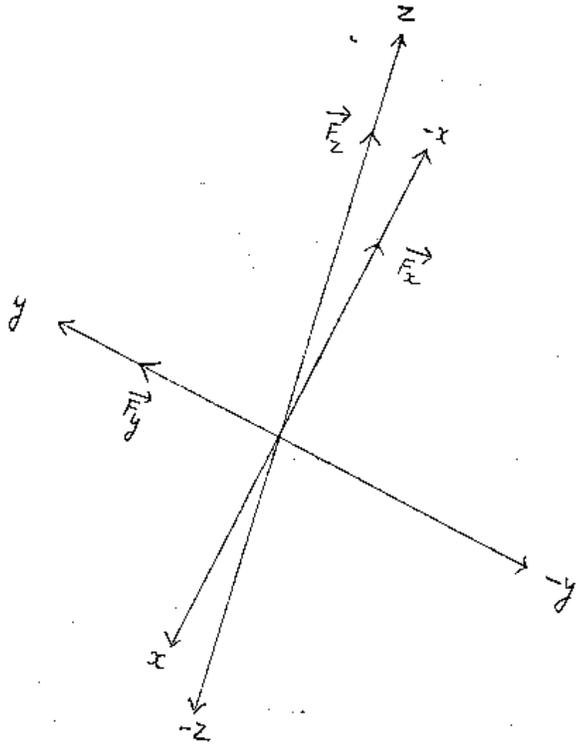
$$F_x = 2 \times 1.6 \times 10^{-19} \times 0.2416 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 0.7738 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x-axis,

$$\text{so, } \vec{F}_x = -0.7738 \times 10^{-13} \text{ N}$$

Forces acting on the helion-3



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 0.7738 \times 10^{-13} \text{ N}$$

$$F_y = 0.4468 \times 10^{-13} \text{ N}$$

$$F_z = 0.4469 \times 10^{-13}$$

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

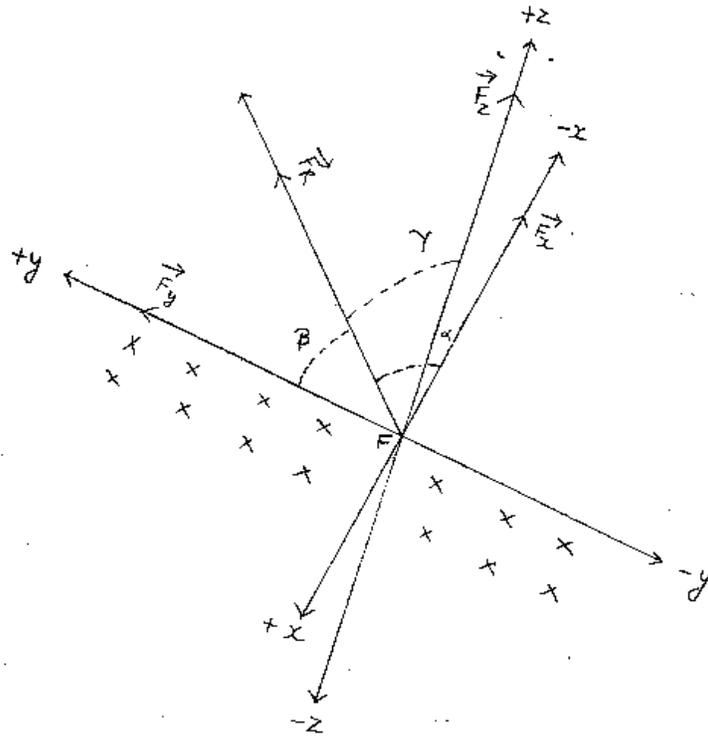
$$F_R^2 = (0.7738 \times 10^{-13})^2 + (0.4468 \times 10^{-13})^2 + (0.4469 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (0.59876644 \times 10^{-26}) + (0.19963024 \times 10^{-26}) + (0.19971961 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 0.99811629 \times 10^{-26} \text{ N}^2$$

$$F_R = 0.9990 \times 10^{-13} \text{ N}$$

Resultant force acting on the helium-3



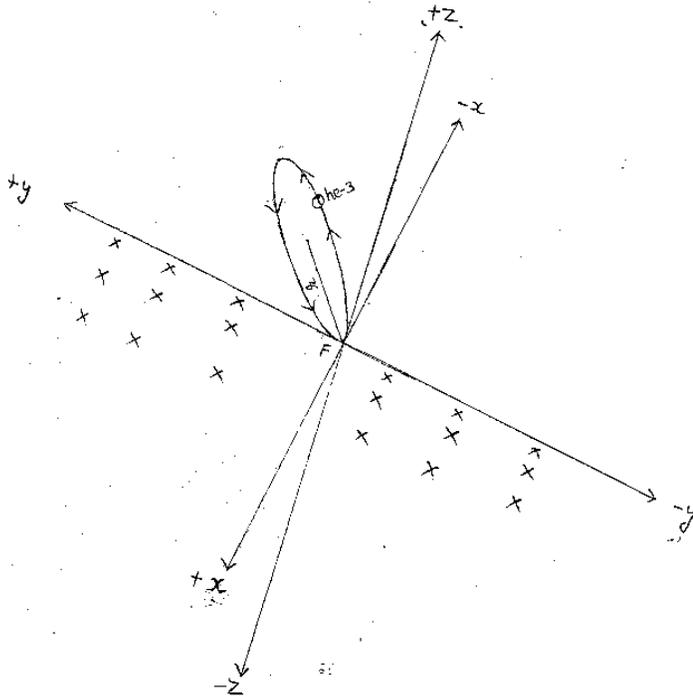
Radius of the circular orbit to be followed by the helium - 3 :

$$\begin{aligned}r &= mv^2 / F_R \\mv^2 &= 0.3896 \times 10^{-13} \text{ J} \\F_r &= 0.9990 \times 10^{-13} \text{ N} \\r &= 0.3896 \times 10^{-13} \text{ J} / 0.9990 \times 10^{-13} \text{ N}\end{aligned}$$

$$r = 0.3899 \text{ m}$$

The circular orbit to be followed by the helium-3 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

C = center of the circular orbit to be followed by the helium-3.



The plane of the circular orbit to be followed by helium -3 makes angles with positive x , y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = -0.7738 \times 10^{-13} \text{ N}$$

$$F_r = 0.9990 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7745$$

$$\alpha = 219.24 \text{ degree } [\because \cos(219.24) = -0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = 0.4468 \times 10^{-13} \text{ N}$$

$$F_r = 0.9990 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4472$$

$$\beta = 63.43 \text{ degree } [\because \cos(63.43) = 0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{\vec{F}_z}{F_r}$$

$$\vec{F}_z = 0.4469 \times 10^{-13} \text{ N}$$

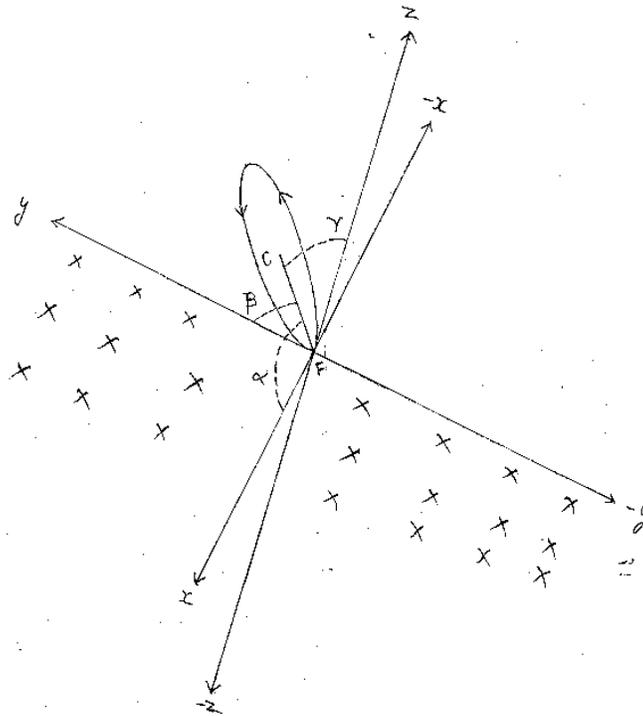
$$F_r = 0.9990 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4473$$

$$\gamma = 63.425 \text{ degree}$$

The plane of the circular orbit to be followed by the helium -3 nucleus makes angles with positive x , y , and z axes as follows :-



Where,

$$\alpha = 219.24 \text{ degree}$$

$$\beta = 63.43 \text{ degree}$$

$$\gamma = 63.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the helium - 3.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 0.3899 \text{ m}$$

$$= 0.7798 \text{ m}$$

$$\cos \alpha = -0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 0.7798 \times (-0.7745) \quad \text{m}$$

$$x_2 - x_1 = -0.6039 \text{ m}$$

$$x_2 = -0.6039 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = 0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 0.7798 \times 0.4472 \text{ m}$$

$$y_2 - y_1 = 0.3487 \text{ m}$$

$$y_2 = 0.3487 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = 0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 0.7798 \times 0.4473 \quad \text{m}$$

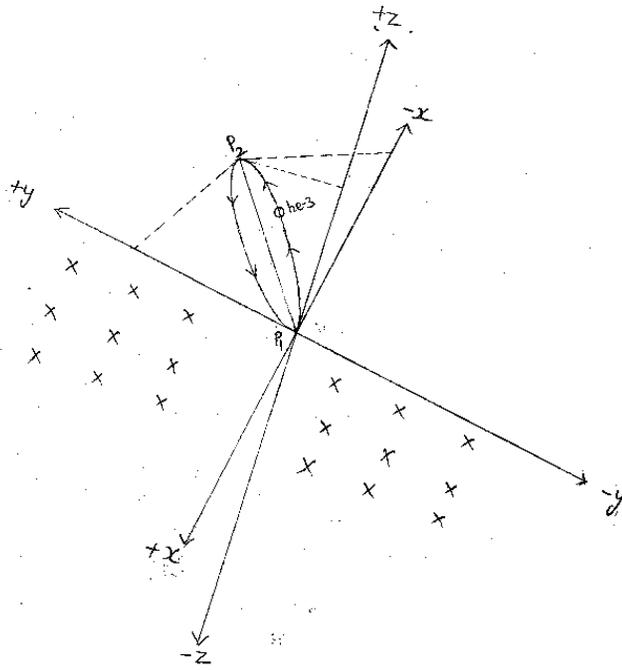
$$z_2 - z_1 = 0.3488 \text{ m}$$

$$z_2 = 0.3488 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the helium - 3 are as shown below.

The line___ is the diameter of the circle .

P_1P_2



Conclusion :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **-x , +y and +z** axes respectively .

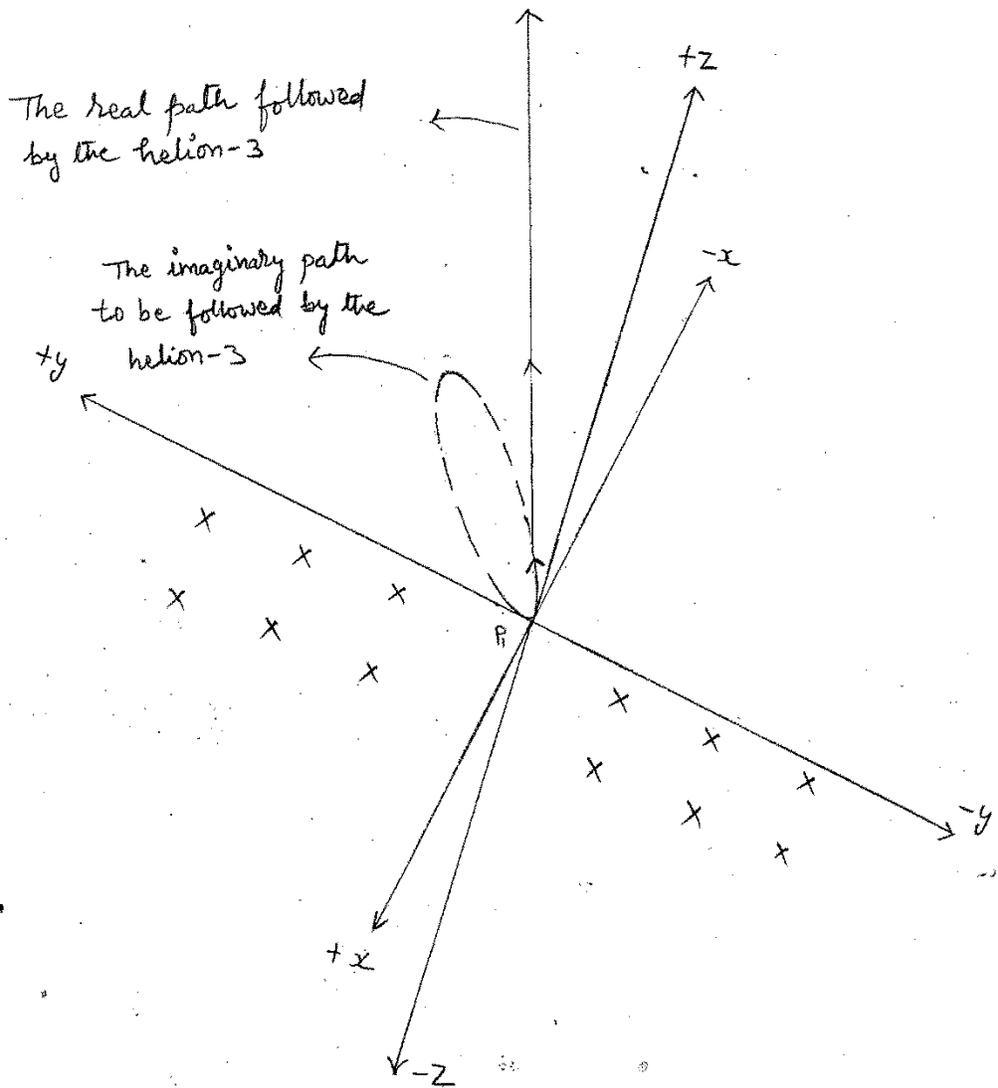
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 0.3899 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.6039 \text{ m}, 0.3487 \text{ m}, 0.3488 \text{ m})$ where the magnetic fields are not applied

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the helium-3 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

Hence the helium-3 nucleus is not confined.



9.. Components of the final momentum (P_f)of the particles

I For helium-4

According to -	Inherited momentum (\vec{P}_{Pinh}) of the helium-4 nucleus	Increased momentum (\vec{P}_{Pinc}) of the helium-4 nucleus when the one- half of the reduced mass freely located between hellion -4 and thehellion -3 converts into energy	Increased momentum (\vec{P}_{Pinc}) of the helium-4 nucleus when the one- half of the reduced mass freely located between hellion - 4 and the neutron converts into energy	Finalmomentum helium-4 nucleus $(\vec{P}_f) = (\vec{P}_{Pinh}) + (\vec{P}_{Pinc})$
X-axis	$\vec{P}_{Px} = 0.9767 \times 10^{-20} \text{ kg m/s}$	$\vec{P}_{Px} = 1.4343 \times 10^{-20} \text{ kg m/s}$	$\vec{P}_{Px} = -0.9818 \times 10^{-20} \text{ kg m/s}$	$\vec{P}_{Px} = 1.4292 \times 10^{-20} \text{ kg m/s}$
y-axis	$\vec{P}_{Py} = 1.6916 \times 10^{-20} \text{ kg m/s}$	$\vec{P}_{Py} = 2.4841 \times 10^{-20} \text{ kg m/s}$	$\vec{P}_{Py} = -1.7003 \times 10^{-20} \text{ kg m/s}$	$\vec{P}_{Py} = 2.4754 \times 10^{-20} \text{ kg m/s}$
z-axis	$\vec{P}_{Pz} = 0 \text{ kg m/s}$	$\vec{P}_{Pz} = 0 \text{ kg m/s}$	$\vec{P}_{Pz} = 0 \text{ kg m/s}$	$\vec{P}_{Pz} = 0 \text{ kg m/s}$

9..Components of the final velocity (V_f)of the particles

I For helium-4

$$1 \quad \vec{V}_x = \frac{\vec{P}_x}{m}$$

$$= 1.4292 \times 10^{-20} \text{ kg m/s}$$

$$6.64449 \times 10^{-27} \text{ kg m/s}$$

$$= 0.2150 \times 10^7 \text{ m/s}$$

$$\vec{v}_y = \frac{\vec{p}_y}{m}$$

$$= 2.4754 \times 10^{-20} \text{ kg m/s}$$

$$6.64449 \times 10^{-27} \text{ kg m/s}$$

$$= 0.3725 \times 10^7 \text{ m/s}$$

$$\vec{v}_z = \frac{\vec{p}_z}{m}$$

$$= 0 \text{ kg m/s} = 0$$

$$6.64449 \times 10^{-27} / \text{kg m/s}$$

10. Final velocity (v_f) of the helion - 4

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.2150 \times 10^7 \text{ m/s}$$

$$V_y = 0.3725 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.2150 \times 10^7)^2 + (0.3725 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.046225 \times 10^{14}) + (0.13875625 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.18498125 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.4300 \times 10^7 \text{ m/s}$$

Final kinetic energy of the helion - 4

$$E = \frac{1}{2} m_{\text{He-4}} V_f^2$$

$$E = \frac{1}{2} \times 6.64449 \times 10^{-27} \times 0.18498125 \times 10^{14} \text{ J}$$

$$= 0.6145530329 \times 10^{-13} \text{ J}$$

$$= 0.384095 \text{ Mev}$$

$$m_{\text{He-4}} V_f^2 = 6.64449 \times 10^{-27} \times 0.18498125 \times 10^{14} \text{ J}$$

$$= 1.2291 \times 10^{-13} \text{ J}$$

Forces acting on the helium - 4 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = 0.2150 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 2 \times 1.6 \times 10^{-19} \times 0.2150 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.6886 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_y is according to (-) y-axis ,

so ,

$$\vec{F}_y = -0.6886 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 2 \times 1.6 \times 10^{-19} \times 0.2150 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 0.6888 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_z is according to (-) Z- axis ,

so ,

$$\vec{F}_z = -0.6888 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = 0.3725 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = 1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

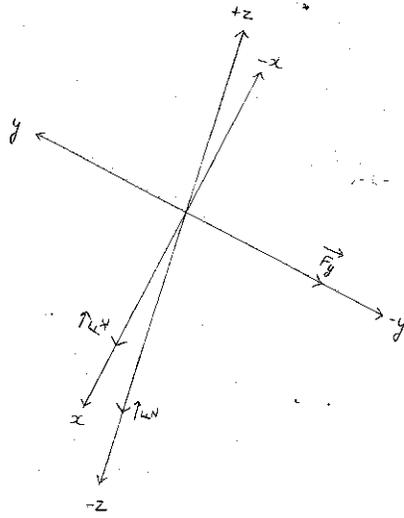
$$F_x = 2 \times 1.6 \times 10^{-19} \times 0.3725 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 1.1931 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x axis,

$$\text{so, } \vec{F}_x = 1.1931 \times 10^{-13} \text{ N}$$

Forces acting on helium -4 nucleus :-



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 1.1931 \times 10^{-13} \text{ N}$$

$$F_y = 0.6886 \times 10^{-13} \text{ N}$$

$$F_z = 0.6888 \times 10^{-13}$$

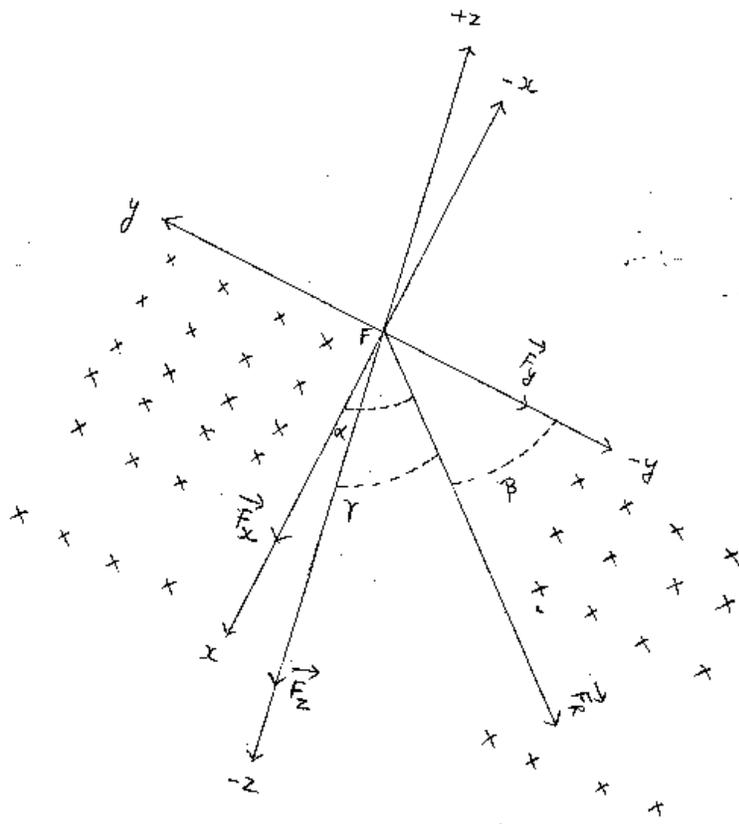
$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_R^2 = (1.1931 \times 10^{-13})^2 + (0.6886 \times 10^{-13})^2 + (0.6888 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (1.42348761 \times 10^{-26}) + (0.47416996 \times 10^{-26}) + (0.47444544 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 2.37210301 \times 10^{-26} \text{ N}^2$$

$$F_R = 1.5401 \times 10^{-13} \text{ N}$$



Radius of the circular orbit followed by the helium - 4 :

$$r = mv^2 / F_R$$

$$mv^2 = 1.2291 \times 10^{-13} \text{ J}$$

$$F_r = 1.5401 \times 10^{-13} \text{ N}$$

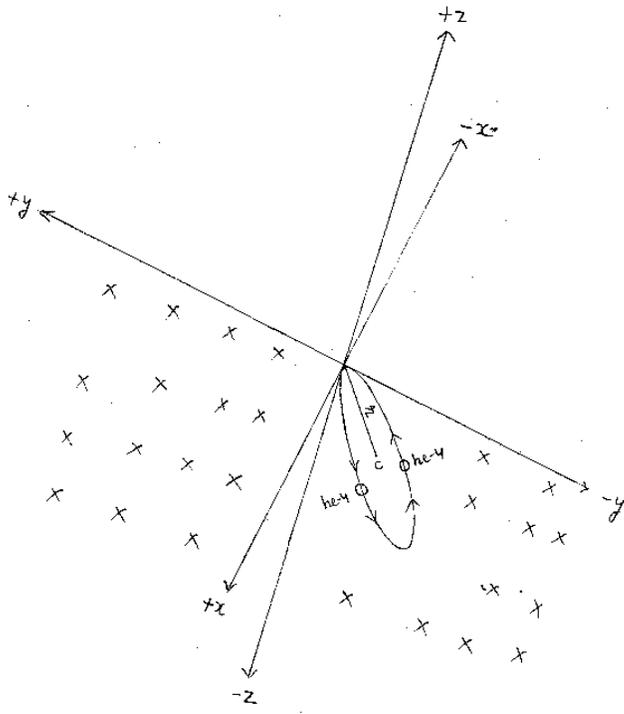
$$1.2291 \times 10^{-13} \text{ J}$$

$$r = \frac{1.2291 \times 10^{-13} \text{ J}}{1.5401 \times 10^{-13} \text{ N}}$$

$$r = 0.7980 \text{ m}$$

The circular orbit followed by helion -4 the lies in the plane made up of positivex-axis, negative y-axis and the negative z-axis.

C= center of the circular orbit followed by thehelion -4



The plane of the circular orbit followed by the helium -4 nucleus makes angles with positive x, y and z-axes as follows :-

1 with x- axis

$$\cos \alpha = \frac{F_{R \cos \alpha}}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = 1.1931 \times 10^{-13} \text{ N}$$

$$F_r = 1.5401 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7746$$

$$\alpha = 39.23 \text{ degree } [\because \cos (39.23) = 0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_{R \cos \beta}}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = -0.6886 \times 10^{-13} \text{ N}$$

$$F_r = 1.5401 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4471$$

$$\beta = 243.44 \text{ degree } [\because \cos (243.44) = -0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_{R \cos \gamma}}{F_r} = \frac{\vec{F}_z}{F_r}$$

$$\vec{F}_z = \underline{-0.6888 \times 10^{-13} \text{ N}}$$

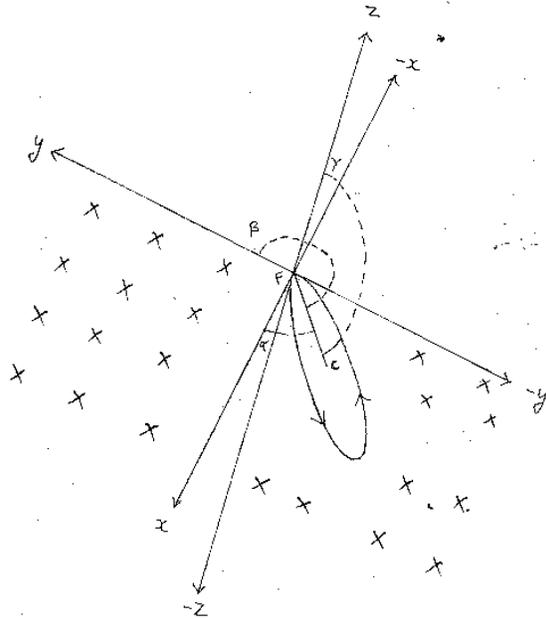
$$F_r = 1.5401 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4472$$

$$\gamma = 243.43 \text{ degree}$$

The plane of the circular orbit followed by the helium -4 nucleus makes angles with positive x , y , and z axes as follows :-



Where,

$$\alpha = 39.23 \text{ degree}$$

$$\beta = 243.44 \text{ degree}$$

$$\gamma = 243.43 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the helium - 4.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$= 2 \times 0.7980 \text{ m}$$

$$= 1.596 \text{ m}$$

$$d = 2 \times r$$

$$\cos \alpha = -0.7746$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 1.596 \times 0.7746 \text{ m}$$

$$x_2 - x_1 = 1.2362 \text{ m}$$

$$x_2 = 1.2362 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

d

$$\cos \beta = -0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 1.596 \times (-0.4471) \text{ m}$$

$$y_2 - y_1 = -0.7135 \text{ m}$$

$$y_2 = -0.7135 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

d

$$\cos \gamma = -0.4472$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 1.596 \times (-0.4472) \text{ m}$$

$$z_2 - z_1 = 0.7137 \text{ m}$$

$$z_2 = 0.7137 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the helium - 4 are as shown below.

The line ___ is the diameter of the circle .

P_1P_2

Conclusion:-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-4 nucleus are along **+x, -y and -z** axes respectively .

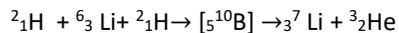
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-4 nucleus lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the helium-4 nucleus to undergo to a circular orbit of radius of 0.7980 m.

It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.2362 \text{ m}, -0.7135 \text{ m}, -0.7137 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

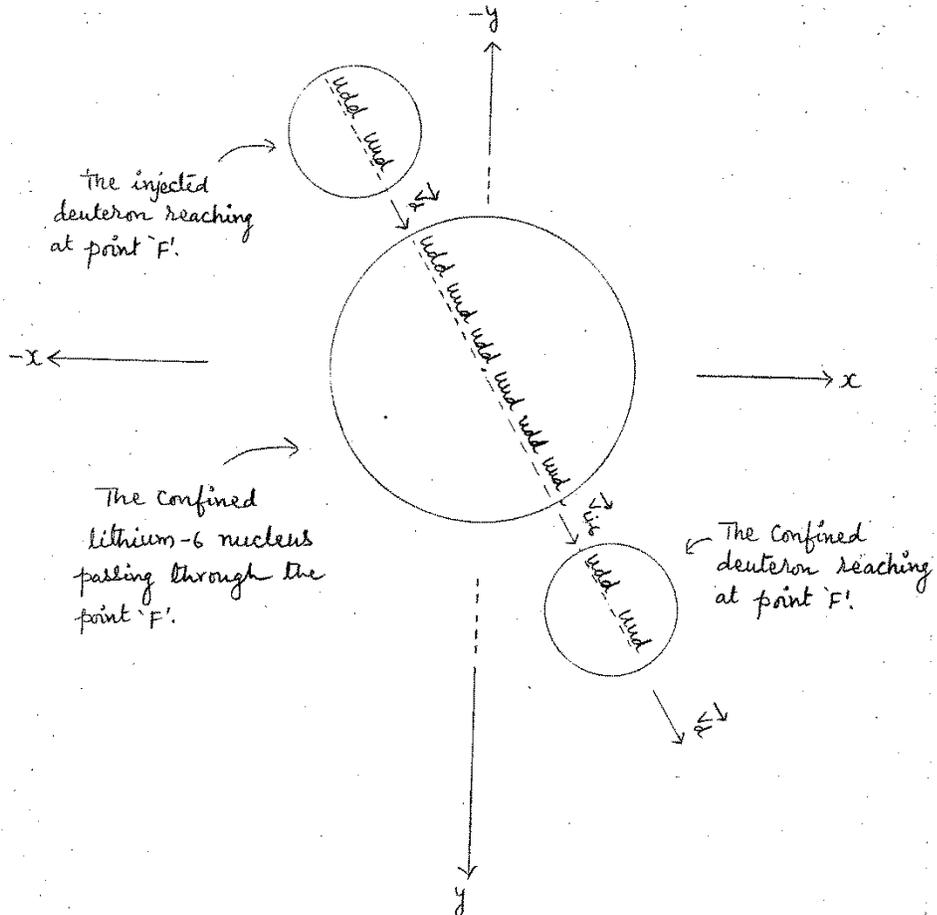
For fusion reaction



The interaction of nuclei :-

The injected deuteron reaches at point F, and interacts [experiences a repulsive force due to the confined lithium-6 and confined deuteron] with the confined lithium-6 and confined deuteron passing through the point F. the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined lithium-6 and confined deuteron.

Interaction of nuclei (1)



Interaction of nuclei (2)

2. Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (the injected deuteron and the lithium-6 nucleus and confined deuteron) behave like a liquid and form a homogeneous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 10 groups of quarks surrounded by the gluons.

The homogenous compound nucleus

(nearby located) groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

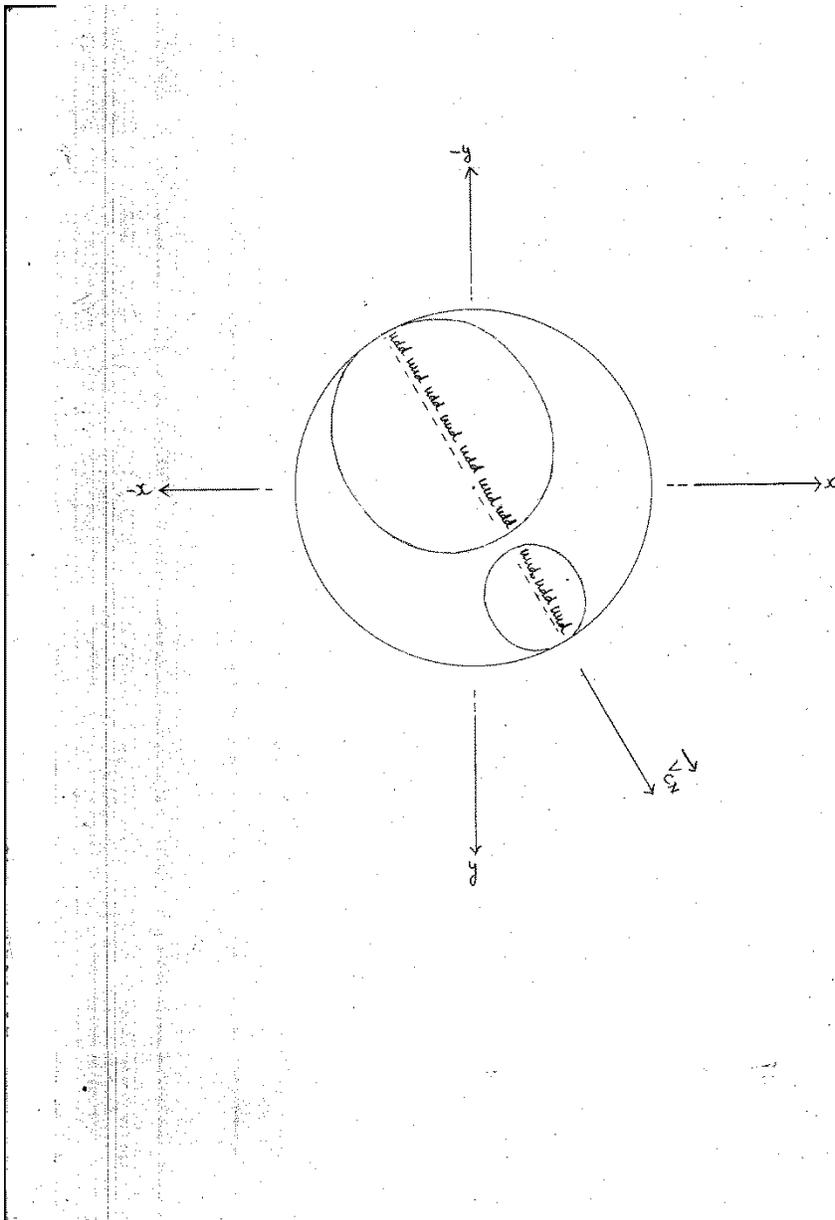
While , the remaining groups of quarks to become a stable nucleus (the helium - 3) includes the other two (nearby located) groups of quarks with their surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe ' A '] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two dissimilar lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the lithium – 7 nucleus and the smaller nucleus is the helium-3.

The greater nucleus is the lobe 'A ' and the smaller nucleus is the lobe 'B' while the remaining space represent the remaining gluons .



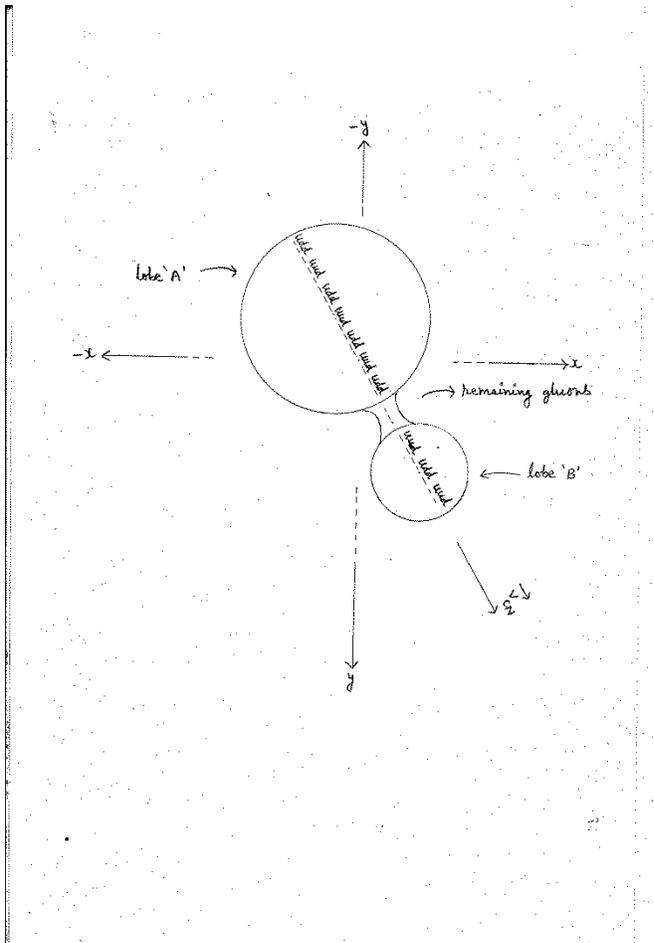
Formaton of lobes

4..Final stage of the heterogeneous compound nucleus :-

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

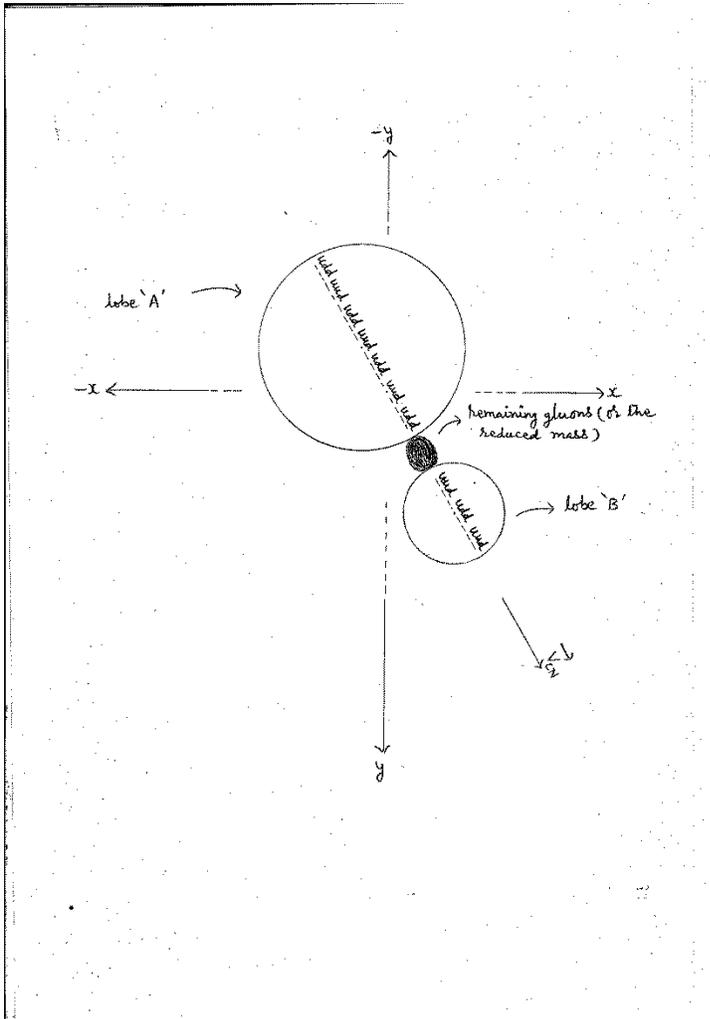
So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogeneous compound nucleus

For $\alpha = 60$ degrees

$\beta = 30$ degrees



Final stage of the heterogenous compound nucleus

where, $\alpha = 60$ degree

$\beta = 30$ degree

Formation of compound nucleus :

Each deuteron has to overcome the the electrostatic repulsive force exerted by the lithion-6 as well as by other deuteron to form a compund nucleus .

(1)Just before fusion, to overcome the electrostatic repulsive force exerted by the lithion-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of eletromagnetic waves its energy equal to 45.5598 kev.

Just before fusion, to overcome the electrostatic repulsive force exerted by the confined deuteron , the deuteron of n^{th} bunch loses (radiates its energy in the form of eletromagnetic waves its energy equal to 5.0622 kev.

so, just before fusion, the total loss in kinetic energy of the deuteron is --

$$E_{\text{loss}} = (5.0622 + 45.5598) \text{ kev} \\ = 50.622 \text{ Kev}$$

so, just before fusion the kinetic energy of deuteron is –

$$E_b = E_{\text{injected}} - E_{\text{loss}} \\ E_b = 153.6 \text{ kev} - 50.622 \text{ kev} \\ = 102.978 \text{ kev} \\ = 0.102978 \text{ Mev}$$

(2)just before fusion lithion – 6 opposes each deuteron with 136.0700 kev

as there are two deuterons so Just before fusion, to overcome the electrostatic repulsive force exerted by the each deuteron, the lithion-6 loses (radiates its energy in the form of eletromagnetic waves) its energy equal to 272.14 kev.

so, just before fusion,

the kinetic energy of lithion -6 is –

$$E_b = E_{\text{confined}} - E_{\text{loss}} \\ E_b = 388.2043 \text{ kev} - 272.14 \text{ kev} \\ = 116.0643 \text{ kev} \\ = 0.1160643 \text{ Mev}$$

Kinetic energy of the compound nucleus

$$\text{K.E.} = [E_b \text{ of injected deuteron}] + [E_b \text{ of lithium-6}] + [E_b \text{ of confined deuteron}]$$

$$= [102.978 \text{ Kev}] + [116.0643 \text{ Kev}] + [102.978 \text{ Kev}]$$

$$= 322.0203 \text{ Kev.}$$

$$= 0.3220203 \text{ Mev}$$

$$M = m_d + m_{\text{Li-6}} + m_d$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}] + [3.3434 \times 10^{-27} \text{ Kg}]$$

$$= 16.6721 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3220203 \text{ meV}$$

$$V_{\text{CN}} = \left(\frac{2 \times 0.3220203 \times 1.6 \times 10^{-13} \text{ }^{\frac{1}{2}}}{16.6721 \times 10^{-27} \text{ kg}} \right) \text{ m/s}$$

$$V_{\text{CN}} = \frac{1.03046496 \times 10^{-13} \text{ }^{\frac{1}{2}}}{16.6721 \times 10^{-27}} \text{ m/s}$$

$$V_{\text{CN}} = [0.06180774827 \times 10^{14}]^{\frac{1}{2}} \text{ m/s}$$

$$V_{\text{CN}} = 0.2486 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$(1) \vec{V}_x = V_{\text{CN}} \cos \alpha$$

$$= 0.2486 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 0.1243 \times 10^7 \text{ m/s}$$

$$(2) \vec{V}_y = V_{\text{CN}} \cos \beta$$

$$= 0.2486 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 0.2152 \text{ m/s}$$

$$(3) \vec{V}_Z = V_{CN} \cos \gamma$$

$$= 0.2486 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus , due to its instability , splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – **lithium-7**, the helium - 3 and the reduced mass (Δm) .

Out of them , the two particles (the **lithium-7**, the helium - 3) are stable while the third one (reduced mass) is unstable .

According to the law of inertia , each particle that is produced due to splitting of the compound nucleus, has an inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}).

So, for conservation of momentum

$$M\vec{V}_{cn} = (m_{Li-7} + \Delta m + m_{He-3})\vec{V}_{cn}$$

Where ,

$$M = \text{mass of the compound nucleus}$$

$$\vec{V}_{cn} = \text{velocity of the compound nucleus}$$

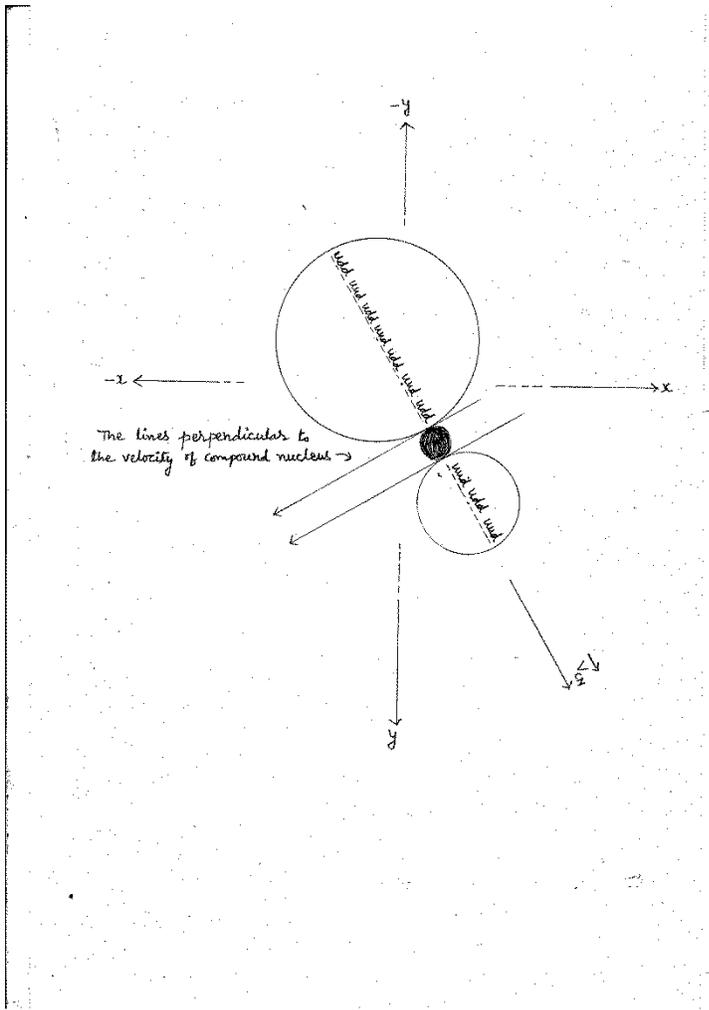
$$m_{Li-7} = \text{mass of the } \mathbf{lithium-7}$$

$$m_{He-3} = \text{mass of the helium - 3 nucleus}$$

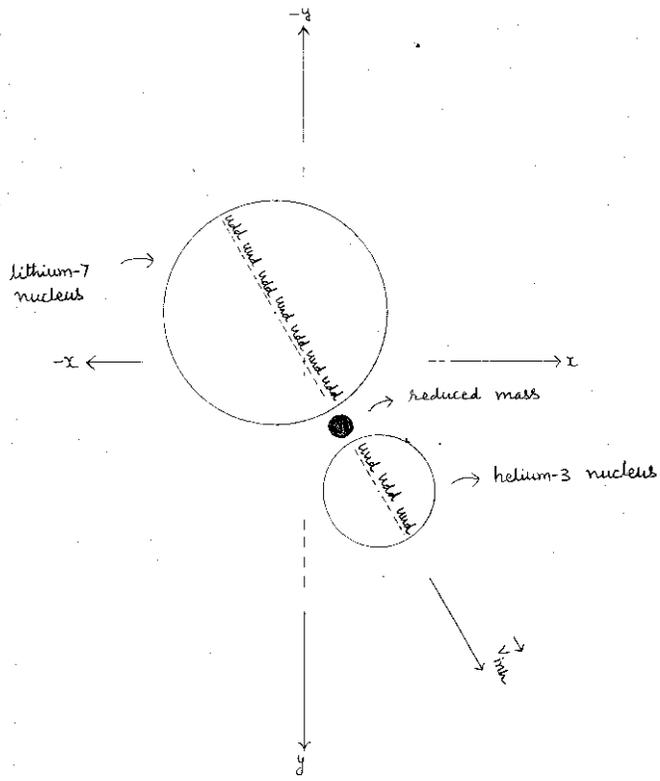
$$\Delta m = \text{reduced mass}$$

The splitting of the heterogeneous compound nucleus

The heterogeneous compound nucleus to show the lines perpendicular to the \vec{V}_{cn}



The splitting of the heterogeneous compound nucleus



Inherited velocity of the particles (s) : -

Each particles has inherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus(\vec{v}_{CN}).

(I). Inherited velocity of the particle lithium -7

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle Li-7

$$1. \vec{v}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1243 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2152 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(II). Inherited velocity of the He-3

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the He-3

$$1. \vec{v}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1243 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2152 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(iii) Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{Li-6} + m_d] - [m_{Li-7} + m_{He-3}]$$

$$\Delta m = [2.01355 + 6.01347708 + 2.01355] - [7.01435884 + 3.014932] \text{ amu}$$

$$\Delta m = [10.04057708] - [10.02929084] \text{ amu}$$

$$\Delta m = 0.01128624 \text{ amu}$$

$$\Delta m = 0.01128624 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm).

$$E_{\text{inh}} = \frac{1}{2} \Delta m V_{\text{CN}}^2$$

$$\Delta m = 0.01128624 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{\text{CN}}^2 = 0.06180774827 \times 10^{14}$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.01128624 \times 1.6605 \times 10^{-27} \times 0.06180774827 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00057916337 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.000361 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.01128624 \times 931 \text{ Mev}$$

$$E_R = 10.507489 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{\text{inh}} + E_R$$

$$E_T = [0.000361 + 10.507489] \text{ Mev}$$

$$E_T = 10.50785 \text{ Mev}$$

Increased energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses .so,the increased energy (E_{inc}) of the particles are :-

1.. For **lithion – 7**

$$E_{inc} = \frac{m_{He-3}}{m_{He-3} + m_{Li-7}} \times E_T$$

$$E_{inc} = \frac{3.014932 \text{ amu}}{[3.014932 + 7.01435884] \text{ amu}} \times 10.50785 \text{ Mev}$$

$$E_{inc} = \frac{3.014932}{10.02929084} \times 10.50785 \text{ Mev}$$

$$E_{inc} = 0.3006126802 \times 10.50785 \text{ Mev}$$

$$E_{inc} = 3.158792 \text{ Mev}$$

2..increased energy of the helium- 3

$$E_{inc} = [E_T] - [\text{increased energy of the Li-7}]$$

$$E_{inc} = [10.50785] - [3.158792] \text{ Mev}$$

$$E_{\text{inc}} = 7.349058 \text{ Mev}$$

6..Increased velocity of the particles .

(1) For helium- 3

$$E_{\text{inc}} = \frac{1}{2} m_{\text{He-3}} V_{\text{inc}}^2$$

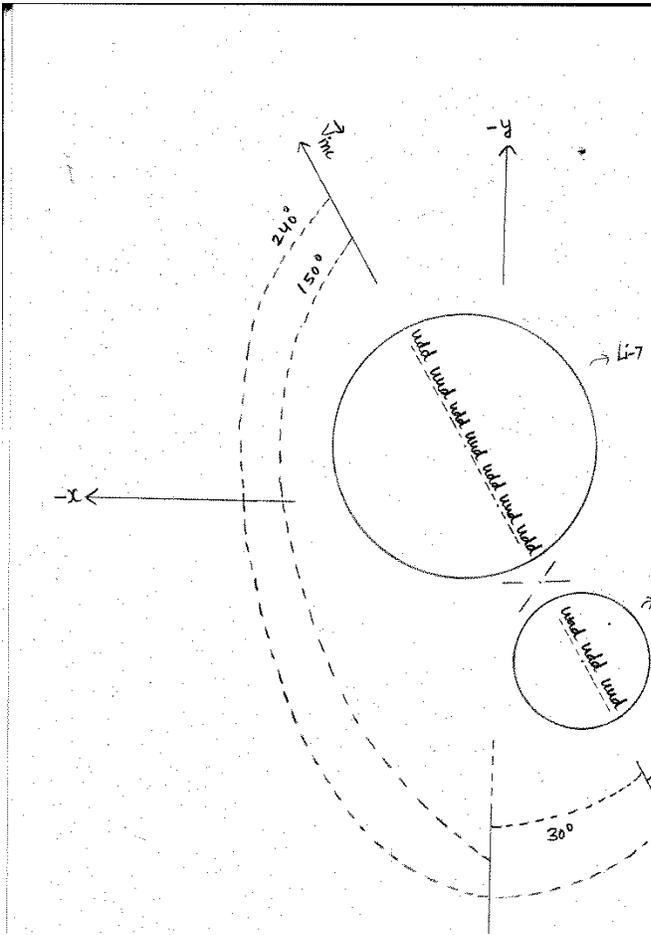
$$\begin{aligned} V_{\text{inc}} &= \left[2 \times E_{\text{inc}} / m_{\text{He-3}} \right]^{\frac{1}{2}} \\ &= \left[\frac{2 \times 7.349058 \times 1.6 \times 10^{-13} \text{ J}}{5.00629 \times 10^{-27} \text{ kg}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= \left[\frac{23.5169856 \times 10^{-13}}{5.00629 \times 10^{-27}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= \left[4.69748768049 \times 10^{14} \right]^{\frac{1}{2}} \text{ m/s} \\ &= 2.1673 \times 10^7 \text{ m/s} \end{aligned}$$

(2) For lithium-7

$$\begin{aligned} V_{\text{inc}} &= \left[2 \times E_{\text{inc}} / m_{\text{Li-7}} \right]^{\frac{1}{2}} \\ &= \left[\frac{2 \times 3.158792 \times 1.6 \times 10^{-13} \text{ J}}{11.6473 \times 10^{-27} \text{ kg}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= \left[\frac{10.1081344 \times 10^{-13}}{11.6473 \times 10^{-27}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= \left[0.86785215457 \times 10^{14} \right]^{\frac{1}{2}} \text{ m/s} \\ &= 0.9315 \times 10^7 \text{ m/s} \end{aligned}$$

7 Angle of propulsion

1. As the reduced mass converts into energy, the total energy (E_T) propel both the particles with equal and opposite momentum.
2. We know that when there a fusion process occurs, then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus (\vec{V}_{CN})].
- 3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis, 30° angle with y-axis and 90° angle with z-axis .
 so, the helium-3 is propelled making 60° angle with x-axis, 30° angle with y-axis and 90° angle with z-axis .
 While the lithium - 7 is propelled making 240° angle with x-axis, 150° angle with y-axis and 90° angle with z-axis .



Components of the increased velocity (V_{inc}) of the particles.

(i) For lithium- 7

$$\vec{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 0.9315 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(240) = -0.5$$

$$\vec{1}_{V_x} = 0.9315 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.4657 \times 10^7 \text{ m/s}$$

$$\vec{2}_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(150) = -0.866$$

$$\vec{2}_{V_y} = 0.9315 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.8066 \times 10^7 \text{ m/s}$$

$$\vec{3}_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\vec{3}_{V_z} = 0.9315 \times 10^7 \times 0$$

$$= 0 \text{ m/s}$$

For helium - 3

$$\vec{1}_{V_x} = V_{inc} \cos \alpha$$

$$V_{inc} = 2.1673 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\vec{1}_{V_x} = 2.1673 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 1.0836 \times 10^7 \text{ m/s}$$

$$\vec{2}_{V_y} = V_{inc} \cos \beta$$

$$\cos \beta = \cos(30) = 0.866$$

$$\vec{2}_{V_y} = 2.1673 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 1.8768 \times 10^7 \text{ m/s}$$

$$\vec{3}_{V_z} = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos(90) = 0$$

$$\vec{3}_{V_z} = 2.1673 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9.. Components of the final velocity (V_f) of the particles

I For lithium-7

According to-	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{V}_f)= $(\vec{v}_{inh})+(\vec{v}_{inc})$
X –axis	$\vec{v}_x = 0.1243 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.4657 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.3414 \times 10^7 \text{ m/s}$
y – axis	$\vec{v}_y = 0.2152 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.8066 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.5914 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..For helium -3

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{V}_f)= $(\vec{v}_{inh})+(\vec{v}_{inc})$
X –axis	$\vec{v}_x = 0.1243 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.0836 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.2079 \times 10^7 \text{ m/s}$
y – axis	$\vec{v}_y = 0.2152 \times 10^7 \text{ m/s}$	$\vec{v}_y = 1.8768 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.092 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final velocity (v_f) of the lithium- 7

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.3414 \times 10^7 \text{ m/s}$$

$$V_y = 0.5914 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.3414 \times 10^7)^2 + (0.5914 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.11655396 \times 10^{14}) + (0.34975396 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.46630792 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.6828 \times 10^7 \text{ m/s}$$

Final kinetic energy of the lithium - 7

$$E = \frac{1}{2} m_{\text{Li-7}} V_f^2$$

$$E = \frac{1}{2} \times 11.6473 \times 10^{-27} \times 0.46630792 \times 10^{14} \text{ J}$$

$$= 2.7156141183 \times 10^{-13} \text{ J}$$

$$= 1.697258 \text{ MeV}$$

$$m_{\text{Li-7}} V_f^2 = 11.6473 \times 10^{-27} \times 0.46630792 \times 10^{14} \text{ J}$$

$$= 5.4312 \times 10^{-13} \text{ J}$$

10.. Final velocity (v_f) of the helium -3

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 1.2079 \times 10^7 \text{ m/s}$$

$$V_y = 2.092 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (1.2079 \times 10^7)^2 + (2.092 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (1.45902241 \times 10^{14}) + (4.376464 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 5.83548641 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 2.4156 \times 10^7 \text{ m/s}$$

Final kinetic energy of the helium -3

$$E = \frac{1}{2} m_{\text{He-3}} V_f^2$$

$$E = \frac{1}{2} \times 5.00629 \times 10^{-27} \times 5.83548641 \times 10^{14} \text{ J}$$

$$= 14.6070686297 \times 10^{-13} \text{ J}$$

$$= 9.129417 \text{ MeV}$$

$$m_{\text{He-3}} v_f^2 = 5.00629 \times 10^{-27} \times 5.83548641 \times 10^{14} \text{ J}$$

$$= 29.2141 \times 10^{-13} \text{ J}$$

Forces acting on the lithion – 7 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.3414 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 3 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 3 \times 1.6 \times 10^{-19} \times 0.3414 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 1.6403 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_y is according to (+) y-axis ,

so ,

$$\vec{F}_y = 1.6403 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 3 \times 1.6 \times 10^{-19} \times 0.3414 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 1.6408 \times 10^{-13} \text{ N}$$

Form the right hand palm rule , the direction of the force \vec{F}_z is according to (+) Z- axis ,

so ,

$$\vec{F}_z = 1.6408 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin\theta$$

$$\vec{v}_y = -0.5914 \times 10^7 \quad \text{m/s}$$

$$\vec{B}_z = 1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin\theta = \sin 90^\circ = 1$$

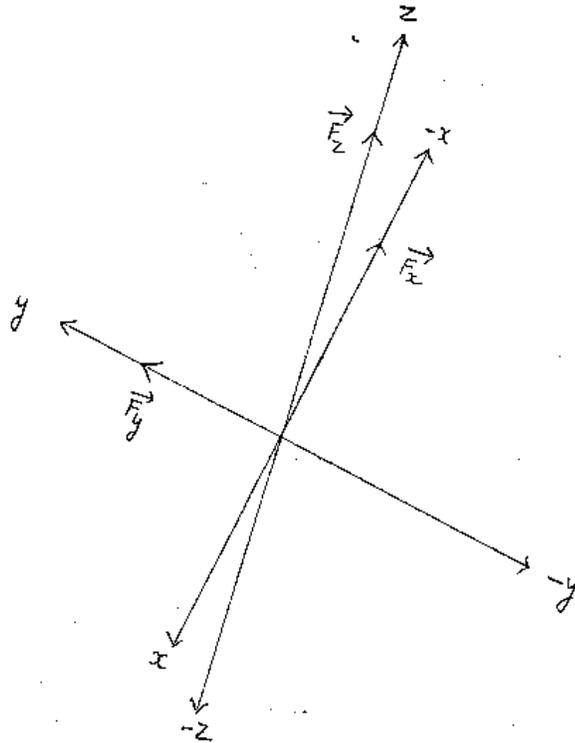
$$F_x = 3 \times 1.6 \times 10^{-19} \times 0.5914 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 2.8415 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x axis,

$$\text{so, } \vec{F}_x = -2.8415 \times 10^{-13} \text{ N}$$

Forces acting on the lithion-7



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 2.8415 \times 10^{-13} \text{ N}$$

$$F_y = 1.6403 \times 10^{-13} \text{ N}$$

$$F_z = 1.6408 \times 10^{-13} \text{ N}$$

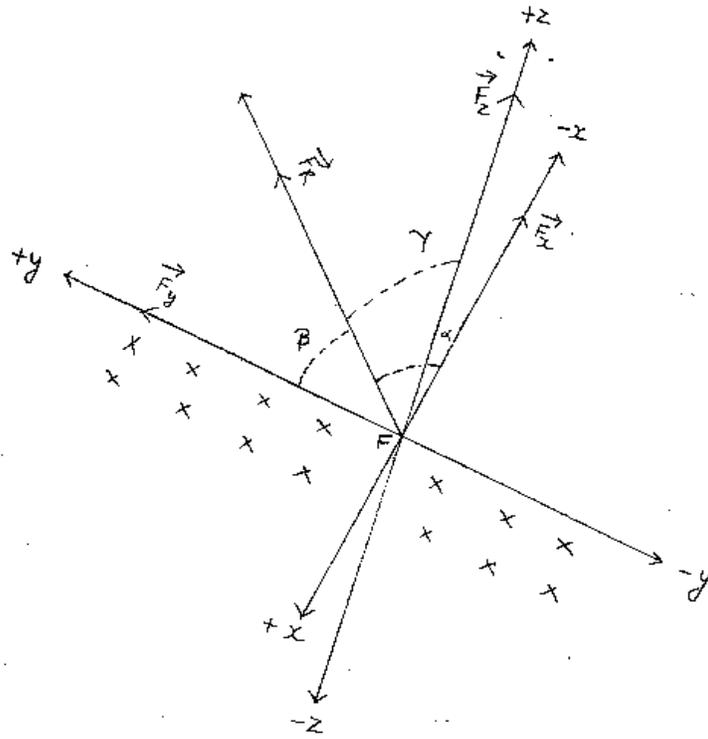
$$F_R^2 = (2.8415 \times 10^{-13})^2 + (1.6403 \times 10^{-13})^2 + (1.6408 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (8.07412225 \times 10^{-26}) + (2.69058409 \times 10^{-26}) + (2.69222464 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 13.45693098 \times 10^{-26} \text{ N}^2$$

$$F_R = 3.6683 \times 10^{-13} \text{ N}$$

Resultant force acting on the lithion-7



Radius of the circular orbit to be followed by the lithion - 7

$$r = mv^2 / F_R$$

$$mv^2 = 5.4312 \times 10^{-13} \text{ J}$$

$$F_r = 3.6683 \times 10^{-13} \text{ N}$$

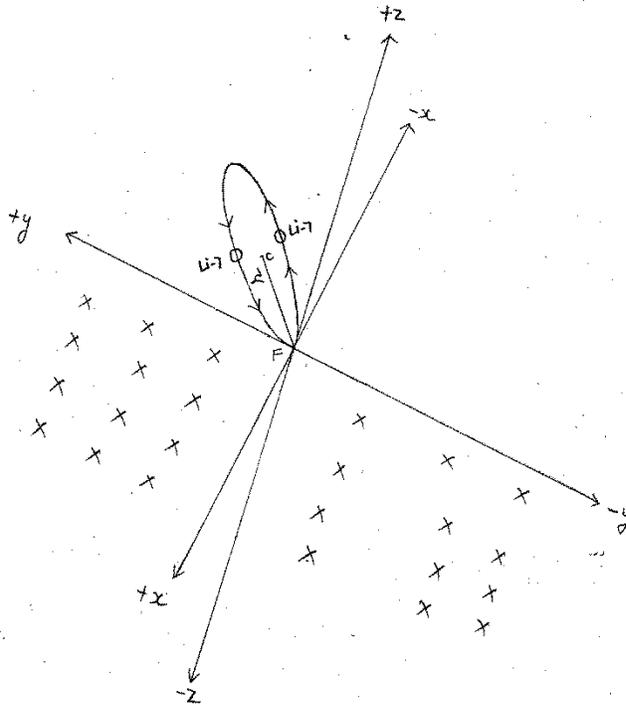
$$5.4312 \times 10^{-13} \text{ J}$$

$$r = \frac{5.4312 \times 10^{-13} \text{ J}}{3.6683 \times 10^{-13} \text{ N}}$$

$$r = 1.4805 \text{ m}$$

The circular orbit to be followed by the lithion -7 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

C= center of the circular orbit to be followed by the lithion -7.



The plane of the circular orbit to be followed by the lithium -7 makes angles with positive x , y and z -axes as follows :-

1 with x - axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = -2.8415 \times 10^{-13} \text{ N}$$

$$F_r = 3.6683 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7746$$

$$\alpha = 219.23 \text{ degree } [\because \cos (219.23) = -0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = 1.6403 \times 10^{-13} \text{ N}$$

$$F_r = 3.6683 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4471$$

$$\beta = 63.44 \text{ degree } [\because \cos (63.44) = 0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{F_z}{F_r}$$

$$\frac{F_z}{F_r} = \underline{1.6408 \times 10^{-13} \text{ N}}$$

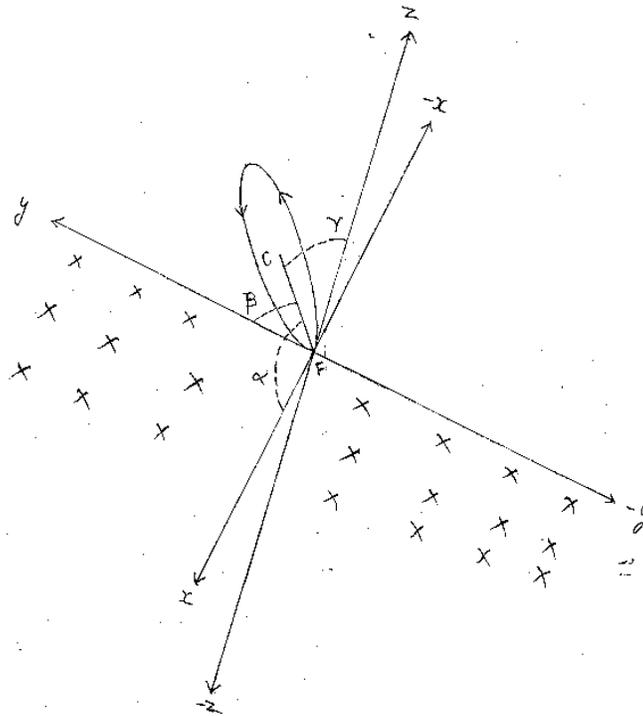
$$F_r = 3.6683 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4472$$

$$\gamma = 63.43 \text{ degree}$$

The plane of the circular orbit to be followed by the lithium ⁻⁷ makes angles with positive x, y, and z axes as follows :-



Where,

$$\alpha = 219.23 \text{ degree}$$

$$\beta = 63.44 \text{ degree}$$

$$\gamma = 63.43 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the lithion- 7.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 1.4805 \text{ m}$$

$$= 2.961 \text{ m}$$

$$\cos \alpha = -0.7746$$

$$\begin{aligned}x_2 - x_1 &= d \times \cos \alpha \\x_2 - x_1 &= 2.961 \times (-0.7746) \quad \text{m} \\x_2 - x_1 &= -2.2935 \text{ m} \\x_2 &= -2.2935 \text{ m} \quad [\because x_1 = 0] \\ \cos \beta &= \frac{y_2 - y_1}{d}\end{aligned}$$

$$\cos \beta = 0.4471$$

$$\begin{aligned}y_2 - y_1 &= d \times \cos \beta \\y_2 - y_1 &= 2.961 \times 0.4471 \quad \text{m} \\y_2 - y_1 &= 1.3238 \text{ m} \\y_2 &= 1.3238 \text{ m} \quad [\because y_1 = 0]\end{aligned}$$

$$\begin{aligned}\cos \gamma &= \frac{z_2 - z_1}{d} \\d\end{aligned}$$

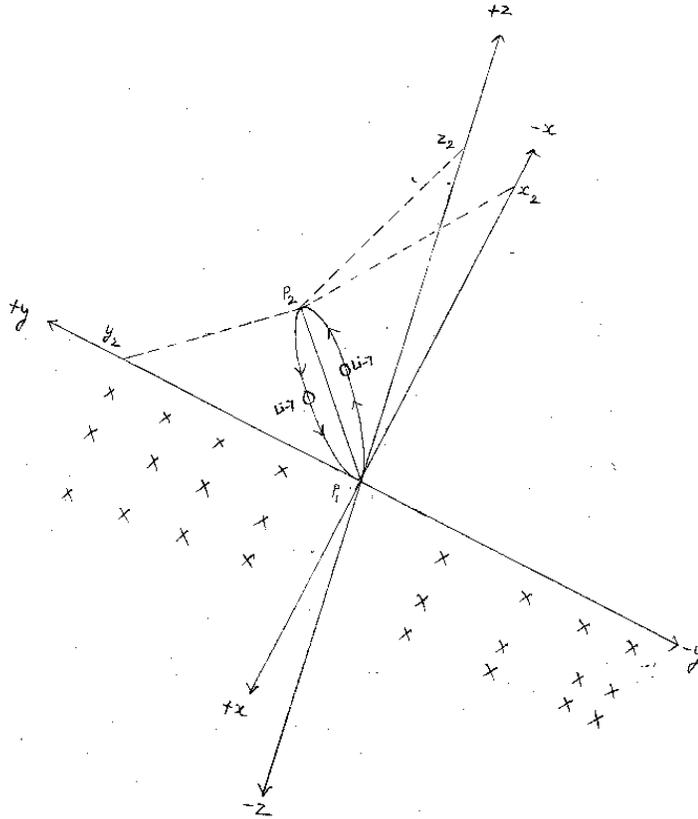
$$\cos \gamma = 0.4472$$

$$\begin{aligned}z_2 - z_1 &= d \times \cos \gamma \\z_2 - z_1 &= 2.961 \times 0.4472 \text{ m} \\z_2 - z_1 &= 1.3241 \text{ m} \\z_2 &= 1.3241 \text{ m} \quad [\because z_1 = 0]\end{aligned}$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium-7 are as shown below.

The line ____ is the diameter of the circle .

P_1P_2



Conclusion :-

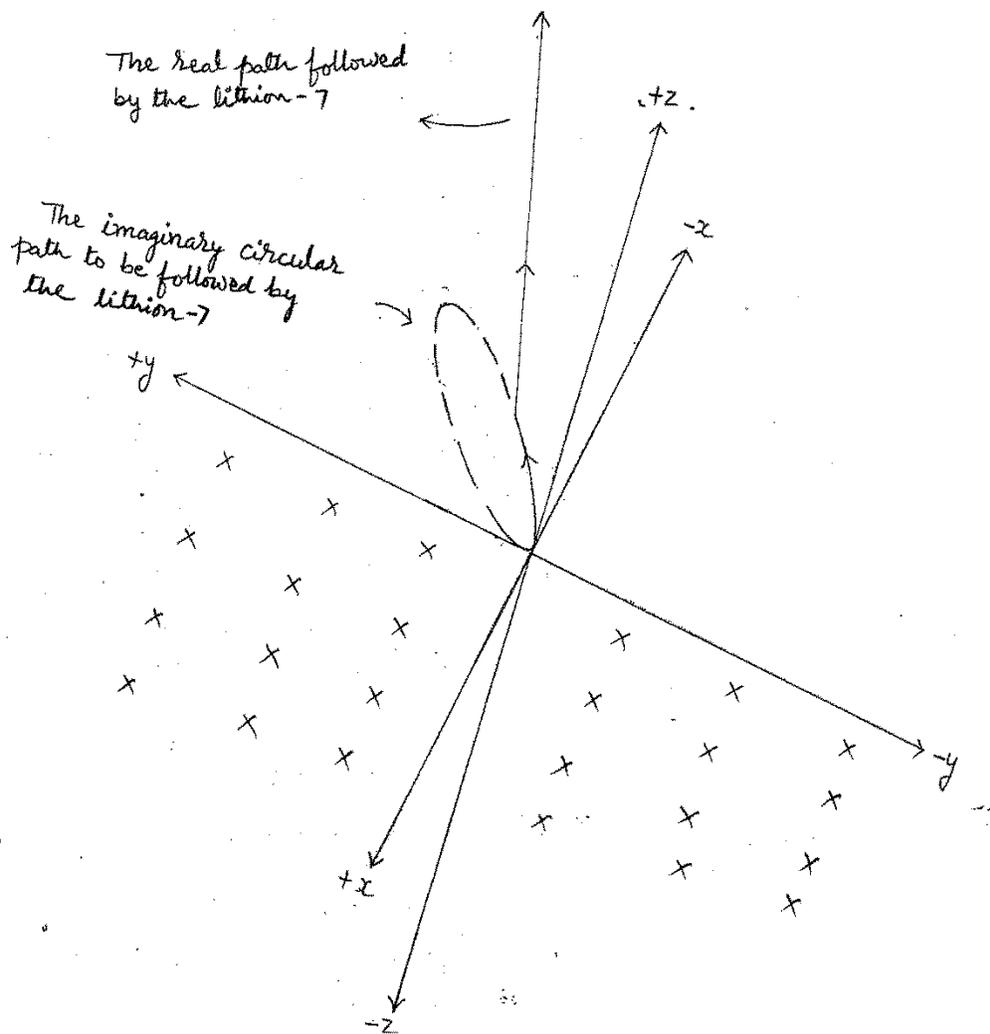
The directions components $\left[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z \right]$ of the resultant force $\left(\vec{F}_r \right)$ that are acting on the lithium-7 nucleus are along **-x, +y and +z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-7 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the lithium-7 nucleus to undergo to a circular orbit of radius 1.4805 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-2.2935 \text{ m}, 1.3238 \text{ m}, 1.3241 \text{ m})$ where the magnetic fields are not applied.

So, It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the lithium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. So, in spite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

The lithium-7 nucleus is not confined within into the tokamak.



Forces acting on the helium-3 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{v}_x = 1.2079 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 2 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 2 \times 1.6 \times 10^{-19} \times 1.2079 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 3.8691 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = -3.8691 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 2 \times 1.6 \times 10^{-19} \times 1.2079 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 3.8703 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = -3.8703 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = 2.092 \times 10^7 \quad \text{m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

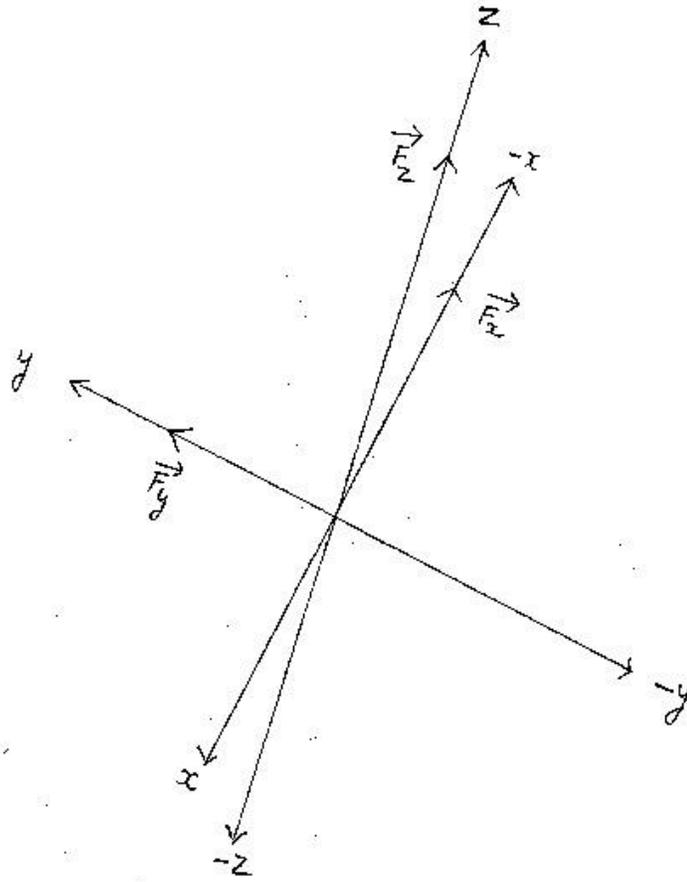
$$\sin \theta = \sin 90^\circ = 1$$

$$F_x = 2 \times 1.6 \times 10^{-19} \times 2.092 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 6.7010 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x-axis,

$$\vec{F}_x = 6.7010 \times 10^{-13} \text{ N}$$



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 6.7010 \times 10^{-13} \text{ N}$$

$$F_y = 3.8691 \times 10^{-13} \text{ N}$$

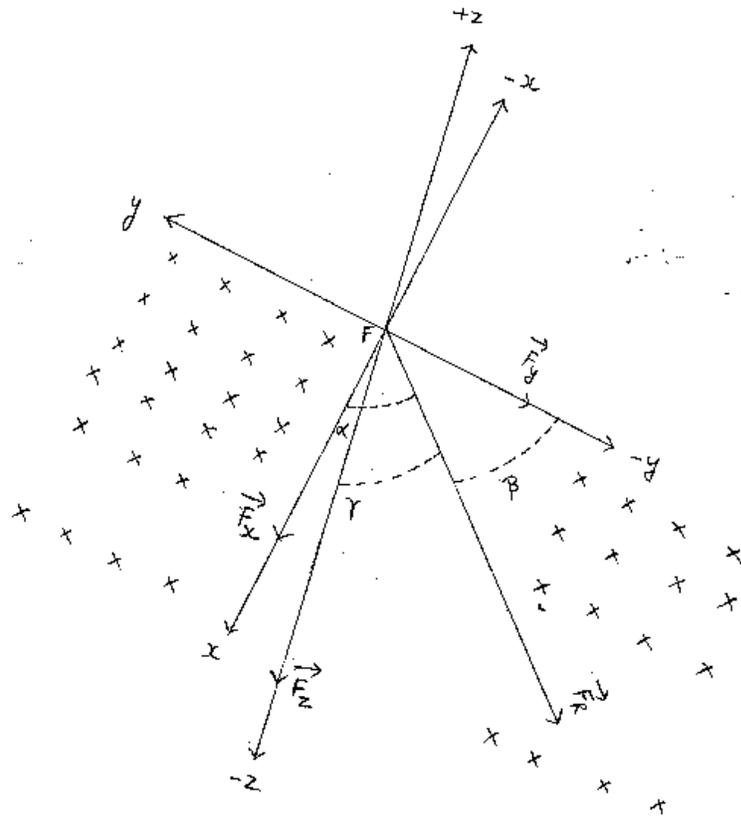
$$F_z = 3.8703 \times 10^{-13} \text{ N}$$

$$F_R^2 = (6.7010 \times 10^{-13})^2 + (3.8691 \times 10^{-13})^2 + (3.8703 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (44.903401 \times 10^{-26}) + (14.96993481 \times 10^{-26}) + (14.97922209 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 74.8525579 \times 10^{-26} \text{ N}^2$$

$$F_R = 8.6517 \times 10^{-13} \text{ N}$$



Radius of the circular orbit to be followed by the helium-3

$$r = mv^2 / F_R$$

$$mv^2 = 29.2141 \times 10^{-13} \text{ J}$$

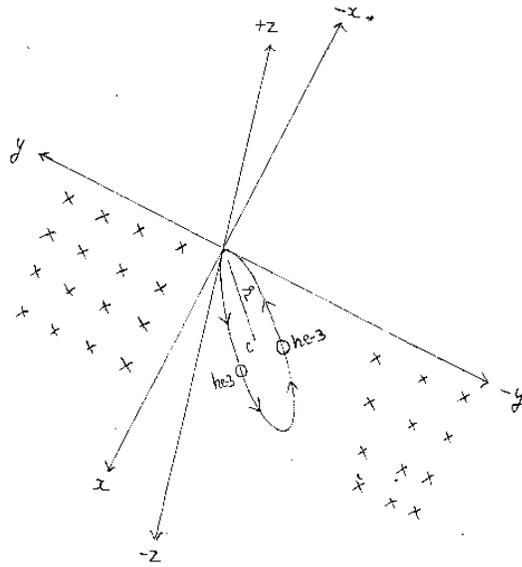
$$F_R = 8.6517 \times 10^{-13} \text{ N}$$

$$r = \frac{29.2141 \times 10^{-13} \text{ J}}{8.6517 \times 10^{-13} \text{ N}}$$

$$r = 3.3766 \text{ m}$$

The circular orbit to be followed by the **helium-3** lies in the plane made up of positive x-axis, positive y-axis and the positive z-axis.

C = center of the circular orbit to be followed by the **helium-3**.



The plane of the circular orbit to be followed by the helium -3 nucleus makes angles with positive x , y and z -axes as follows :-

1 with x - axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = 6.7010 \times 10^{-13} \text{ N}$$

$$F_r = 8.6517 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos(39.24) = 0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = -3.8691 \times 10^{-13} \text{ N}$$

$$F_r = 8.6517 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4472$$

$$\beta = 243.43 \text{ degree } [\because \cos(243.43) = -0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{F_z}{F_r}$$

$$\frac{F_z}{F_r} = \underline{-3.8703 \times 10^{-13} \text{ N}}$$

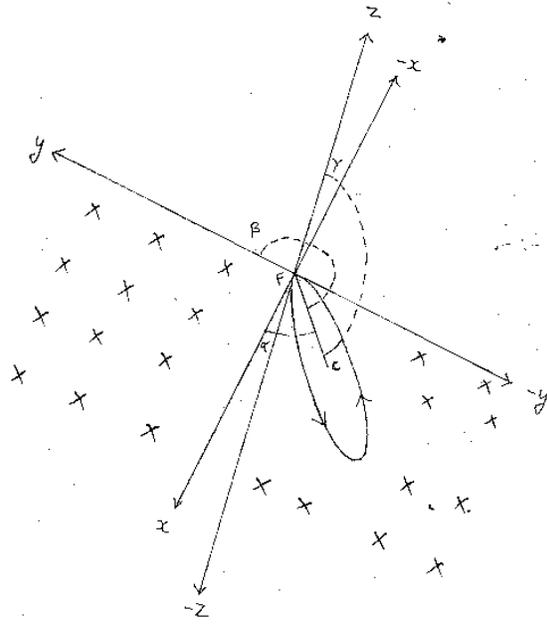
$$F_r = 8.6517 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.425 \text{ degree}$$

The plane of the circular orbit to be followed by the helium -3 nucleus makes angles with positive x, y, and z axes as follows :-



Where,

$$\alpha = 39.24 \text{ degree}$$

$$\beta = 243.43 \text{ degree}$$

$$\gamma = 243.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the **helium-3**.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 3.3766 \text{ m}$$

$$= 6.7532 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 6.7532 \times 0.7745 \quad \text{m}$$

$$x_2 - x_1 = 5.2303 \text{ m}$$

$$x_2 = 5.2303 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = -0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 6.7532 \times (-0.4472) \text{ m}$$

$$y_2 - y_1 = -3.0200 \text{ m}$$

$$y_2 = -3.0200 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 6.7532 \times (-0.4473) \quad \text{m}$$

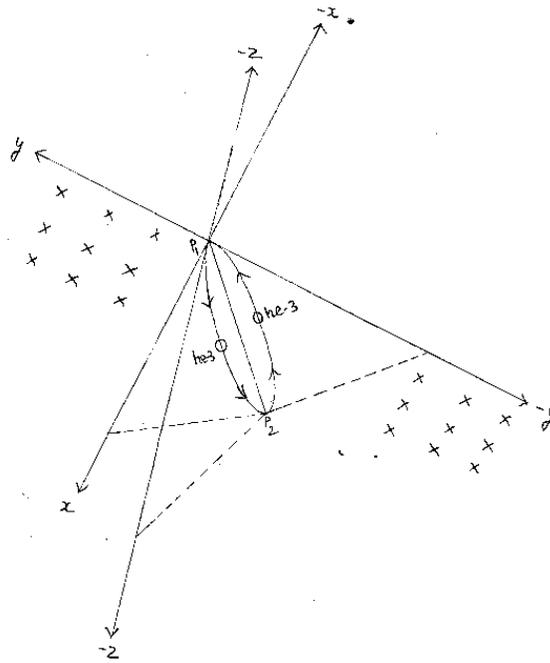
$$z_2 - z_1 = -3.0207 \text{ m}$$

$$z_2 = -3.0207 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle obtained by the helium - 3 are as shown below.

The line_____ is the diameter of the circle .

P_1P_2



Conclusion :-

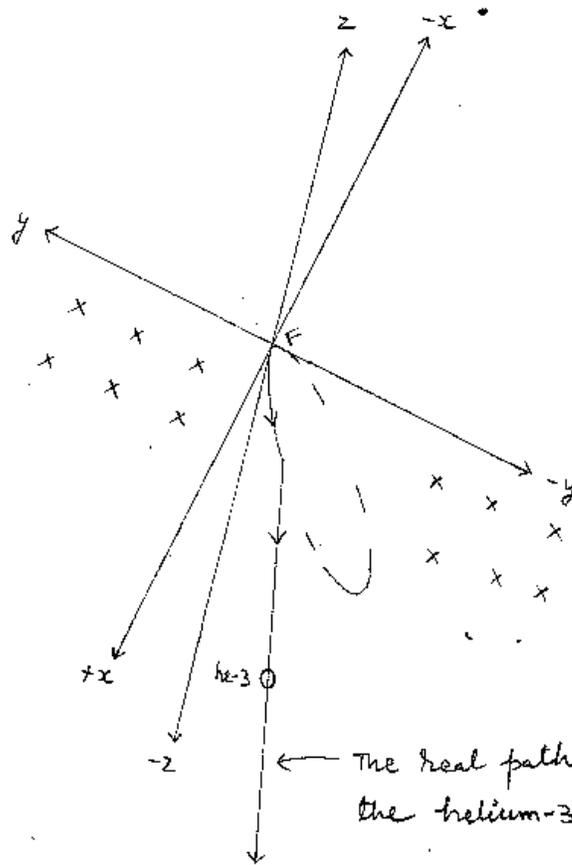
The directions components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-3 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 3.3766 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(5.2303\text{m}, -3.0200\text{ m}, -3.0207\text{ m})$. in trying to complete its circle, due to lack of space, it strikes the base wall of the tokamak.

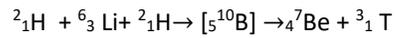
Hence the helium-3 nucleus is not confined.



← The real path followed by the helium-3 nucleus.

(In trying to follow the circular orbit, the produced helium-3 nucleus strike to the base wall of the tokamak. so, it can not complete the circle.)

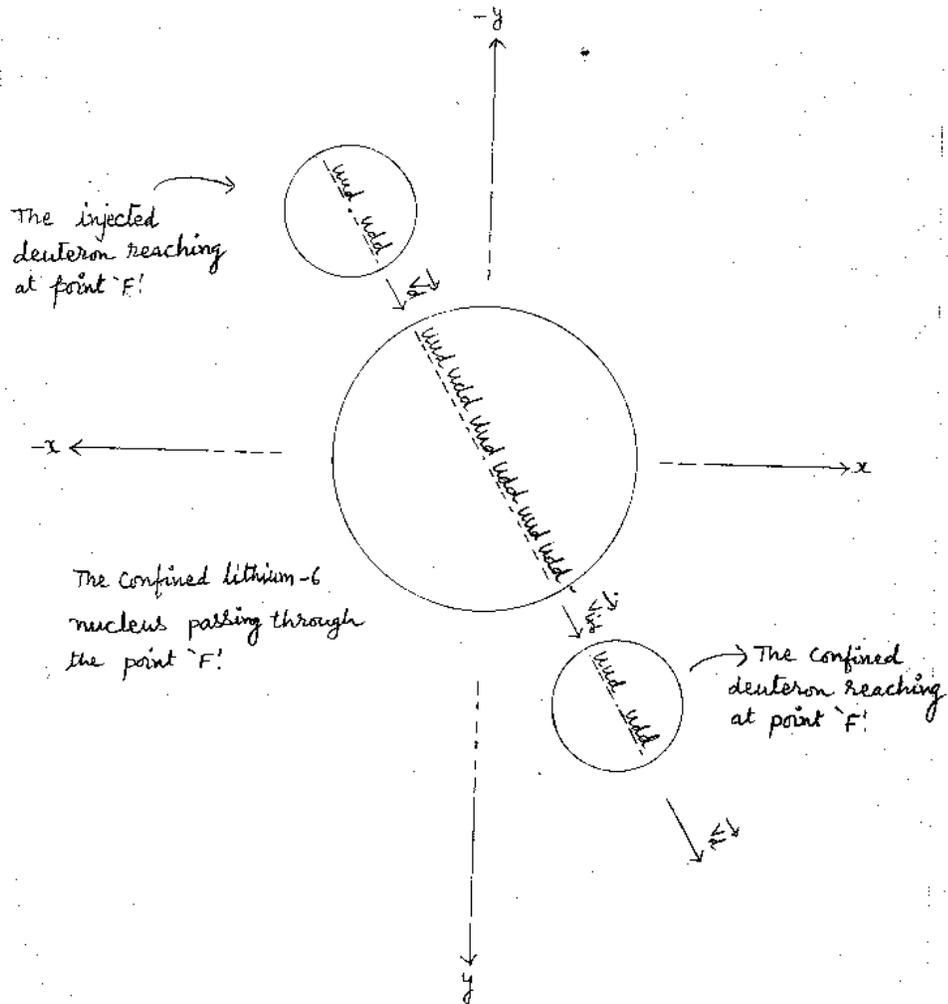
For fusion reaction

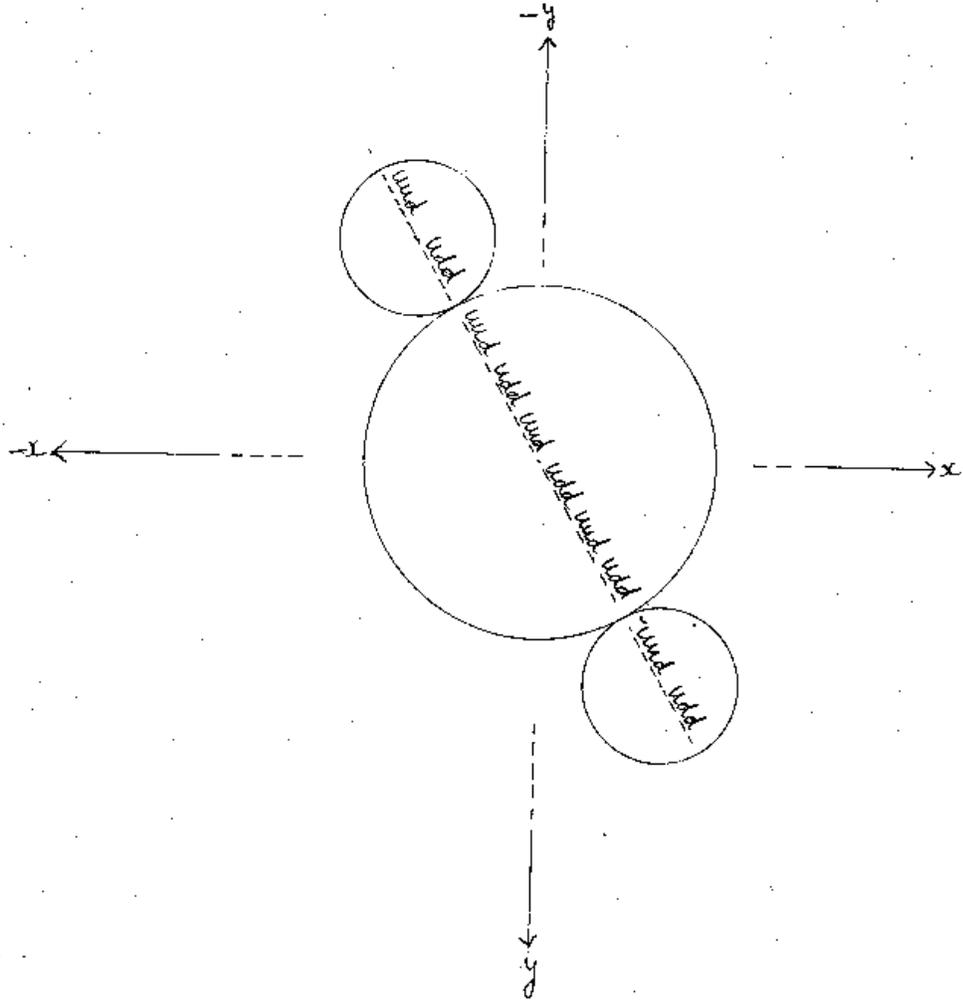


1.The interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined lithium-6 and confined deuteron] with the confined lithium-6 and confined deuteron passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined lithium-6 and confined deuteron.

Interaction of nuclei :-



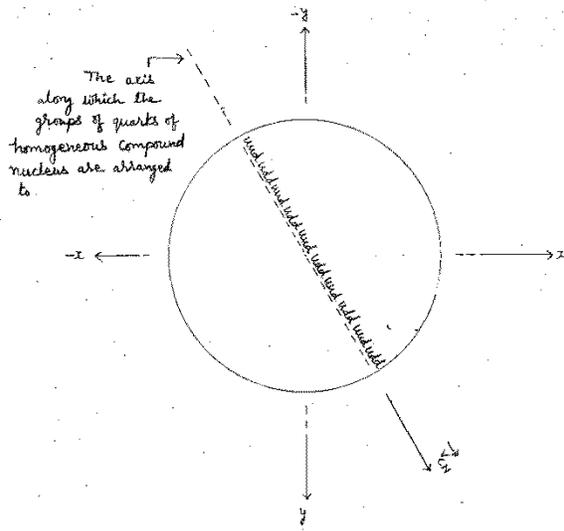


2. Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (the injected deuteron and the lithium-6 nucleus and confined deuteron) behave like a liquid and form a homogeneous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 10 groups of quarks surrounded by the gluons.

The homogenous compound nucleus



where,

$$\alpha = 60 \text{ degrees}$$

$$\beta = 30 \text{ degrees}$$

3. Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogenous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the beryllium-7) than the reactant one (the lithium-6) includes the other six (nearby located) groups of quarks with their surrounding gluons and rearrange to form the ' A ' lobe of the heterogeneous compound nucleus.

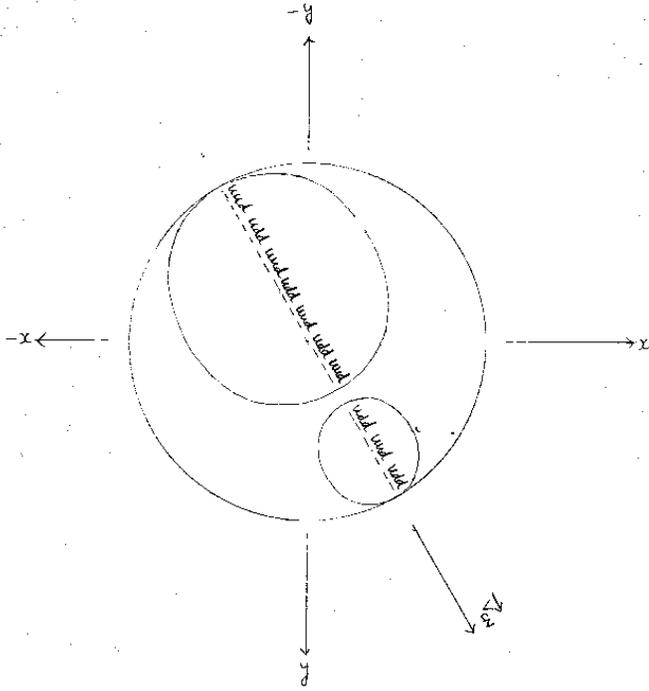
While , the remaining groups of quarks to become a stable nucleus (the triton) includes the other two (nearby located) groups of quarks with their surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe ' A '] and rearrange to form the ' B ' lobe of the heterogeneous compound nucleus .

Thus , due to formation of two dissimilar lobes within into the homogeneous compound nucleus , the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the beryllium-7 nucleus and the smaller nucleus is the triton.

The greater nucleus is the lobe ' A ' and the smaller nucleus is the lobe ' B ' while the remaining space represent the remaining gluons .



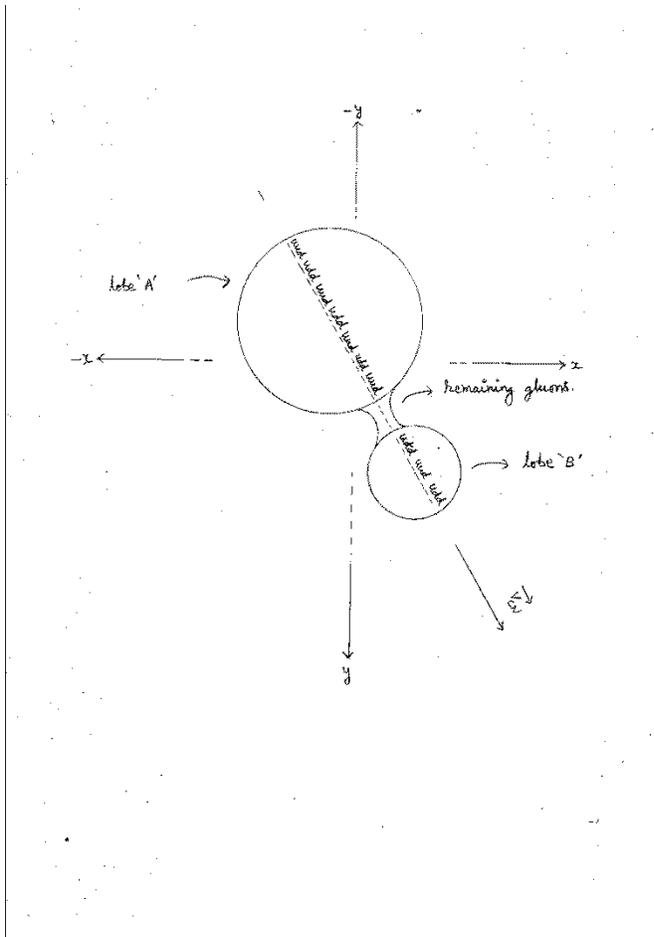
Formaton of lobes

4. Final stage of the heterogeneous compound nucleus : -

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

So, finally , the heterogeneous compound nucleus becomes like an abnormal digity eight or becomes as a dumbbell.



The heterogenous compound nucleus

For $\alpha = 60$ degree

$\beta = 30$ degree

Formation of compound nucleus :

Each deuteron has to overcome the electrostatic repulsive force exerted by the lithium-6 and deuteron to form a compound nucleus .

Just before fusion, to overcome the electrostatic repulsive force exerted by the lithium-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves its energy equal to 136.070070 kev.

Just before fusion, to overcome the electrostatic repulsive force exerted by the confined deuteron , the deuteron of n^{th} bunch loses (radiates its energy in the form of electromagnetic waves its energy equal to 5.0622 kev.

so, just before fusion, the total loss in kinetic energy of the deuteron is --

$$E_{\text{loss}} = (5.0622 + 136.07007) \text{ kev} \\ = 141.13227 \text{ Kev}$$

so, just before fusion the kinetic energy of deuteron is –

$$E_b = E_{\text{injected}} - E_{\text{loss}} \\ E_b = 204.8 \text{ kev} - 141.13227 \text{ kev} \\ = 63.66773 \text{ kev} \\ = 0.06366773 \text{ Mev}$$

Formation of compound nucleus :

Each deuteron has to overcome the the electrostatic repulsive force exerted by the lithion-6 as well as by other deuteron to form a compund nucleus .

(1)Just before fusion, to overcome the electrostatic repulsive force exerted by the lithion-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of eletromagnetic waves its energy equal to 45.5598 kev.

Just before fusion, to overcome the electrostatic repulsive force exerted by the confined deuteron , the deuteron of n^{th} bunch loses (radiates its energy in the form of eletromagnetic waves its energy equal to 5.0622 kev.

so, just before fusion, the total loss in kinetic energy of the deuteron is --

$$E_{\text{loss}} = (5.0622 + 45.5598) \text{ kev} \\ = 50.622 \text{ Kev}$$

so, just before fusion the kinetic energy of deuteron is –

$$E_b = E_{\text{injected}} - E_{\text{loss}} \\ E_b = 153.6 \text{ kev} - 50.622 \text{ kev} \\ = 102.978 \text{ kev} \\ = 0.102978 \text{ Mev}$$

(2)just before fusion lithion – 6 opposes each deuteron with 136.0700 kev

as there are two deuterons so Just before fusion, to overcome the electrostatic repulsive force exerted by the each deuteron, the lithion-6 loses (radiates its energy in the form of eletromagnetic waves) its energy equal to 272.14 kev.

so, just before fusion,

the kinetic energy of lithion -6 is –

$$E_b = E_{\text{confined}} - E_{\text{loss}} \\ E_b = 388.2043 \text{ kev} - 272.14 \text{ kev} \\ = 116.0643 \text{ kev} \\ = 0.1160643 \text{ Mev}$$

Kinetic energy of the compound nucleus

$$\text{K.E.} = [E_b \text{ of injected deuteron}] + [E_b \text{ of lithium-6}] + [E_b \text{ of confined deuteron}]$$

$$= [102.978 \text{ Kev}] + [116.0643 \text{ Kev}] + [102.978 \text{ Kev}]$$

$$= 322.0203 \text{ Kev.}$$

$$= 0.3220203 \text{ Mev}$$

$$M = m_d + m_{\text{Li-6}} + m_d$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}] + [3.3434 \times 10^{-27} \text{ Kg}]$$

$$= 16.6721 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3220203 \text{ meV}$$

$$V_{\text{CN}} = \left(\frac{2 \times 0.3220203 \times 1.6 \times 10^{-13} \text{ }^{\frac{1}{2}}}{16.6721 \times 10^{-27} \text{ kg}} \right) \text{ m/s}$$

$$V_{\text{CN}} = \frac{1.03046496 \times 10^{-13} \text{ }^{\frac{1}{2}}}{16.6721 \times 10^{-27}} \text{ m/s}$$

$$V_{\text{CN}} = [0.06180774827 \times 10^{14}] \text{ }^{\frac{1}{2}} \text{ m/s}$$

$$V_{\text{CN}} = 0.2486 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$(1). \vec{V}_x = V_{\text{CN}} \cos \alpha$$

$$= 0.2486 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 0.1243 \times 10^7 \text{ m/s}$$

$$(2) \vec{V}_y = V_{CN} \cos \beta$$

$$= 0.2486 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 0.2152 \text{ m/s}$$

$$(3) \vec{V}_z = V_{CN} \cos \gamma$$

$$= 0.2486 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus , due to its instability , splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles – **beryllium-7**, the triton and the reduced mass (Δm) .

Out of them , the two particles (the **beryllium-7** and the triton) are stable while the third one (reduced mass) is unstable .

According to the law of inertia , each particle that is produced due to splitting of the compound nucleus , has an inherited velocity (\vec{V}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}) .

So, for conservation of momentum

$$M\vec{V}_{cn} = (m_{Be-7} + \Delta m + m_t)\vec{V}_{cn}$$

Where ,

M = mass of the compound nucleus

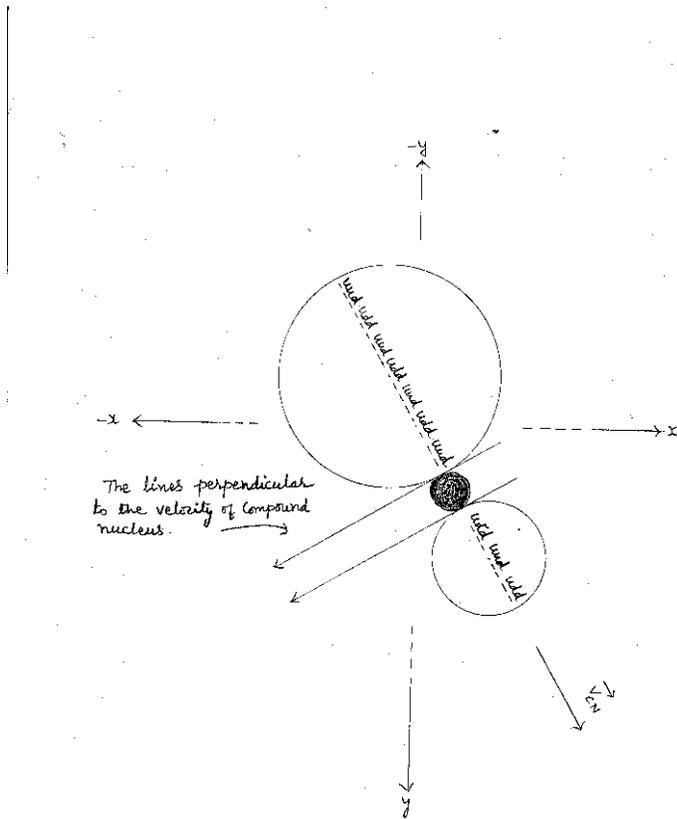
\vec{V}_{cn} = velocity of the compound nucleus

m_{Be-7} = mass of the **beryllium-7**

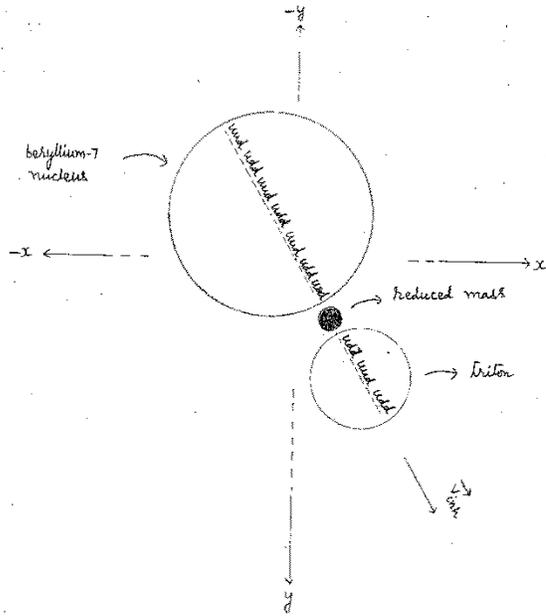
m_t = mass of the triton

Δm = reduced mass

The splitting of the heterogeneous compound nucleus



The heterogenous compound nucleus to show the lines perpendicular to the \vec{V}_{cm}



Inherited velocity of the particles (s) :-

Each particles has inherited velocity (\vec{V}_{inh}) equal to the velocity of the compound nucleus(\vec{V}_{cn}).

(I). Inherited velocity of the particle Beryllium-7

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle Beryllium-7

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1243 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2152 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(II) . Inherited velocity of the triton

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the triton

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1243 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2152 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(iii) Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into energy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{\text{Li-6}} + m_d] - [m_{\text{Be-7}} + m_t]$$

$$\Delta m = [2.01355 + 6.01347708 + 2.01355] - [7.01473555 + 3.0155] \text{ amu}$$

$$\Delta m = [10.04057708] - [10.03023555] \text{ amu}$$

$$\Delta m = 0.01034153 \text{ amu}$$

$$\Delta m = 0.01034153 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm).

$$E_{\text{inh}} = \frac{1}{2} \Delta m V_{\text{CN}}^2$$

$$\Delta m = 0.01034153 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{\text{CN}}^2 = 0.06180774827 \times 10^{14}$$

$$E_{\text{inh}} = \frac{1}{2} \times 0.01034153 \times 1.6605 \times 10^{-27} \times 0.06180774827 \times 10^{14} \text{ J}$$

$$E_{\text{inh}} = 0.00053068474 \times 10^{-13} \text{ J}$$

$$E_{\text{inh}} = 0.000331 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.01034153 \times 931 \text{ Mev}$$

$$E_R = 9.627964 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{\text{inh}} + E_R$$

$$E_T = [0.000331 + 9.627964] \text{ Mev}$$

$$E_T = 9.628295 \text{ Mev}$$

Increased energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses .So ,the increased energy (E_{inc}) of the particles are :-

1.. For beryllium -7

$$E_{inc} = \frac{m_t}{m_t + m_{Be-7}} \times E_T$$

$$E_{inc} = \frac{3.0155 \text{ amu}}{[3.0155 + 7.01473555] \text{ amu}} \times 9.628295 \text{ Mev}$$

$$E_{inc} = \frac{3.0155}{10.03023555} \times 9.628295 \text{ Mev}$$

$$E_{inc} = 0.30064099541 \times 9.628295 \text{ Mev}$$

$$E_{inc} = 2.894660 \text{ Mev}$$

2..increased energy of the triton

$$E_{inc} = [E_T] - [\text{increased energy of the Be-7}]$$

$$E_{inc} = [9.628295] - [2.894660] \text{ Mev}$$

$$E_{inc} = 6.733635 \text{ Mev}$$

6. Increased velocity of the particles .

(1) For triton

$$E_{inc} = \frac{1}{2} m_t v_{inc}^2$$

$$v_{inc} = \left[\frac{2 \times E_{inc}}{m_t} \right]^{\frac{1}{2}} = \left[\frac{2 \times 6.733635 \times 1.6 \times 10^{-13} \text{ J}}{5.0072 \times 10^{-27} \text{ kg}} \right]^{\frac{1}{2}} \text{ m/s}$$

$$= \left(\frac{21.547632 \times 10^{-13}}{5.0072 \times 10^{-27}} \right)^{\frac{1}{2}} \text{ m/s}$$

$$= \left[4.30332960536 \times 10^{14} \right]^{\frac{1}{2}} \text{ m/s}$$

$$= 2.0744 \times 10^7 \text{ m/s}$$

(2). For beryllium-7

$$v_{inc} = \left[\frac{2 \times E_{inc}}{m_{Be-7}} \right]^{\frac{1}{2}}$$

$$= \left(\frac{2 \times 2.894660 \times 1.6 \times 10^{-13} \text{ J}}{11.6479 \times 10^{-27} \text{ kg}} \right)^{\frac{1}{2}}$$

$$= \left(\frac{9.262912 \times 10^{-13}}{11.6479 \times 10^{-27}} \right)^{\frac{1}{2}} \text{ m/s}$$

$$= \left[0.79524309102 \times 10^{14} \right]^{\frac{1}{2}} \text{ m/s}$$

$$= 0.8917 \times 10^7 \text{ m/s}$$

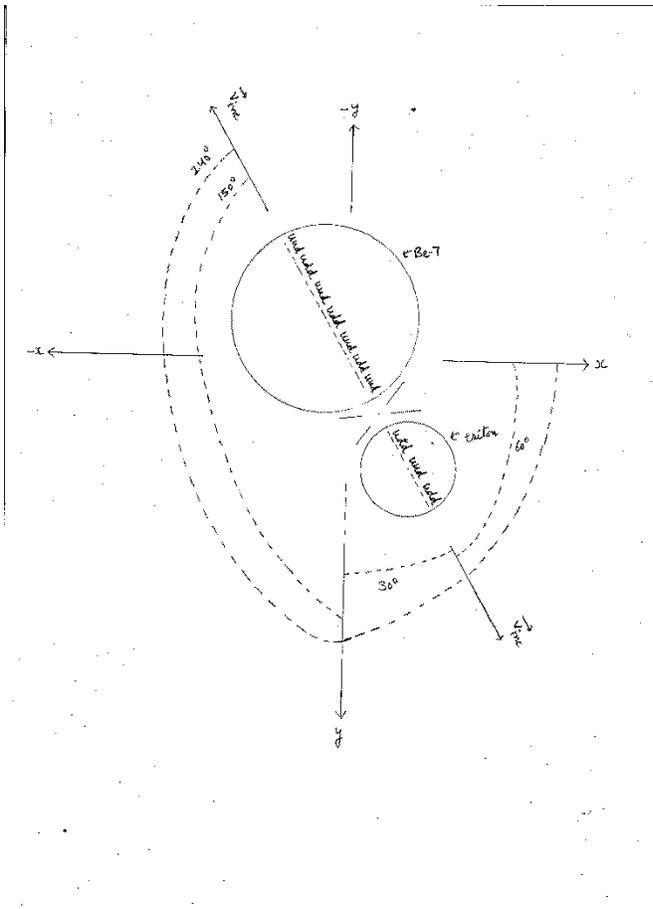
7. Angle of propulsion

1 As the reduced mass converts into energy , the total energy (E_T) propel both the particles with equal and opposite momentum.

2. We know that when there a fusion process occurs , then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus (\vec{V}_{CN}) .]

3.. At point ' F ' , as V_{CN} makes 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .

so, the triton is propelled making 60° angle with x-axis , 30° angle with y-axis and 90° angle with z-axis .
While the beryllium - 7 is propelled making 240° angle with x-axis, 150° angle with y-axis and 90° angle with z-axis .



Components of the increased velocity (V_{inc}) of the particles.

(i) For beryllium - 7

$$1. \vec{v}_x = v_{inc} \cos \alpha$$

$$v_{inc} = 0.8917 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(240) = -0.5$$

$$\vec{v}_x = 0.8917 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.4458 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_y = v_{inc} \cos \beta$$

$$\cos \beta = \cos(150) = -0.866$$

$$\vec{v}_y = 0.8917 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.7722 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_z = v_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\vec{v}_z = 0.8917 \times 10^7 \times 0$$

$$= 0 \text{ m/s}$$

(II) For triton

$$1. \vec{v}_x = v_{inc} \cos \alpha$$

$$v_{inc} = 2.0744 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\vec{v}_x = 2.0744 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 1.0372 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_y = v_{inc} \cos \beta$$

$$\cos \beta = \cos(30) = 0.866$$

$$\vec{v}_y = 2.0744 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 1.7964 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_z = v_{inc} \cos \gamma$$

$$\cos \gamma = \cos(90) = 0$$

$$\vec{v}_z = 2.0744 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9. Components of the final velocity (v_f) of the particles

IFORberyllium- 7

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) $=(\vec{v}_{inh})+(\vec{v}_{inc})$
X – axis	$\vec{v}_x = 0.1243 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.4458 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.3215 \times 10^7 \text{ m/s}$
y –axis	$\vec{v}_y = 0.2152 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.7722 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.557 \times 10^7 \text{ m/s}$
z – axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..Fortriton

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) $=(\vec{v}_{inh})+(\vec{v}_{inc})$
X –axis	$\vec{v}_x = 0.1243 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.0372 \times 10^7 \text{ m/s}$	$\vec{v}_x = 1.1615 \times 10^7 \text{ m/s}$
y– axis	$\vec{v}_y = 0.2152 \times 10^7 \text{ m/s}$	$\vec{v}_y = 1.7964 \times 10^7 \text{ m/s}$	$\vec{v}_y = 2.0116 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final velocity (v f) of theberyllium - 7

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.3215 \times 10^7 \text{ m/s}$$

$$V_y = 0.557 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (0.3215 \times 10^7)^2 + (0.557 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.10336225 \times 10^{14}) + (0.310249 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.41361125 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.6431 \times 10^7 \text{ m/s}$$

Final kinetic energy of the beryllium - 7

$$E = \frac{1}{2} m_{\text{Be-7}} V_f^2$$

$$E = \frac{1}{2} \times 11.6479 \times 10^{-27} \times 0.41361125 \times 10^{14} \text{ J}$$

$$= 2.40885123943 \times 10^{-13} \text{ J}$$

$$= 1.505532 \text{ Mev}$$

$$m_{\text{Be-7}} V_f^2 = 11.6479 \times 10^{-27} \times 0.41361125 \times 10^{14} \text{ J}$$

$$= 4.8177 \times 10^{-13} \text{ J}$$

10.. Final velocity (v_f) of the triton

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 1.1615 \times 10^7 \text{ m/s}$$

$$V_y = 2.0116 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (1.1615 \times 10^7)^2 + (2.0116 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (1.34908225 \times 10^{14}) + (4.04653456 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 5.39561681 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 2.3228 \times 10^7 \text{ m/s}$$

Final kinetic energy of the triton

$$E = \frac{1}{2} m_t V_f^2$$

$$E = \frac{1}{2} \times 5.0072 \times 10^{-27} \times 5.39561681 \times 10^{14} \text{ J}$$

$$= 13.5084662455 \times 10^{-13} \text{ J}$$

$$= 8.442791 \text{ Mev}$$

$$m_t V_f^2 = 5.0072 \times 10^{-27} \times 5.39561681 \times 10^{14} \text{ J}$$

$$= 27.0169 \times 10^{-13} \text{ J}$$

Forces acting on the beryllium - 7 nucleus

$$1 F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.3215 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 4 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 4 \times 1.6 \times 10^{-19} \times 0.3215 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 2.0596 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

so,

$$\vec{F}_y = 2.0596 \times 10^{-13} \text{ N}$$

$$2 F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 4 \times 1.6 \times 10^{-19} \times 0.3215 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N}$$

$$= 2.0602 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (+) Z-axis,

so,

$$\vec{F}_z = 2.0602 \times 10^{-13} \text{ N}$$

$$3 F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = -0.557 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

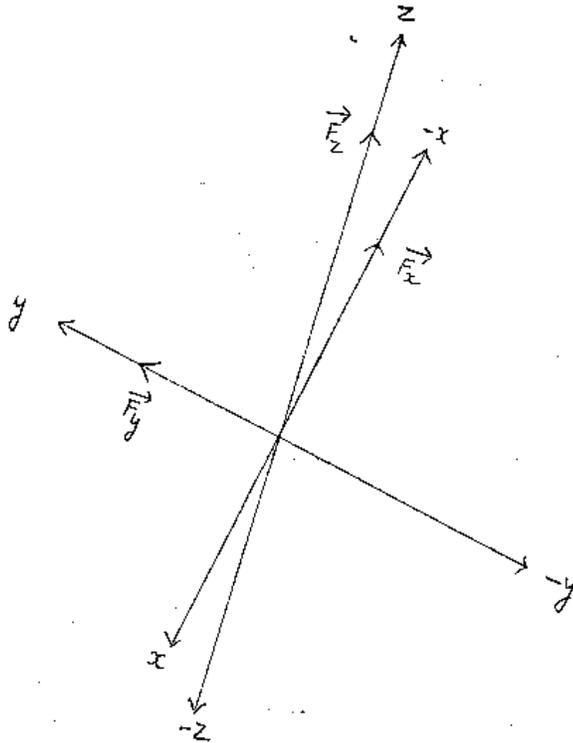
$$F_x = 4 \times 1.6 \times 10^{-19} \times 0.557 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 3.5683 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x axis,

$$\text{so, } \vec{F}_x = -3.5683 \times 10^{-13} \text{ N}$$

Forces acting on the beryllium-7



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 3.5683 \times 10^{-13} \text{ N}$$

$$F_y = 2.0596 \times 10^{-13} \text{ N}$$

$$F_z = 2.0602 \times 10^{-13} \text{ N}$$

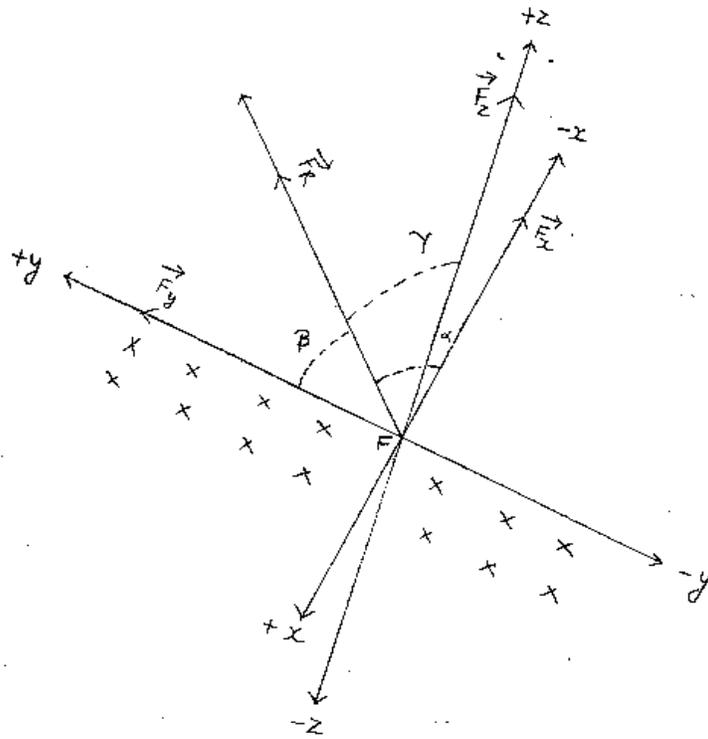
$$F_R^2 = (3.5683 \times 10^{-13})^2 + (2.0596 \times 10^{-13})^2 + (2.0602 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (12.73276489 \times 10^{-26}) + (4.24195216 \times 10^{-26}) + (4.24442404 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 21.21914109 \times 10^{-26} \text{ N}^2$$

$$F_R = 4.6064 \times 10^{-13} \text{ N}$$

Resultant force acting on the beryllium-7



Radius of the circular orbit to be followed by the beryllium - 7

$$r = \frac{mv^2}{F_R}$$

$$mv^2 = 4.8177 \times 10^{-13} \text{ J}$$

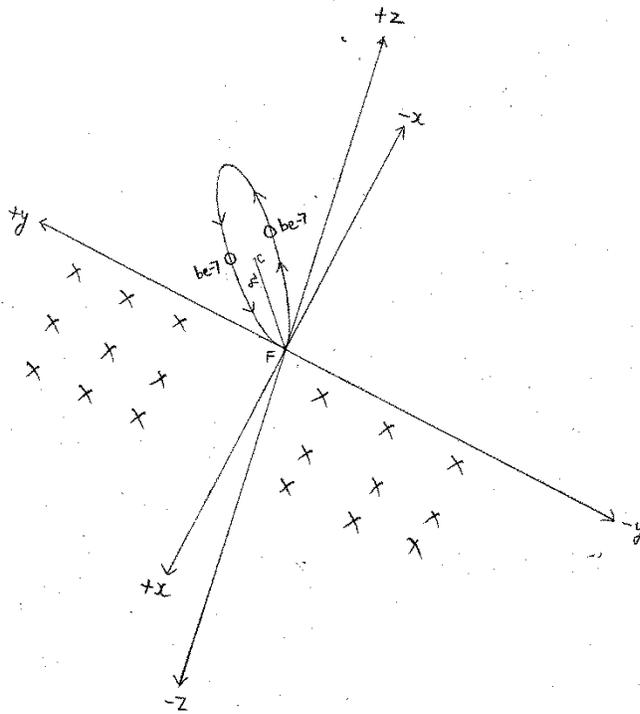
$$F_R = 4.6064 \times 10^{-13} \text{ N}$$

$$r = \frac{4.8177 \times 10^{-13} \text{ J}}{4.6064 \times 10^{-13} \text{ N}}$$

$$r = 1.0458 \text{ m}$$

The circular orbit to be followed by the beryllium - 7 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

C= center of the circular orbit to be followed by the beryllium - 7.



The plane of the circular orbit to be followed by the beryllium -7 makes angles with positive x , y and z -axes as follows :-

1 with x - axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = -3.5683 \times 10^{-13} \text{ N}$$

$$F_r = 4.6064 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7746$$

$$\alpha = 219.23 \text{ degree } [\because \cos(219.23) = -0.7746]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = 2.0596 \times 10^{-13} \text{ N}$$

$$F_r = 4.6064 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4471$$

$$\beta = 63.44 \text{ degree } [\because \cos(63.44) = 0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{\vec{F}_z}{F_r}$$

$$\vec{F}_z = 2.0602 \times 10^{-13} \text{ N}$$

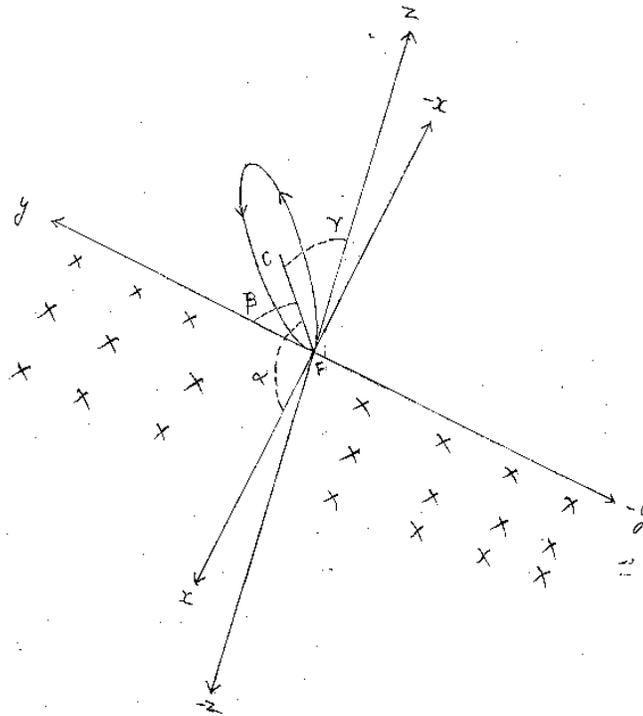
$$F_r = 4.6064 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4472$$

$$\gamma = 63.43 \text{ degree}$$

The plane of the circular orbit to be followed by the beryllium -7 makes angles with positive x, y, and z axes as follows :-



Where,

$$\alpha = 219.23 \text{ degree}$$

$$\beta = 63.44 \text{ degree}$$

$$\gamma = 63.43 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium - 7.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

d

$$d = 2 \times r$$

$$= 2 \times 1.0458 \text{ m}$$

$$= 2.0916 \text{ m}$$

$$\cos \alpha = -0.7746$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 2.0916 \times (-0.7746) \text{ m}$$

$$x_2 - x_1 = -1.6201 \text{ m}$$

$$x_2 = -1.6201 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = 0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 2.0916 \times 0.4471 \text{ m}$$

$$y_2 - y_1 = 0.9351 \text{ m}$$

$$y_2 = 0.9351 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = 0.4472$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 2.0916 \times 0.4472 \text{ m}$$

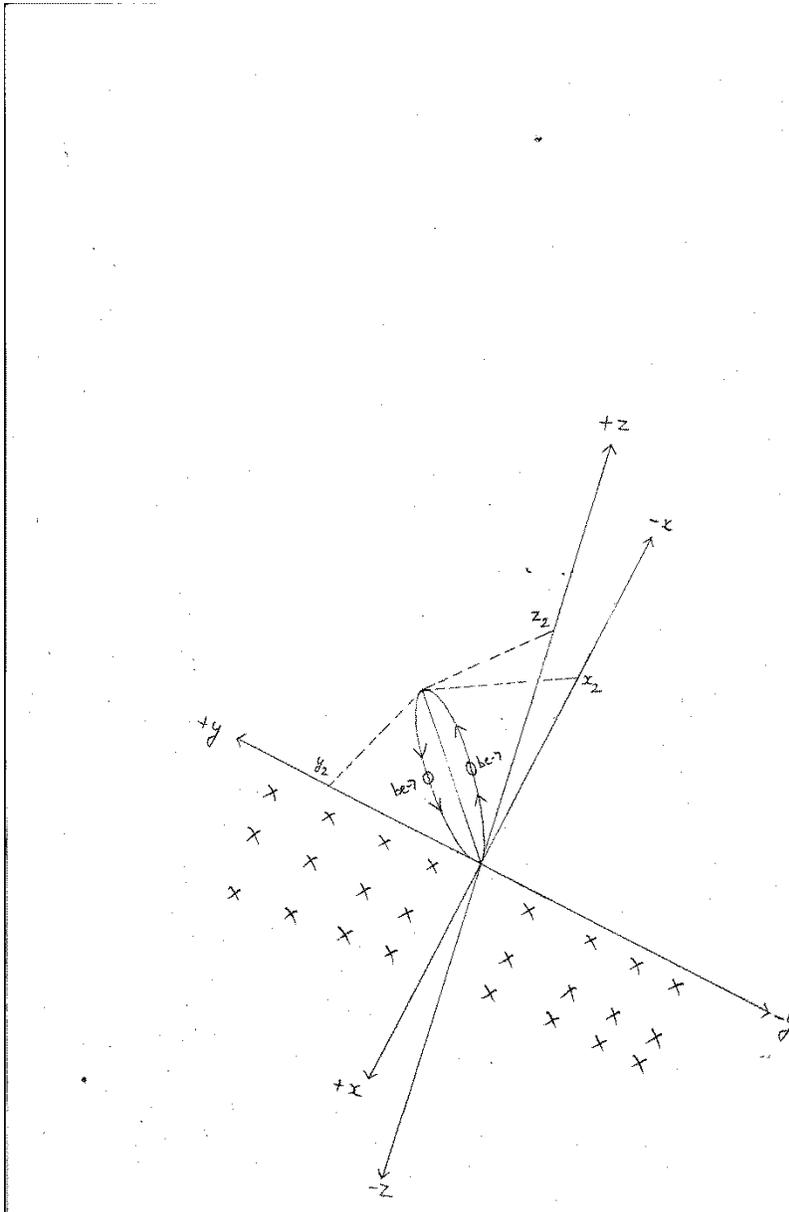
$$z_2 - z_1 = 0.9353 \text{ m}$$

$$z_2 = 0.9353 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium-7 are as shown below.

The line _____ is the diameter of the circle .

P_1P_2



Conclusion :-

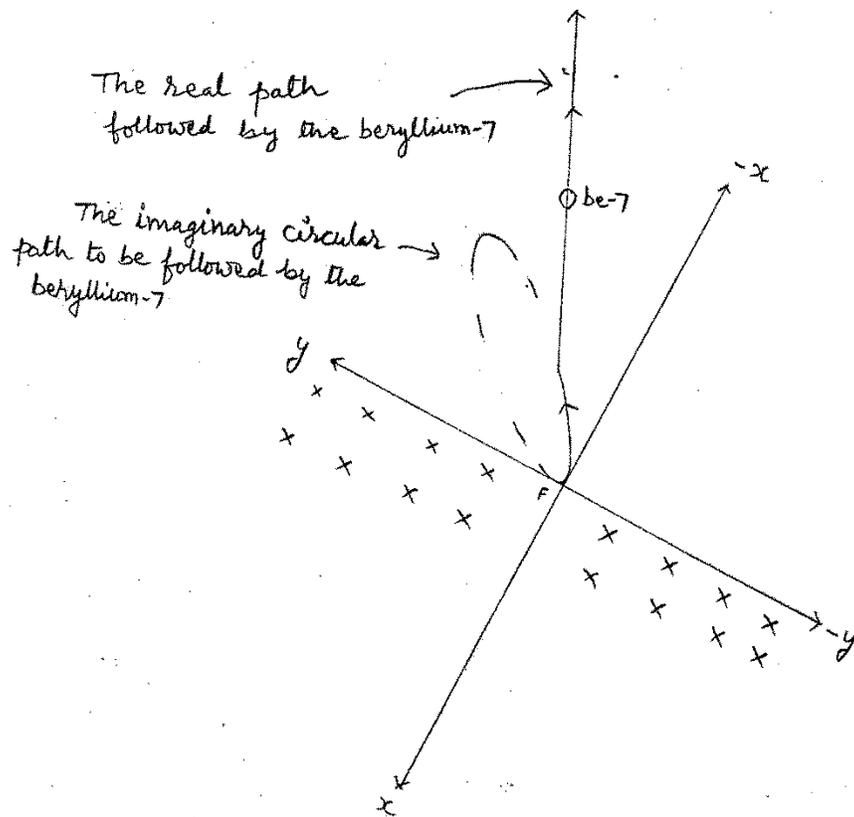
The direction components $\left[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z \right]$ of the resultant force $\left(\vec{F}_r \right)$ that are acting on the beryllium-7 nucleus are along **-x, +y and +z** axes respectively.

So by seeing the direction of the resultant force ($\vec{F_r}$) we come to know that the circular orbit to be followed by the beryllium-7 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force ($\vec{F_r}$) tends the beryllium-7 nucleus to undergo to a circular orbit of radius 1.0458 m . It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.6201 \text{ m}, 0.9351 \text{ m}, 0.9353 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the beryllium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

The beryllium-7 nucleus is not confined within into the tokamak.



Forces acting on the triton

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = 1.1615 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 1.6 \times 10^{-19} \times 1.1615 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 1.8602 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = -1.8602 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 1.6 \times 10^{-19} \times 1.1615 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N}$$

$$= 1.8608 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = -1.8608 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = 2.0116 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

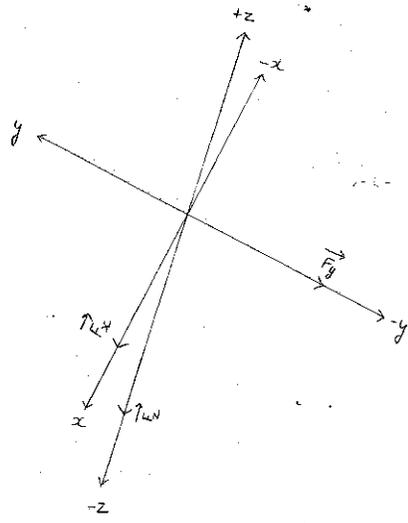
$$\sin \theta = \sin 90^\circ = 1$$

$$F_x = 1.6 \times 10^{-19} \times 2.0116 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 3.2217 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x-axis,

$$\vec{F}_x = 3.2217 \times 10^{-13} \text{ N}$$



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 3.2217 \times 10^{-13} \text{ N}$$

$$F_y = 1.8602 \times 10^{-13} \text{ N}$$

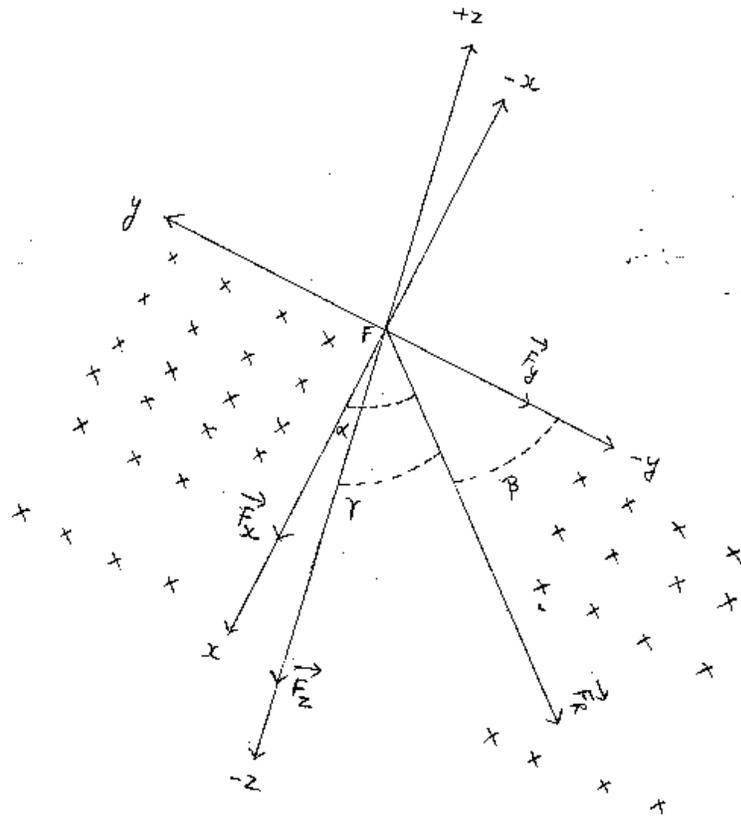
$$F_z = 1.8608 \times 10^{-13} \text{ N}$$

$$F_R^2 = (3.2217 \times 10^{-13})^2 + (1.8602 \times 10^{-13})^2 + (1.8608 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (10.37935089 \times 10^{-26}) + (3.46034404 \times 10^{-26}) + (3.46257664 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 17.30227157 \times 10^{-26} \text{ N}^2$$

$$F_R = 4.1595 \times 10^{-13} \text{ N}$$



Radius of the circular orbit to be followed by the **triton**

$$r = mv^2 / F_R$$

$$mv^2 = 27.0169 \times 10^{-13} \quad \text{J}$$

$$F_R = 4.1595 \times 10^{-13} \quad \text{N}$$

$$27.0169 \times 10^{-13} \text{J}$$

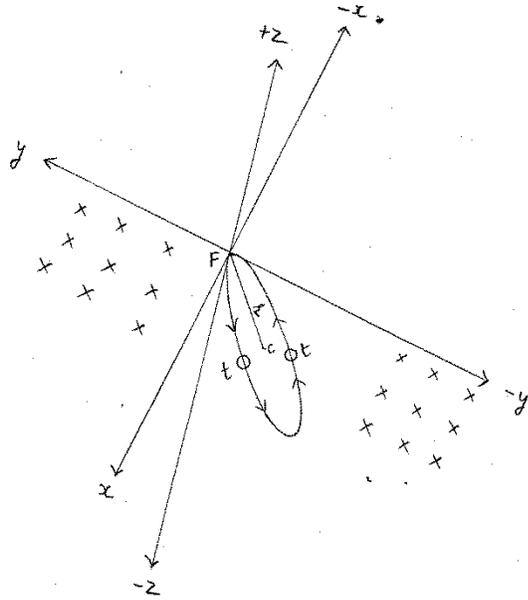
$$r = \frac{\quad}{\quad}$$

$$4.1595 \times 10^{-13} \quad \text{N}$$

$$r = 6.4952 \quad \text{m}$$

The circular orbit followed by the **triton** lies in the plane made up of positive x-axis, negative y-axis and the negative z-axis.

C = center of the circular orbit to be followed by the triton.



The plane of the circular orbit to be followed by the triton makes angles with positive x , y and z -axes as follows :-

1 with x - axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = 3.2217 \times 10^{-13} \text{ N}$$

$$F_r = 4.1595 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos () =]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = -1.8602 \times 10^{-13} \text{ N}$$

$$F_r = 4.1595 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4472$$

$$\beta = 243.43 \text{ degree } [\because \cos (243.43) = -0.4472]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{F_z}{F_r}$$

$$\frac{F_z}{F_r} = \underline{-1.8608 \times 10^{-13} \text{ N}}$$

$$F_r = 4.1595 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.44 \text{ degree}$$

The plane of the circular orbit to be followed by the triton makes angles with positive x , y , and z axes as follows :-

$$= 2 \times 6.4952 \text{ m}$$

$$= 12.9904 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 12.9904 \times 0.7745 \quad \text{m}$$

$$x_2 - x_1 = 10.0610 \text{ m}$$

$$x_2 = 10.0610 \text{ m} [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = -0.4472$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 12.9904 \times (-0.4472) \text{ m}$$

$$y_2 - y_1 = -5.8093 \text{ m}$$

$$y_2 = -5.8093 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 12.9904 \times (-0.4473) \quad \text{m}$$

$$z_2 - z_1 = -5.8106 \text{ m}$$

$$z_2 = -5.8106 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1(x_1, y_1, z_1)$ and $p_2(x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the triton are as shown below.

The line is the diameter of the circle .

P_1P_2

Conclusion :-

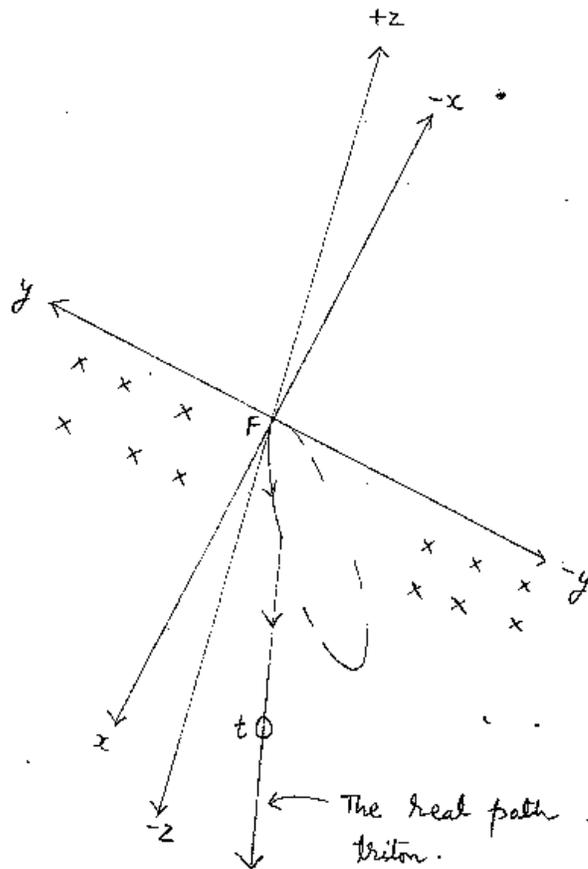
The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the triton are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the triton lies in the plane made up of positive x- axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the triton to undergo to a circular orbit of radius 6.4952 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(10.0610 \text{ m}, -5.8093 \text{ m}, -5.8106 \text{ m})$. in trying to complete its circle , due to lack of space ,it strike to the base wall of the tokamak.

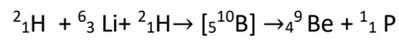
Hence the triton is not confined.



← The real path followed by the triton.

(In trying to complete the circular orbit, the produced Triton strike to the base wall of the tokamak. so, it cannot complete the circle.)

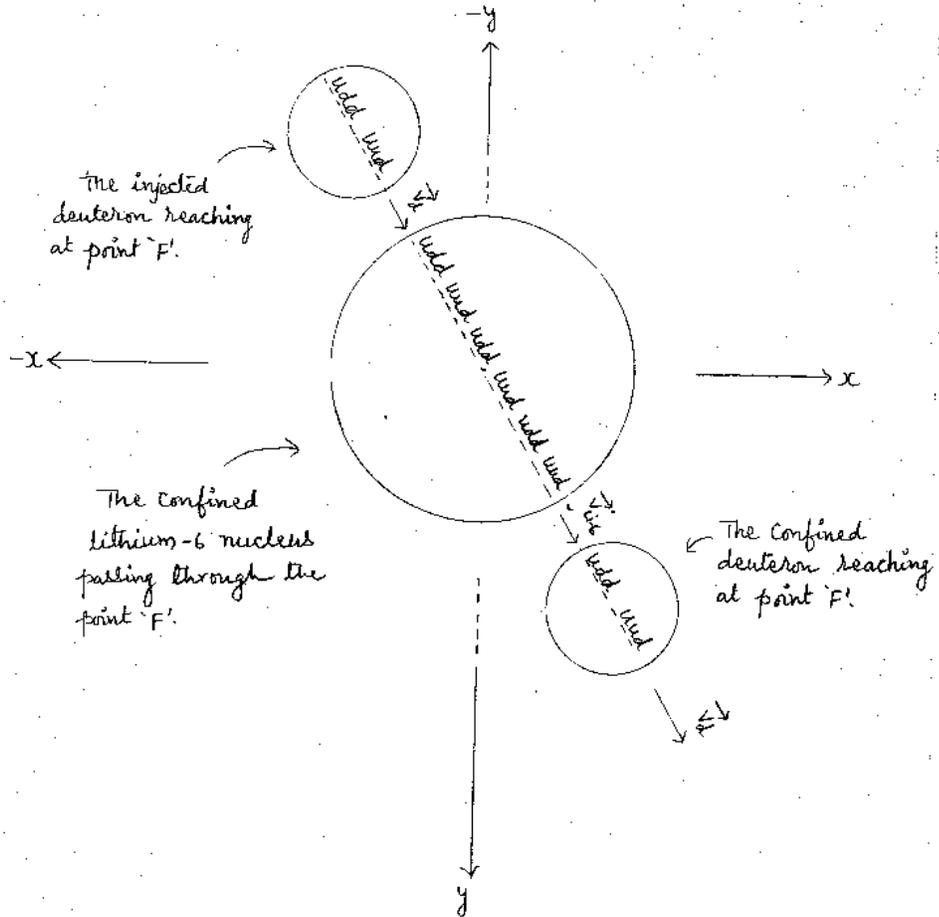
For fusion reaction



The interaction of nuclei :-

The injected deuteron reaches at point F ,and interacts [experiences a repulsive force due to the confined lithium-6 and confined deuteron] with the confined lithium-6 and confined deuteron passing through the point F . the injected deuteron overcomes the electrostatic repulsive force and – a like two solid spheres join - the injected deuteron dissimilarly joins with the confined lithium-6 and confined deuteron.

Interaction of nuclei :-

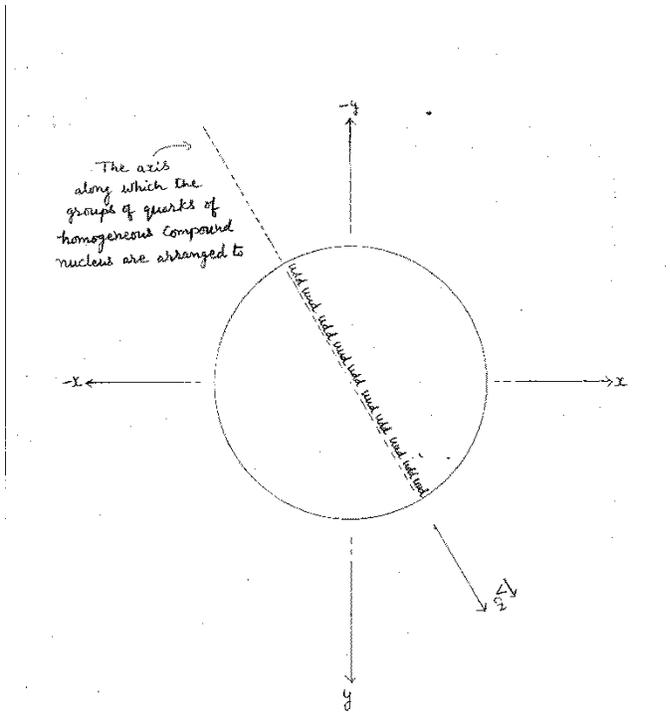


2. Formation of the homogeneous compound nucleus : -

The constituents (quarks and gluons) of the dissimilarly joined nuclei (the injected deuteron and the lithium-6 nucleus and confined deuteron) behave like a liquid and form a homogeneous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons .

Thus within the homogeneous compound nucleus – each group of quarks is surrounded by the gluons in equal proportion . so, within the homogeneous compound nucleus there are 10 groups of quarks surrounded by the gluons.

The homogenous compound nucleus



where, velocity of compound nucleus makes angles with positive x, y and z axes as follows :-

$$\alpha = 60 \text{ degrees}$$

$$\beta = 30 \text{ degrees}$$

$$\gamma = 90 \text{ degrees}$$

3 . Formation of lobes within into the homogeneous compound nucleus or the transformation of the homogenous compound nucleus into the heterogeneous compound nucleus : -

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the beryllium-9) than the reactant one (the lithium-6) includes the other six (nearby located) groups of quarks with their surrounding gluons and rearrange to form the 'A' lobe of the heterogeneous compound nucleus.

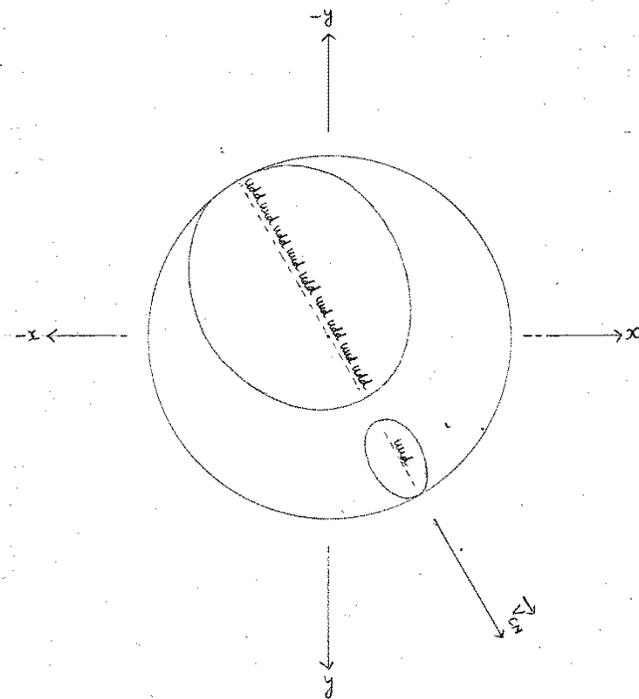
While, the remaining groups of quarks to become a stable nucleus (the proton) includes the other two (nearby located) groups of quarks with their surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe 'A'] and rearrange to form the 'B' lobe of the heterogeneous compound nucleus.

Thus, due to formation of two dissimilar lobes within into the homogeneous compound nucleus, the homogeneous compound nucleus transforms into the heterogeneous compound nucleus.

Formation of lobes

Within into the homogeneous compound nucleus the greater nucleus is the beryllium-9 nucleus and the smaller nucleus is the proton.

The greater nucleus is the lobe 'A' and the smaller nucleus is the lobe 'B' while the remaining space represent the remaining gluons.



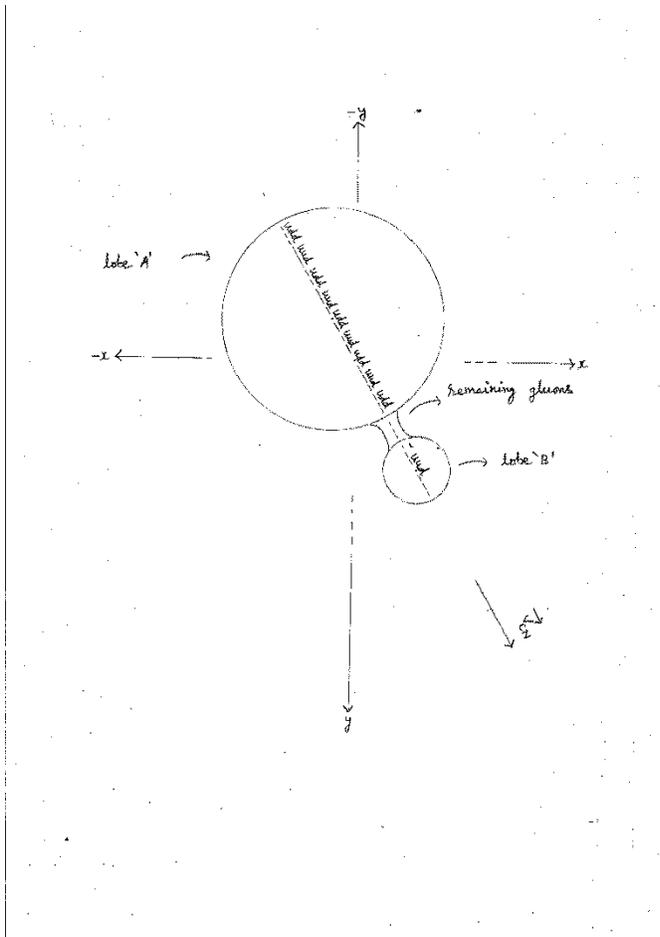
Formaton of lobes

4. Final stage of the heterogeneous compound nucleus : -

The process of formation of lobes creates void between the lobes . so, the remaining gluons (or the mass that is not involved in the formation of any lobe) rearrange to fill the voids between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogeneous compound nucleus .

Thus , the reduced mass (or the remaining gluons) keeps both the dissimilar lobes of the heterogeneous compound nucleus joined them together .

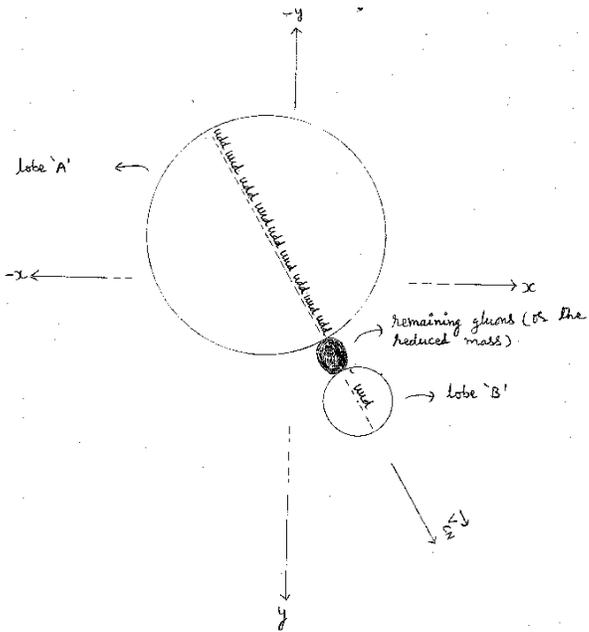
So, finally , the heterogeneous compound nucleus becomes like an abnormal digiteight or becomes as a dumbbell.



The heterogenous compound nucleus

For $\alpha = 60$ degree

$\beta = 30$ degree



Final stage of the heterogeneous compound nucleus

where, $\alpha = 60$ degree

$\beta = 30$ degree

Formation of compound nucleus :

Each deuteron has to overcome the the electrostatic repulsive force exerted by the lithion-6 as well as by other deuteron to form a compund nucleus .

(1)Just before fusion, to overcome the electrostatic repulsive force exerted by the lithion-6 , the deuteron of n^{th} bunch loses (radiates its energy in the form of eletromagnetic waves its energy equal to 45.5598 kev.

Just before fusion, to overcome the electrostatic repulsive force exerted by the confined deuteron , the deuteron of n^{th} bunch loses (radiates its energy in the form of eletromagnetic waves its energy equal to 5.0622 kev.

so, just before fusion, the total loss in kinetic energy of the deuteron is --

$$E_{\text{loss}} = (5.0622 + 45.5598) \text{ kev} \\ = 50.622 \text{ Kev}$$

so, just before fusion the kinetic energy of deuteron is –

$$E_b = E_{\text{injected}} - E_{\text{loss}} \\ E_b = 153.6 \text{ kev} - 50.622 \text{ kev} \\ = 102.978 \text{ kev} \\ = 0.102978 \text{ Mev}$$

(2)just before fusion lithion – 6 opposes each deuteron with 136.0700 kev

as there are two deuterons so Just before fusion, to overcome the electrostatic repulsive force exerted by the each deuteron, the lithion-6 loses (radiates its energy in the form of eletromagnetic waves) its energy equal to 272.14 kev.

so, just before fusion,

the kinetic energy of lithion -6 is –

$$E_b = E_{\text{confined}} - E_{\text{loss}} \\ E_b = 388.2043 \text{ kev} - 272.14 \text{ kev} \\ = 116.0643 \text{ kev} \\ = 0.1160643 \text{ Mev}$$

Kinetic energy of the compound nucleus

$$\text{K.E.} = [E_b \text{ of injected deuteron}] + [E_b \text{ of lithium-6}] + [E_b \text{ of confined deuteron}]$$

$$= [102.978 \text{ Kev}] + [116.0643 \text{ Kev}] + [102.978 \text{ Kev}]$$

$$= 322.0203 \text{ Kev.}$$

$$= 0.3220203 \text{ Mev}$$

$$M = m_d + m_{\text{Li-6}} + m_d$$

$$= [3.3434 \times 10^{-27} \text{ Kg}] + [9.9853 \times 10^{-27} \text{ Kg}] + [3.3434 \times 10^{-27} \text{ Kg}]$$

$$= 16.6721 \times 10^{-27} \text{ Kg}$$

Velocity of compound nucleus

$$\text{K.E.} = \frac{1}{2} M V_{\text{CN}}^2 = 0.3220203 \text{ mev}$$

$$V_{\text{CN}} = \left(\frac{2 \times 0.3220203 \times 1.6 \times 10^{-13} \text{ }^{\frac{1}{2}}}{16.6721 \times 10^{-27} \text{ kg}} \right) \text{ m/s}$$

$$V_{\text{CN}} = \frac{1.03046496 \times 10^{-13} \text{ }^{\frac{1}{2}}}{16.6721 \times 10^{-27}} \text{ m/s}$$

$$V_{\text{CN}} = [0.06180774827 \times 10^{14}]^{\frac{1}{2}} \text{ m/s}$$

$$V_{\text{CN}} = 0.2486 \times 10^7 \text{ m/s}$$

Components of velocity of compound nucleus

$$(1) \vec{V}_x = V_{\text{CN}} \cos \alpha$$

$$= 0.2486 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 0.1243 \times 10^7 \text{ m/s}$$

$$(2) \vec{V}_y = V_{\text{CN}} \cos \beta$$

$$= 0.2486 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 0.2152 \text{ m/s}$$

$$(3) \vec{V}_Z = V_{CN} \cos \gamma$$

$$= 0.2486 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

The splitting of the heterogeneous compound nucleus : -

The heterogeneous compound nucleus , due to its instability , splits according to the lines perpendicular to the direction of the velocity of the compound nucleus (\vec{V}_{cn}) into the three particles –**beryllium-9**, the proton and the reduced mass (Δm) .

Out of them , the two particles (the **beryllium-9** and the proton) are stable while the third one (reduced mass) is unstable .

According to the law of inertia, each particle that is produced due to splitting of the compound nucleus , has an inherited velocity (\vec{V}_{inh}) equal to the velocity of the compound nucleus (\vec{V}_{cn}).

So, for conservation of momentum

$$M\vec{V}_{cn} = (m_{Be-9} + \Delta m + m_p)\vec{V}_{cn}$$

Where ,

M = mass of the compound nucleus
 \vec{V}_{cn} = velocity of the compound nucleus

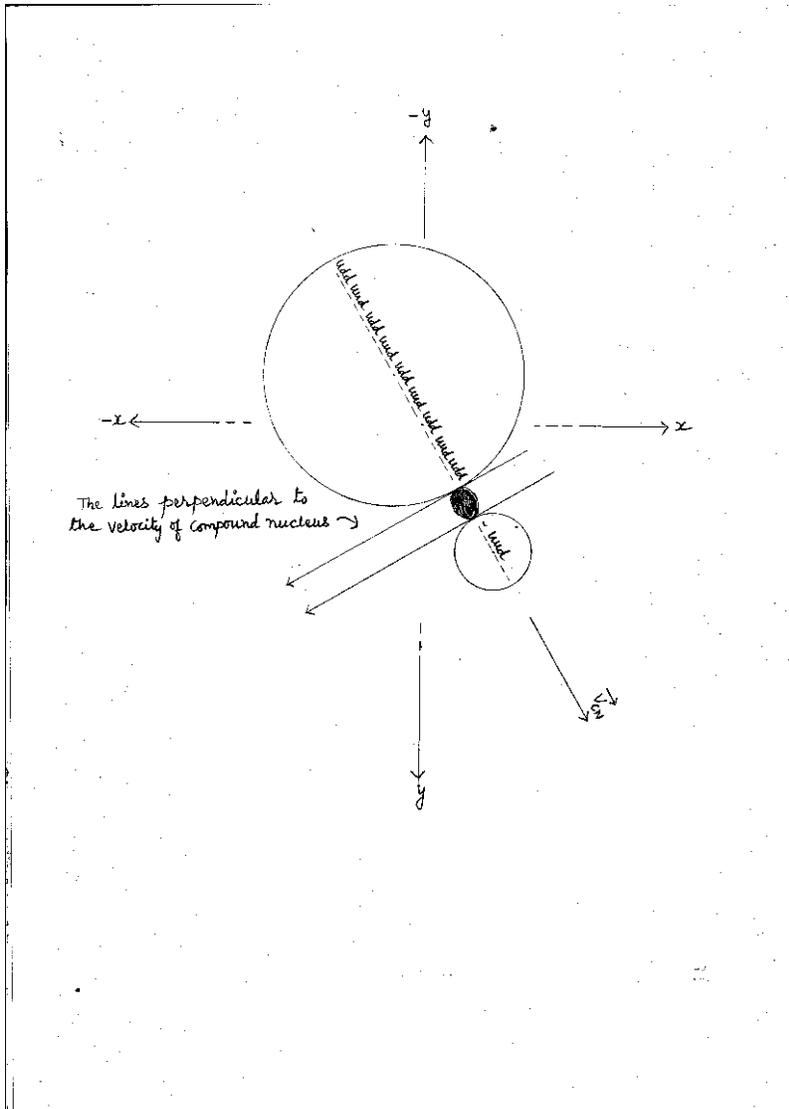
m_{Be-9} = mass of the **beryllium-9**

m_p = mass of the proton

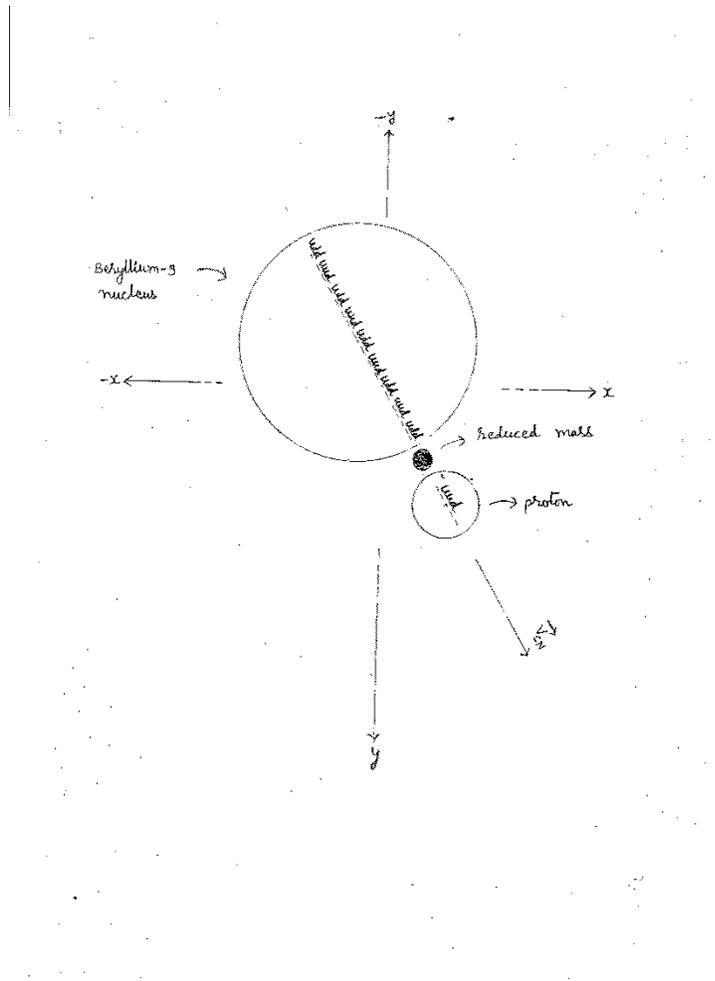
Δm = reduced mass

The splitting of the heterogeneous compound nucleus

The heterogeneous compound nucleus to show the lines perpendicular to the \vec{v}_{cn}



The splitting of the heterogenous compound nucleus



Inherited velocity of the particles (s) : -

Each particles hasinherited velocity (\vec{v}_{inh}) equal to the velocity of the compound nucleus(\vec{v}_{cn}) .

(I) . Inherited velocity of the particle Beryllium-9

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Components of the inherited velocity of the particle Beryllium-9

$$1. \vec{v}_{V_x} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1243 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_{V_y} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2152 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_{V_z} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(II). Inherited velocity of the proton

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Componentsoftheinherited velocityof the proton

$$1. \vec{v}_{V_x} = V_{inh} \cos \alpha = V_{CN} \cos \alpha = 0.1243 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_{V_y} = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.2152 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_{V_z} = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

(iii) Inherited velocity of the reduced mass

$$V_{inh} = V_{CN} = 0.2486 \times 10^7 \text{ m/s}$$

Propulsion of the particles

Reduced mass converts into enrgy and total energy (E_T) propel both the particles with equal and opposite momentum.

Reduced mass

$$\Delta m = [m_d + m_{Li-6} + m_d] - [m_{Be-9} + m_p]$$

$$\Delta m = [2.01355 + 6.01347708 + 2.01355] - [9.00998792 + 1.007276] \text{ amu}$$

$$\Delta m = [10.04057708] - [10.01726392] \text{ amu}$$

$$\Delta m = 0.02331316 \text{ amu}$$

$$\Delta m = 0.02331316 \times 1.6605 \times 10^{-27} \text{ kg}$$

The Inherited kinetic energy of reduced mass (Δm) .

$$E_{inh} = \frac{1}{2} \Delta m V_{CN}^2$$

$$\Delta m = 0.02331316 \times 1.6605 \times 10^{-27} \text{ kg}$$

$$V_{CN}^2 = 0.06180774827 \times 10^{14}$$

$$E_{inh} = \frac{1}{2} \times 0.02331316 \times 1.6605 \times 10^{-27} \times 0.06180774827 \times 10^{14} \text{ J}$$

$$E_{inh} = 0.00119633539 \times 10^{-13} \text{ J}$$

$$E_{inh} = 0.000747 \text{ Mev}$$

Released energy (E_R)

$$E_R = \Delta m c^2$$

$$E_R = 0.02331316 \times 931 \text{ Mev}$$

$$E_R = 21.704551 \text{ Mev}$$

Total energy (E_T)

$$E_T = E_{inh} + E_R$$

$$E_T = [0.000747 + 21.704551] \text{ Mev}$$

$$E_T = 21.705298 \text{ Mev}$$

Increased energy of the particles (s) :-

The total energy (E_T) is divided between the particles in inverse proportion to their masses. So, the increased energy (E_{inc}) of the particles are :-

1. For beryllium -9

$$E_{inc} = \frac{m_p}{m_p + m_{Be-9}} \times E_T$$

$$E_{inc} = \frac{1.007276 \text{ amu}}{[1.007276 + 9.0098792] \text{ amu}} \times 21.705298 \text{ Mev}$$

$$E_{inc} = \frac{1.007276}{10.01726392} \times 21.705298 \text{ Mev}$$

$$E_{inc} = 0.10055400437 \times 21.705298 \text{ Mev}$$

$$E_{inc} = 2.182554 \text{ Mev}$$

2. increased energy of the proton

$$E_{inc} = [E_T] - [\text{increased energy of the Be-9}]$$

$$E_{inc} = [21.705298] - [2.182554] \text{ Mev}$$

$$E_{inc} = 19.522744 \text{ Mev}$$

6. Increased velocity of the particles .

(1) For proton

$$E_{inc} = \frac{1}{2} m_p v_{inc}^2$$

$$\begin{aligned} v_{inc} &= [2 \times E_{inc} / m_p]^{\frac{1}{2}} \\ &= \left[\frac{2 \times 19.522744 \times 1.6 \times 10^{-13} \text{ J}}{1.6726 \times 10^{-27} \text{ kg}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= \left[\frac{62.4727808 \times 10^{-13}}{1.6726 \times 10^{-27}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= [37.350699988 \times 10^{14}]^{\frac{1}{2}} \text{ m/s} \\ &= 6.1115 \times 10^7 \text{ m/s} \end{aligned}$$

(2) For beryllium-9

$$\begin{aligned} v_{inc} &= [2 \times E_{inc} / m_{Be-9}]^{\frac{1}{2}} \\ &= \left[\frac{2 \times 2.182554 \times 1.6 \times 10^{-13} \text{ J}}{14.9610 \times 10^{-27} \text{ kg}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= \left[\frac{6.9841728 \times 10^{-13}}{14.9610 \times 10^{-27}} \right]^{\frac{1}{2}} \text{ m/s} \\ &= [0.46682526569 \times 10^{14}]^{\frac{1}{2}} \text{ m/s} \\ &= 0.6832 \times 10^7 \text{ m/s} \end{aligned}$$

7. Angle of propulsion

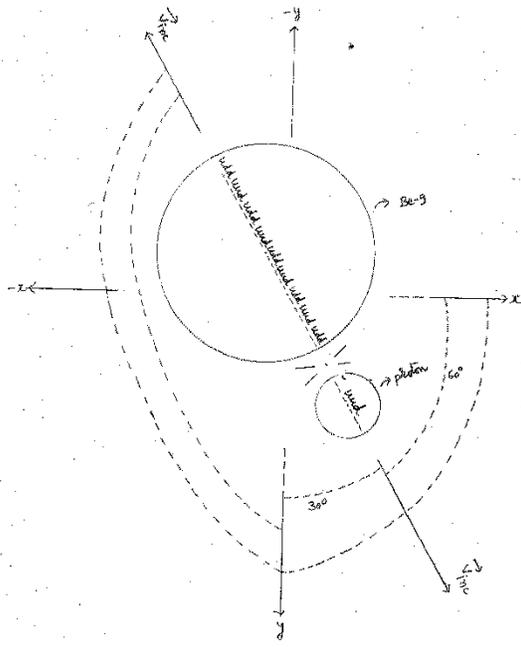
1. As the reduced mass converts into energy, the total energy (E_T) propels both the particles with equal and opposite momentum.

2. We know that when there is a fusion process, then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus (\vec{V}_{CN})].

3. At point 'F', as V_{CN} makes 60° angle with x-axis, 30° angle with y-axis and 90° angle with z-axis.

so, the proton is propelled making 60° angle with x-axis, 30° angle with y-axis and 90° angle with z-axis. While the beryllium - 9 is propelled making 240° angle with x-axis, 150° angle with y-axis and 90° angle with z-axis.

Propulsion of the particles



Components of the increased velocity (V_{inc}) of the particles.

(i) For beryllium - 9

$$1. \vec{v}_x = v_{inc} \cos \alpha$$

$$v_{inc} = 0.6832 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(240) = -0.5$$

$$\vec{v}_x = 0.6832 \times 10^7 \times (-0.5) \text{ m/s}$$

$$= -0.3416 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_y = v_{inc} \cos \beta$$

$$\cos \beta = \cos(150) = -0.866$$

$$\vec{v}_y = 0.6832 \times 10^7 \times (-0.866) \text{ m/s}$$

$$= -0.5916 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_z = v_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\vec{v}_z = 0.6832 \times 10^7 \times 0$$

$$= 0 \text{ m/s}$$

(ii) For proton

$$1. \vec{v}_x = v_{inc} \cos \alpha$$

$$v_{inc} = 6.1115 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \cos(60) = 0.5$$

$$\vec{v}_x = 6.1115 \times 10^7 \times 0.5 \text{ m/s}$$

$$= 3.0557 \times 10^7 \text{ m/s}$$

$$2. \vec{v}_y = v_{inc} \cos \beta$$

$$\cos \beta = \cos(30) = 0.866$$

$$\vec{v}_y = 6.1115 \times 10^7 \times 0.866 \text{ m/s}$$

$$= 5.2925 \times 10^7 \text{ m/s}$$

$$3. \vec{v}_z = v_{inc} \cos \gamma$$

$$\cos \gamma = \cos(90) = 0$$

$$\vec{v}_z = 6.1115 \times 10^7 \times 0 \text{ m/s}$$

$$= 0 \text{ m/s}$$

9.. Components of the final velocity (v_f) of the particles

IForberyllium- 9

According to-	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f) $=(\vec{v}_{inh})+(\vec{v}_{inc})$
X – axis	$\vec{v}_x = 0.1243 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.3416 \times 10^7 \text{ m/s}$	$\vec{v}_x = -0.2173 \times 10^7 \text{ m/s}$
y –axis	$\vec{v}_y = 0.2152 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.5916 \times 10^7 \text{ m/s}$	$\vec{v}_y = -0.3764 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

2..Forproton

According to -	Inherited Velocity(\vec{v}_{inh})	Increased Velocity(\vec{v}_{inc})	Final velocity (\vec{v}_f)= $(\vec{v}_{inh})+(\vec{v}_{inc})$
X– axis	$\vec{v}_x = 0.1243 \times 10^7 \text{ m/s}$	$\vec{v}_x = 3.0557 \times 10^7 \text{ m/s}$	$\vec{v}_x = 3.18 \times 10^7 \text{ m/s}$
y– axis	$\vec{v}_y = 0.2152 \times 10^7 \text{ m/s}$	$\vec{v}_y = 5.2925 \times 10^7 \text{ m/s}$	$\vec{v}_y = 5.5077 \times 10^7 \text{ m/s}$
z –axis	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$	$\vec{v}_z = 0 \text{ m/s}$

10.. Final velocity (vf) of the beryllium - 9

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 0.2173 \times 10^7 \text{ m/s}$$

$$V_y = 0.3764 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V^2 = (0.2173 \times 10^7)^2 + (0.3764 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (0.04721929 \times 10^{14}) + (0.14167696 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 0.18889625 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 0.4346 \times 10^7 \text{ m/s}$$

Final kinetic energy of the beryllium - 9

$$E = \frac{1}{2} m_{\text{Be-9}} V_f^2$$

$$E = \frac{1}{2} \times 14.9610 \times 10^{-27} \times 0.18889625 \times 10^{14} \text{ J}$$

$$= 1.41303839812 \times 10^{-13} \text{ J}$$

$$= 0.883148 \text{ MeV}$$

$$m_{\text{Be-9}} V_f^2 = 14.9610 \times 10^{-27} \times 0.18889625 \times 10^{14} \text{ J}$$

$$= 2.8260 \times 10^{-13} \text{ J}$$

10.. Final velocity (vf) of the proton

$$V^2 = V_x^2 + V_y^2 + V_z^2$$

$$V_x = 3.18 \times 10^7 \text{ m/s}$$

$$V_y = 5.5077 \times 10^7 \text{ m/s}$$

$$V_z = 0 \text{ m/s}$$

$$V_f^2 = (3.18 \times 10^7)^2 + (5.5077 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$V_f^2 = (10.1124 \times 10^{14}) + (30.33475929 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_f^2 = 40.44715929 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$V_f = 6.3598 \times 10^7 \text{ m/s}$$

Final kinetic energy of the proton

$$E = \frac{1}{2} m_p V_f^2$$

$$E = \frac{1}{2} \times 1.6726 \times 10^{-27} \times 40.44715929 \times 10^{14} \text{ J}$$

$$= 33.8259593142 \times 10^{-13} \text{ J}$$

$$= 21.141224 \text{ MeV}$$

$$m_p v_f^2 = 1.6726 \times 10^{-27} \times 40.44715929 \times 10^{14} \text{ J}$$

$$= 67.6519 \times 10^{-13} \text{ J}$$

Forces acting on the beryllium – 9 nucleus

$$1 \quad F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = -0.2173 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$q = 4 \times 1.6 \times 10^{-19} \text{ C}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 4 \times 1.6 \times 10^{-19} \times 0.2173 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 1.3921 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_y is according to (+) y-axis,

so,

$$\vec{F}_y = 1.3921 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_z = 4 \times 1.6 \times 10^{-19} \times 0.2173 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \quad \text{N}$$

$$= 1.3925 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_z is according to (+) Z- axis,

so,

$$\vec{F}_z = 1.3925 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{v}_y = -0.3764 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

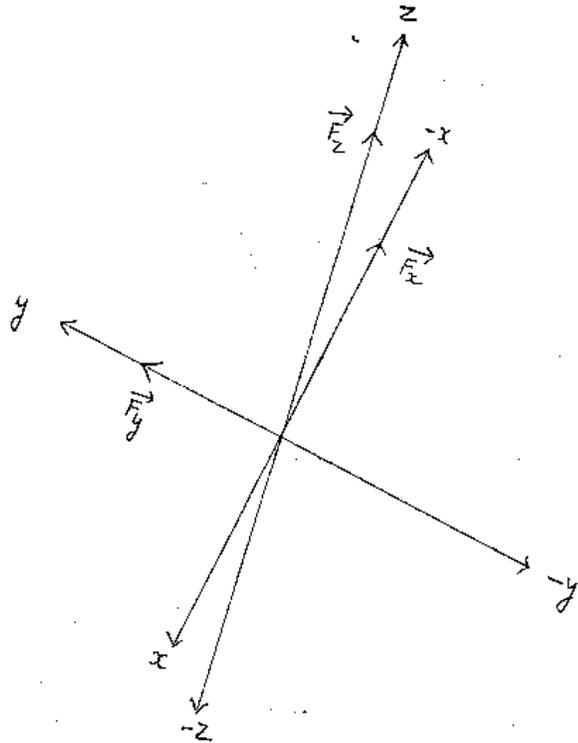
$$F_x = 4 \times 1.6 \times 10^{-19} \times 0.3764 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 2.4113 \times 10^{-13} \text{ N}$$

From the right hand palm rule, the direction of the force \vec{F}_x is according to (-) x axis,

$$\text{so, } \vec{F}_x = -2.4113 \times 10^{-13} \text{ N}$$

Forces acting on the beryllium-9



Resultant force (F_R) :

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 2.4113 \times 10^{-13} \text{ N}$$

$$F_y = 1.3921 \times 10^{-13} \text{ N}$$

$$F_z = 1.3925 \times 10^{-13} \text{ N}$$

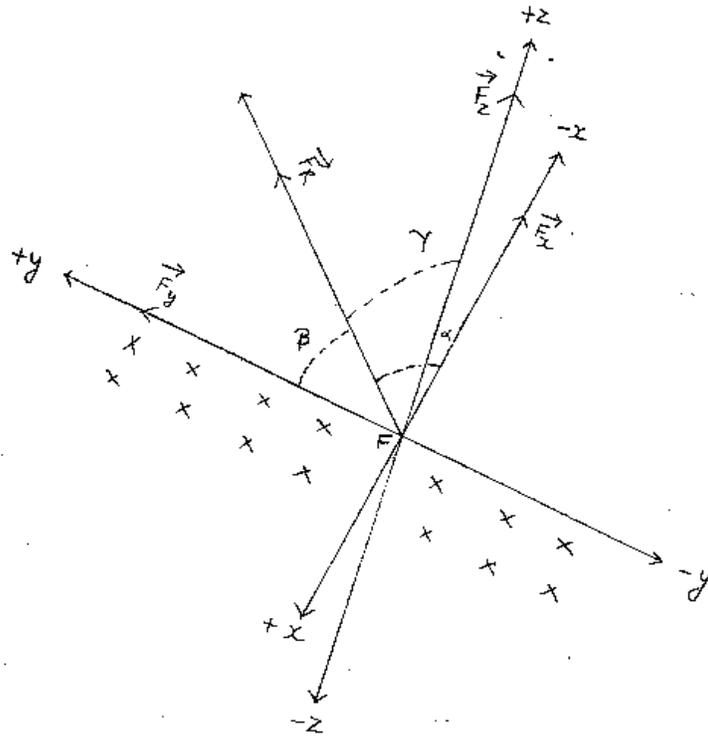
$$F_R^2 = (2.4113 \times 10^{-13})^2 + (1.3921 \times 10^{-13})^2 + (1.3925 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (5.81436769 \times 10^{-26}) + (1.93794241 \times 10^{-26}) + (1.93905625 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 9.69136635 \times 10^{-26} \text{ N}^2$$

$$F_R = 3.1130 \times 10^{-13} \text{ N}$$

Resultant force acting on the beryllium-9



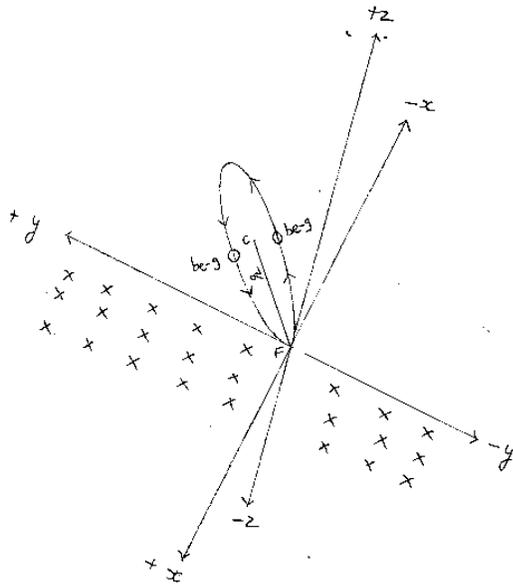
Radius of the circular orbit to be followed by the beryllium - 9

$$r = mv^2 / F_R$$
$$mv^2 = 2.8260 \times 10^{-13} \text{ J}$$
$$F_r = 3.1130 \times 10^{-13} \text{ N}$$
$$r = \frac{2.8260 \times 10^{-13} \text{ J}}{3.1130 \times 10^{-13} \text{ N}}$$

$$r = 0.9078 \text{ m}$$

The circular orbit to be followed by the beryllium - 9 lies in the plane made up of negative x-axis, positive y-axis and the positive z-axis.

C= center of the circular orbit to be followed by the beryllium - 9.



The plane of the circular orbit to be followed by the beryllium -9 makes angles with positive x, y and z-axes as follows:-

1 with x- axis

$$\cos \alpha = \frac{F_x}{F_r} = \frac{F_x}{F_r}$$

$$\frac{F_x}{F_r} = -2.4113 \times 10^{-13} \text{ N}$$

$$F_r = 3.1130 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = -0.7745$$

$$\alpha = 219.24 \text{ degree } [\because \cos (219.24) = -0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_y}{F_r} = \frac{F_y}{F_r}$$

$$\frac{F_y}{F_r} = 1.3921 \times 10^{-13} \text{ N}$$

$$F_r = 3.1130 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = 0.4471$$

$$\beta = 63.44 \text{ degree } [\because \cos (63.44) = 0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_z}{F_r} = \frac{F_z}{F_r}$$

$$\frac{F_z}{F_r} = \underline{1.3925 \times 10^{-13} \text{ N}}$$

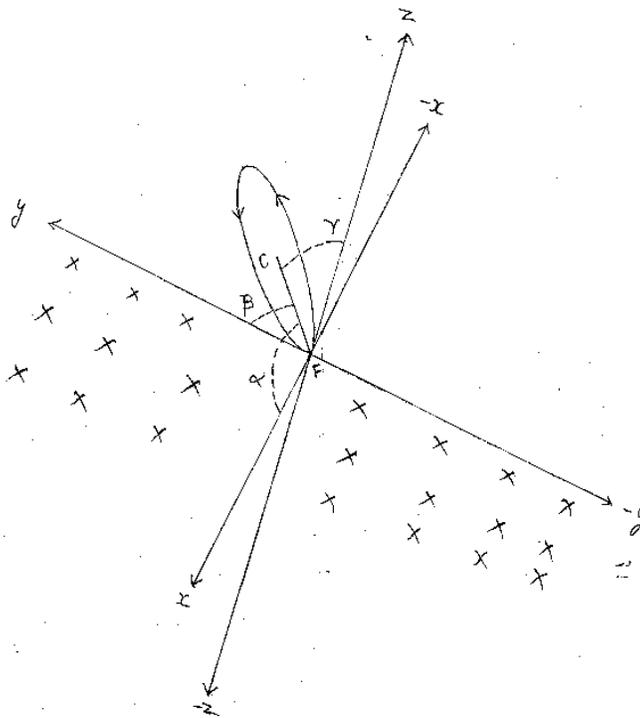
$$F_r = 3.1130 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = 0.4473$$

$$\gamma = 63.425 \text{ degree}$$

The Plane of the circular orbit to be followed by the beryllium -9 makes angles with positive x , y , and z axes as follows :-



Where,

$$\alpha = 219.24 \text{ degree}$$

$$\beta = 63.44 \text{ degree}$$

$$\gamma = 63.425 \text{ degree}$$

The cartesian coordinates of the points $P_1(x_1, y_1, z_1)$ and $P_2(x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium - 9.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$= 2 \times 0.9078 \text{ m}$$

$$d = 2 \times r$$

$$= 1.8156 \text{ m}$$

$$\cos \alpha = -0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 1.8156 \times (-0.7745) \quad \text{m}$$

$$x_2 - x_1 = -1.4061 \text{ m}$$

$$x_2 = -1.4061 \text{ m} \quad [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = 0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 1.8156 \times 0.4471 \text{ m}$$

$$y_2 - y_1 = 0.8117 \text{ m}$$

$$y_2 = 0.8117 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = 0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 1.8156 \times 0.4473 \quad \text{m}$$

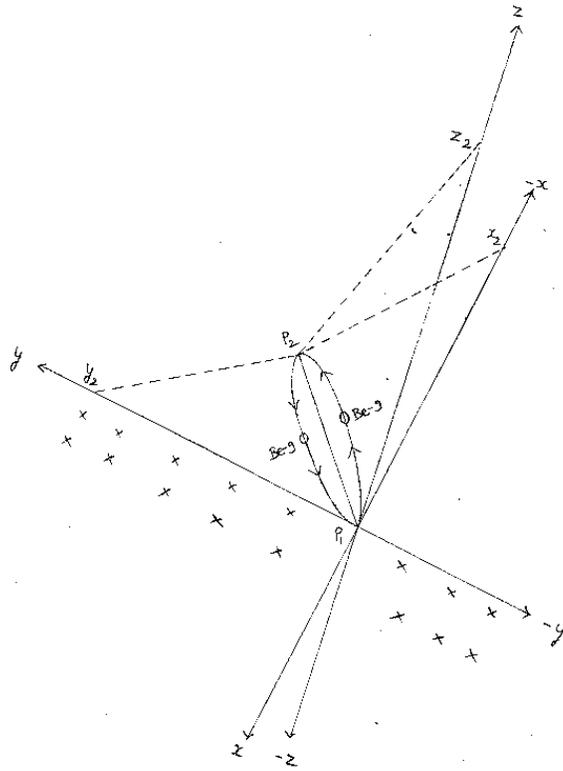
$$z_2 - z_1 = 0.8121 \text{ m}$$

$$z_2 = 0.8121 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the beryllium-9 are as shown below.

The line ____ is the diameter of the circle .

P_1P_2



Conclusion :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the beryllium-9 nucleus are along **-x, +y and +z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the beryllium -9 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-9 nucleus to undergo to a circular orbit of radius 0.9078 m . It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.4061\text{m}, 0.8117 \text{ m}, 0.8121 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the beryllium-9 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

The beryllium-9 nucleus is not confined within into the tokamak.

Forces acting on the proton

$$1 F_y = q V_x B_z \sin \theta$$

$$\vec{V}_x = 3.18 \times 10^7 \text{ m/s}$$

$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Te}$$

$$q = 1.6 \times 10^{-19} \text{ c}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$F_y = 1.6 \times 10^{-19} \times 3.18 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N}$$

$$= 5.0930 \times 10^{-13} \text{ N}$$

Form the right hand palm rule, the direction of the force \vec{F}_y is according to (-) y-axis,

so,

$$\vec{F}_y = -5.0930 \times 10^{-13} \text{ N}$$

$$2 \quad F_z = q V_x B_y \sin \theta$$

$$\vec{B}_y = 1.0013 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_z &= 1.6 \times 10^{-19} \times 3.18 \times 10^7 \times 1.0013 \times 10^{-1} \times 1 \text{ N} \\ &= 5.0946 \times 10^{-13} \text{ N} \end{aligned}$$

Form the right hand palm rule, the direction of the force \vec{F}_z is according to (-) Z-axis,

so,

$$\vec{F}_z = -5.0946 \times 10^{-13} \text{ N}$$

$$3 \quad F_x = q V_y B_z \sin \theta$$

$$\vec{V}_y = 5.5077 \times 10^7 \text{ m/s}$$

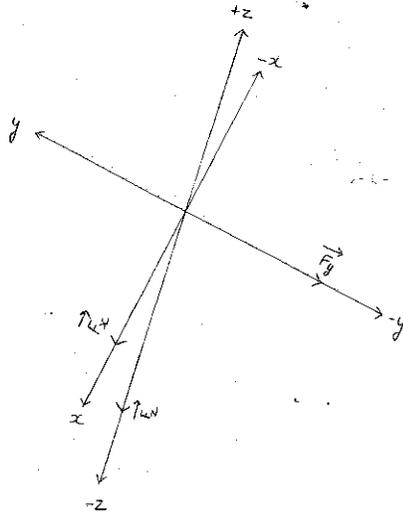
$$\vec{B}_z = -1.001 \times 10^{-1} \text{ Tesla}$$

$$\sin \theta = \sin 90^\circ = 1$$

$$\begin{aligned} F_x &= 1.6 \times 10^{-19} \times 5.5077 \times 10^7 \times 1.001 \times 10^{-1} \times 1 \text{ N} \\ &= 8.8211 \times 10^{-13} \text{ N} \end{aligned}$$

Form the right hand palm rule, the direction of the force \vec{F}_x is according to (+) x-axis,

$$SO, \vec{F}_x = 8.8211 \times 10^{-13} \text{N}$$



Resultant force (F_R):

$$F_R^2 = F_x^2 + F_y^2 + F_z^2$$

$$F_x = 8.8211 \times 10^{-13} \text{ N}$$

$$F_y = 5.0930 \times 10^{-13} \text{ N}$$

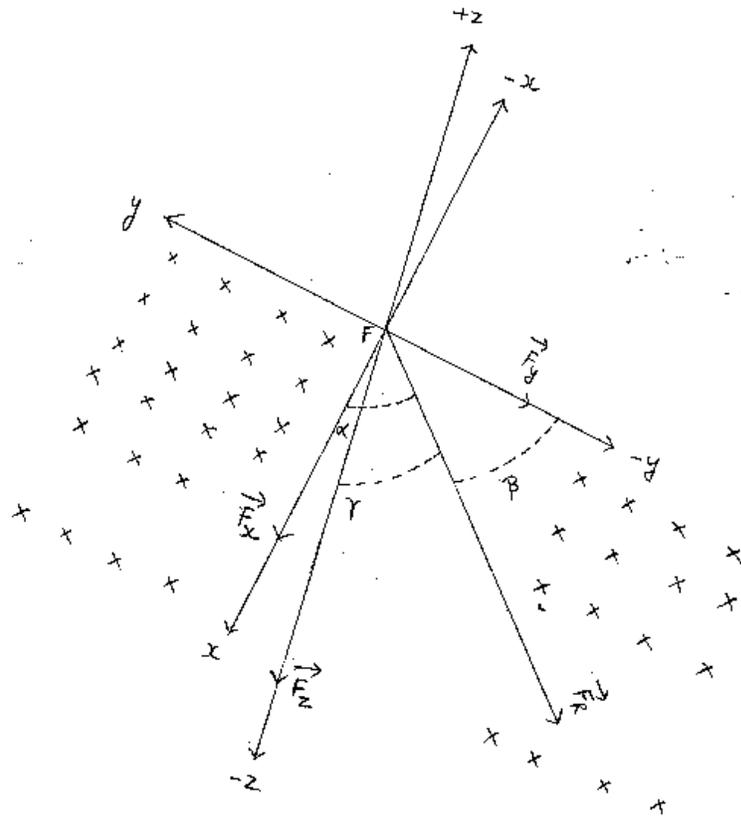
$$F_z = 5.0946 \times 10^{-13} \text{ N}$$

$$F_R^2 = (8.8211 \times 10^{-13})^2 + (5.0930 \times 10^{-13})^2 + (5.0946 \times 10^{-13})^2 \text{ N}^2$$

$$F_R^2 = (77.81180521 \times 10^{-26}) + (25.938649 \times 10^{-26}) + (25.95494916 \times 10^{-26}) \text{ N}^2$$

$$F_R^2 = 129.70540337 \times 10^{-26} \text{ N}^2$$

$$F_R = 11.3888 \times 10^{-13} \text{ N}$$



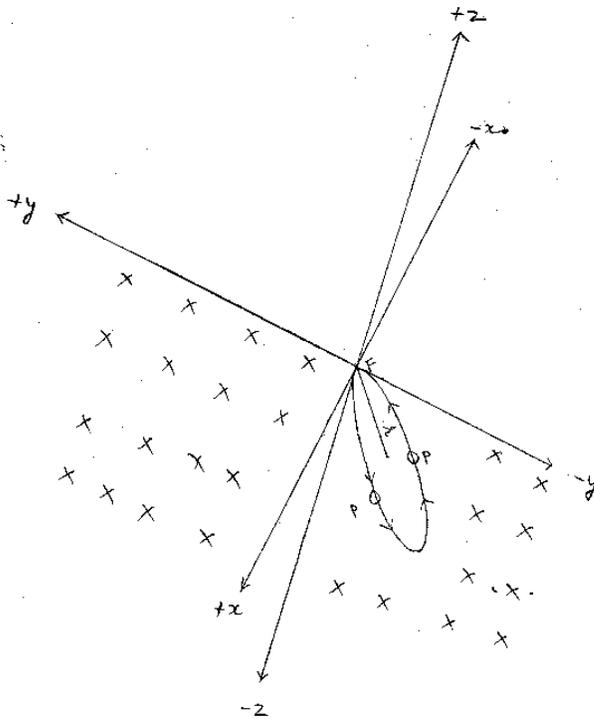
Radius of the circular orbit to be followed by the proton

$$\begin{aligned}r &= mv^2 / F_R \\mv^2 &= 67.6519 \times 10^{-13} \text{ J} \\F_R &= 11.3888 \times 10^{-13} \text{ N} \\r &= \frac{67.6519 \times 10^{-13} \text{ J}}{11.3888 \times 10^{-13} \text{ N}}\end{aligned}$$

$$r = 5.9402 \text{ m}$$

The circular orbit to be followed by the **proton** lies in the plane made up of positive x-axis, negative y-axis and the negative z-axis.

C_p = center of the circular orbit by the **proton**.



Angles that make the resultant force (F_R)

[acting on the proton when the proton is at point 'F'] with positive x, y and z -axes .

1 with x - axis

$$\cos \alpha = \frac{F_R \cos \alpha}{F_r} = \frac{\vec{F}_x}{F_r}$$

$$\vec{F}_x = 8.8211 \times 10^{-13} \text{ N}$$

$$F_r = 11.3888 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \alpha = 0.7745$$

$$\alpha = 39.24 \text{ degree } [\because \cos(39.24) = 0.7745]$$

2 with y- axis

$$\cos \beta = \frac{F_R \cos \beta}{F_r} = \frac{\vec{F}_y}{F_r}$$

$$\vec{F}_y = -5.0930 \times 10^{-13} \text{ N}$$

$$F_r = 11.3888 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \beta = -0.4471$$

$$\beta = 243.44 \text{ degree } [\because \cos(243.44) = -0.4471]$$

3 with z- axis

$$\cos \gamma = \frac{F_R \cos \gamma}{F_r} = \frac{\vec{F}_z}{F_r}$$

$$\vec{F}_z = -5.0946 \times 10^{-13} \text{ N}$$

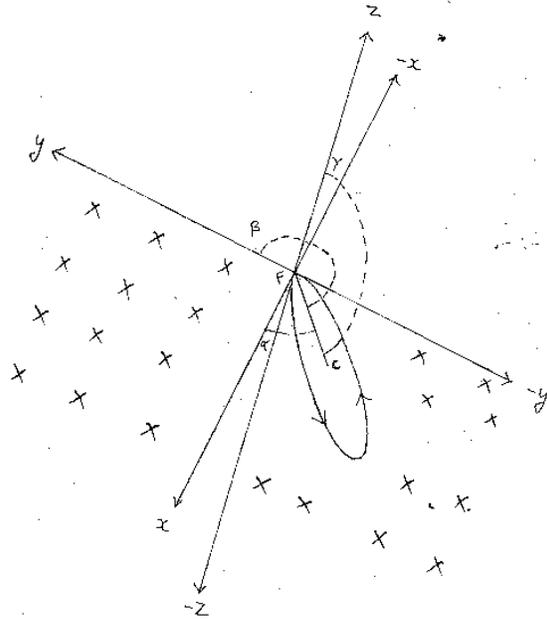
$$F_r = 11.3888 \times 10^{-13} \text{ N}$$

Putting values

$$\cos \gamma = -0.4473$$

$$\gamma = 243.425 \text{ degree}$$

Angles that make the resultant force (\vec{F}_r) at point 'F' with positive x, y, and z axes.



Where,

$$\alpha = 39.24 \text{ degree}$$

$$\beta = 243.44 \text{ degree}$$

$$\gamma = 243.425 \text{ degree}$$

The cartesian coordinates of the points $P_1 (x_1, y_1, z_1)$ and $P_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the **proton**.

$$\cos \alpha = \frac{x_2 - x_1}{d}$$

$$d = 2 \times r$$

$$= 2 \times 5.9402 \text{ m}$$

$$= 11.8804 \text{ m}$$

$$\cos \alpha = 0.7745$$

$$x_2 - x_1 = d \times \cos \alpha$$

$$x_2 - x_1 = 11.8804 \times 0.7745 \quad \text{m}$$

$$x_2 - x_1 = 9.2013 \text{ m}$$

$$x_2 = 9.2013 \text{ m} [\because x_1 = 0]$$

$$\cos \beta = \frac{y_2 - y_1}{d}$$

$$\cos \beta = -0.4471$$

$$y_2 - y_1 = d \times \cos \beta$$

$$y_2 - y_1 = 11.8804 \times (-0.4471) \text{ m}$$

$$y_2 - y_1 = -5.3117 \text{ m}$$

$$y_2 = -5.3117 \text{ m} \quad [\because y_1 = 0]$$

$$\cos \gamma = \frac{z_2 - z_1}{d}$$

$$\cos \gamma = -0.4473$$

$$z_2 - z_1 = d \times \cos \gamma$$

$$z_2 - z_1 = 11.8804 \times (-0.4473) \quad \text{m}$$

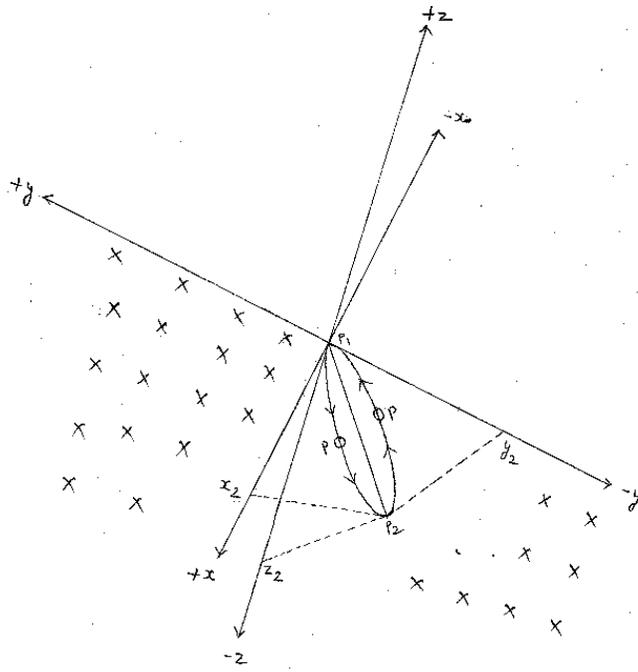
$$z_2 - z_1 = -5.3141 \text{ m}$$

$$z_2 = -5.3141 \text{ m} \quad [\because z_1 = 0]$$

The cartesian coordinates of the point $p_1 (x_1, y_1, z_1)$ and $p_2 (x_2, y_2, z_2)$ located on the circumference of the circle to be obtained by the proton are as shown below.

The line_____ is the diameter of the circle .

P_1P_2



Conclusion :-

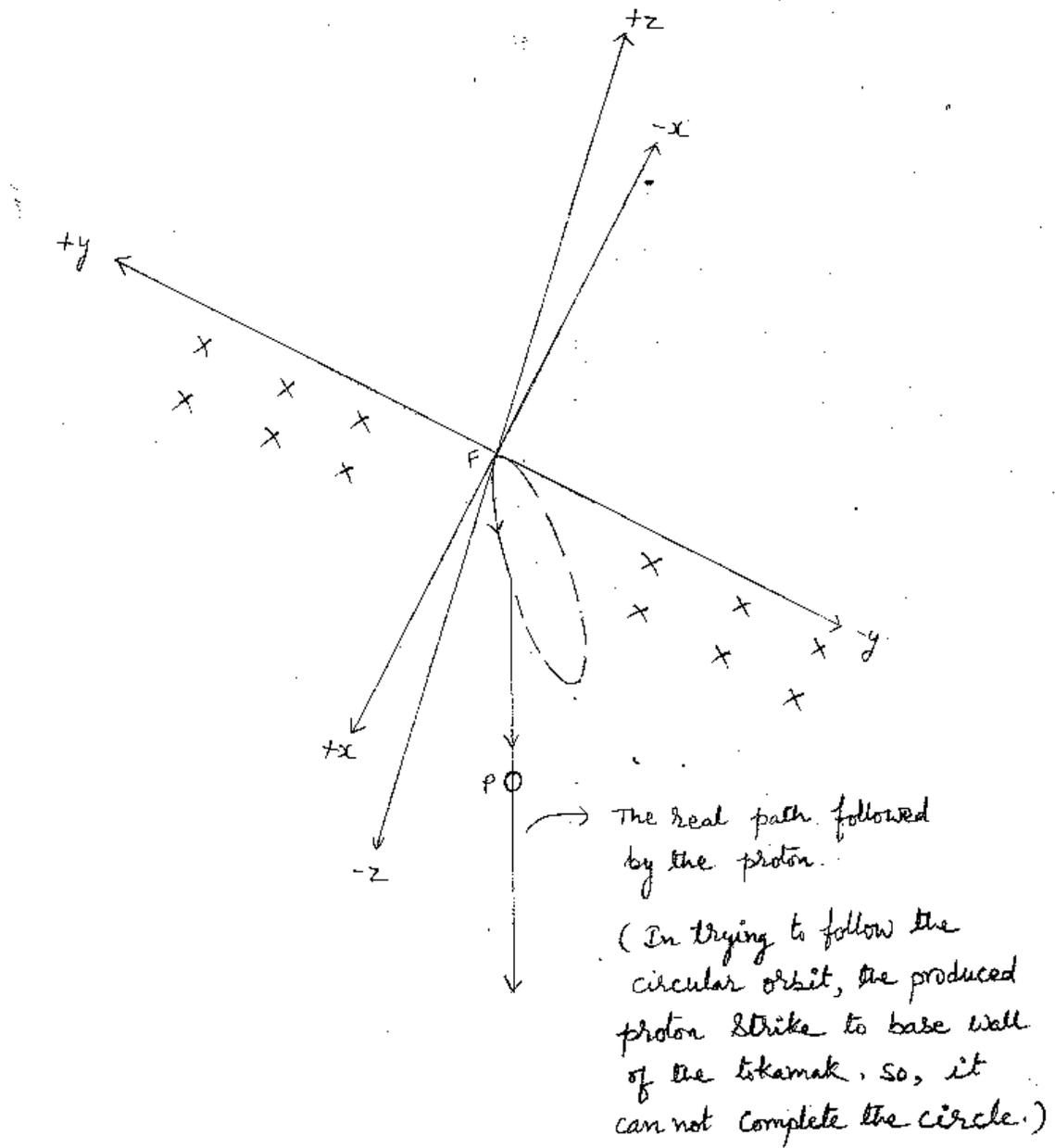
The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x, -y and -z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 5.9402 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(9.2013 \text{ m}, -5.3117 \text{ m}, -5.3141 \text{ m})$. in trying to complete its circle , due to lack of space , it strike to the base wall of the tokamak.

Hence the proton is not confined.



Summary

The confinement and the extraction of the particles :-

Either the charged particles will remain confined within the tokamak or not. As, due to applied magnetic fields, each charged particle will have to go through a circular motion. So to take decision about confinement of each charged particle, we will consider the Cartesian coordinates to be achieved by the each charged particle (either it is injected or produced during fusion reactions) during its circular motion. With the help of Cartesian coordinates to be achieved by each particle, we will come to know that either the charged particle will remain confined within the tokamak or due to lack of space within the tokamak, will have to strike to wall of tokamak. If the charged particle, strike to the wall of the tokamak, it will transfer its energy to the tokamak and thus will attain a gaseous state. Then the vacuum pumps attached to tokamak, will extract all these undesired particles (gases).

€ Conclusion for the injected deuteron

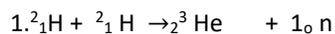
The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the deuteron are along **+x, -y and -z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the deuteron lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the deuteron to undergo to a circular orbit of radius of 0.7160 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.1092 \text{ m}, -0.6403 \text{ m}, -0.6406 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within the tokamak. And uninterruptedly goes on completing its circle until it fuses with the deuteron of later injected bunch (that reaches at point "F") at point "F"

€1. When we Consider the fusion reaction(1)



[injected] [confined]

Conclusion for the produced helium -3 nucleus :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **-x, +y and +z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

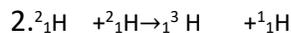
The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 0.4842 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.7501 \text{ m}, 0.4329 \text{ m}, 0.4331 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travels along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the helium-3 nucleus gets rid of magnetic fields, it leaves its circular motion, starts its linear motion. So, in spite of completing its circle, it travels upward and strikes the roof wall of the tokamak.

Hence the helium-3 nucleus is not confined.

€2. When we consider the fusion reaction(2)



[injected] [confined]

Conclusion for the produced proton :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x**, **-y** and **-z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis.

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 2.5977 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(4.0238 \text{ m}, -2.3233 \text{ m}, -2.3239 \text{ m})$. In trying to complete its circle, due to lack of space, it strikes the base wall of the tokamak.

Hence the proton is not confined.

Conclusion for the produced triton :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the triton are along **-x**, **+y** and **+z** axes respectively.

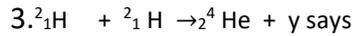
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the triton lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the triton to undergo to a circular orbit of radius 1.1918 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.8463 \text{ m}, 1.0659 \text{ m}, 1.0661 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travels along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the triton gets rid of magnetic fields, it leaves its circular motion, starts its linear motion. So, in spite of completing its circle, it travels upward and strikes the roof wall of the tokamak.

Hence the triton is not confined.

€ 3. When we consider fusion reaction (3)



[injected] [confined] (Confined)

Conclusion for the produced helium -4 nucleus :-

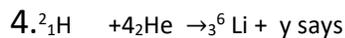
The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the helium-4 nucleus are along **+x, -y and -z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-4 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the helium-4 nucleus to undergo to a circular orbit of radius of 0.6997 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.0838 \text{ m}, -0.6258 \text{ m}, -0.6259 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

€ 4. When we consider the fusion reaction (4)



[injected] [confined] [confined]

Conclusion for the produced lithium -6 nucleus :-

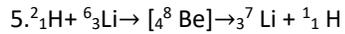
The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-6 nucleus are along **+x, -y and -z** axes respectively

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-6 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are applied.

The resultant force (\vec{F}_r) tends the lithium-6 nucleus to undergo to a circular orbit of radius of 0.6557 m. It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.0158 \text{ m}, -0.5863 \text{ m}, -0.5865 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F"

€ 5. when we consider fusion reaction (5)



[injected] [confined]

Conclusion for the produced lithium -7 nucleus:-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the lithium-7 nucleus are along **-x ,+y and +z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-7 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the lithium-7 nucleus to undergo to a circular orbit of radius 0.2645 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.4098 \text{ m}, 0.2364 \text{ m}, 0.2365 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the lithium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion .so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

So the lithium-7 nucleus is not confined.

Conclusion for the produced proton :-

The directions components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x , -y and -z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x- axis, negative y-axis and negative z-axis

The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 2.9812m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(4.6178 \text{ m}, -2.6657 \text{ m}, -2.6669 \text{ m})$. in trying to complete its circle , due to lack of space ,it strike to the base wall of the tokamak.

Hence the proton is not confined.

€ 6. When we consider the fusion reaction (6):-



(injected) (confined)

Conclusion for the produced beryllium -7 nucleus :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the beryllium-7 nucleus are along **-x , +y and +z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the beryllium-7 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-7 nucleus to undergo to a circular orbit of radius 0.0773 m .

It starts its circular motion from point P₁(0,0,0) and tries to reach at point P₂(-0.1198 m, 0.0690 m, 0.0690m) where the magnetic fields are not applied.

So , It starts its circular motion from point P₁(0,0,0) and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the beryllium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , in spite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

Hence the beryllium-7 nucleus is not confined.

€ 7. When we consider the fusion reaction (7)



(injected) (confined)

Conclusion for the produced right hand side propelled helium -4 nucleus :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the right hand side propelled helium-4 are along **+x , -y and -z** axes respectively

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the right hand side propelled helium-4 lies in the plane made up of positive x- axis, negative y-axis and negative z-axis

The resultant force (\vec{F}_r) tends the right hand side propelled helium-4 to undergo to a circular orbit of radius 4.8509 m.

It starts its circular motion from point P₁(0,0,0) and tries to reach at point P₂(7.5140 m, -4.3376 m, -4.3396 m). in trying to complete its circle , due to lack of space , it strikes to the base wall of the tokamak.

Hence the right hand side propelled helium-4 is not confined.

Conclusion for the left hand side propelled helium -4 nucleus :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the left hand side propelled helium-4 nucleus are along **-x , +y and +z** axes respectively

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the left hand side propelled helium-4 nucleus. lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

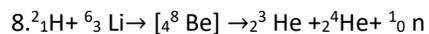
The resultant force (\vec{F}_r) tends the left hand side propelled helium-4 nucleus to undergo to a circular orbit of radius 3.7601m

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-5.8243 \text{ m}, 3.3630 \text{ m}, 3.3637 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the left hand side propelled helium-4 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and striketo the roof wall of the tokamak.

So theleft hand side propelled helium-4 nucleus is not confined.

€ 8. When we consider the fusion reaction (8)



Conclusion for the produced helium -3 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **-x , +y and +z** axes respectively .

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium -3 nucleus lies in the plane made up of negative x- axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 0.3899 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-0.6039 \text{ m}, 0.3487 \text{ m}, 0.3488 \text{ m})$ where the magnetic fields are not applied.

So , It starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the helium-3 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion . so , inspite of completing its circle , it travel upward and strike to the roof wall of the tokamak.

Hence the helium-3 nucleus is not confined.

Conclusion for the produced helium -4 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the helium-4 nucleus are along **+x , -y and -z** axes respectively .

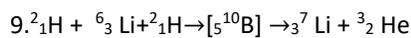
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-4 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the helium-4 nucleus to undergo to a circular orbit of radius of 0.7980 m.

It starts its circular motion from point $P_1(0,0,0)$ and reaches at point $P_2(1.2362 \text{ m}, -0.7135 \text{ m}, -0.7137 \text{ m})$ and again reaches at point P_1 .

Thus it remains confined within into the tokamak and uninterruptedly goes on completing its circle until it fuses with the confined deuteron or deuteron of later injected bunch (that reaches at point "F") at point "F".

€ 9. When we consider the fusion reaction (9)



(injected) (confined) (confined)

Conclusion for the produced lithium-7 nucleus :-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the lithium-7 nucleus are along **-x, +y and +z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the lithium-7 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the lithium-7 nucleus to undergo to a circular orbit of radius 1.4805 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-2.2935 \text{ m}, 1.3238 \text{ m}, 1.3241 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travel along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. so as the lithium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. so, in spite of completing its circle, it travel upward and strike to the roof wall of the tokamak.

The lithium-7 nucleus is not confined within into the tokamak.

Conclusion for the produced helium -3 nucleus:-

The directions components [\vec{F}_x, \vec{F}_y , and \vec{F}_z] of the resultant force (\vec{F}_r) that are acting on the helium-3 nucleus are along **+x, -y and -z** axes respectively.

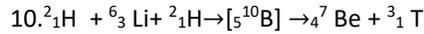
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-3 nucleus lies in the plane made up of positive x-axis, negative y-axis and negative z-axis

The resultant force (\vec{F}_r) tends the helium-3 nucleus to undergo to a circular orbit of radius 3.3766 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(5.2303 \text{ m}, -3.0200 \text{ m}, -3.0207 \text{ m})$. In trying to complete its circle, due to lack of space, it strikes the base wall of the tokamak.

Hence the helium-3 nucleus is not confined.

€ 10. When we consider the fusion reaction (10)



Conclusion for the produced beryllium-7 nucleus :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the beryllium-7 nucleus are along **-x, +y and +z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the beryllium-7 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-7 nucleus to undergo to a circular orbit of radius 1.0458 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.6201 \text{ m}, 0.9351 \text{ m}, 0.9353 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travels along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the beryllium-7 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. So, in spite of completing its circle, it travels upward and strikes the roof wall of the tokamak.

The beryllium-7 nucleus is not confined within into the tokamak.

Conclusion for the produced triton :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{ and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the triton are along **+x, -y and -z** axes respectively.

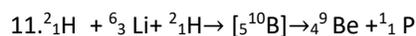
So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the triton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis.

The resultant force (\vec{F}_r) tends the triton to undergo to a circular orbit of radius 6.4952 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(10.0610 \text{ m}, -5.8093 \text{ m}, -5.8106 \text{ m})$. In trying to complete its circle, due to lack of space, it strikes the base wall of the tokamak.

Hence the triton is not confined.

€ 11. When we consider fusion reaction (11)



Conclusion for the produced beryllium-9 nucleus :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the beryllium-9 nucleus are along **-x, +y and +z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the helium-3 nucleus lies in the plane made up of negative x-axis, positive y-axis and positive z-axis where the magnetic fields are not applied.

The resultant force (\vec{F}_r) tends the beryllium-9 nucleus to undergo to a circular orbit of radius 0.9078 m. It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(-1.4061 \text{ m}, 0.8117 \text{ m}, 0.8121 \text{ m})$ where the magnetic fields are not applied.

So, it starts its circular motion from point $P_1(0,0,0)$ and as it travels along a negligible circular path (distance), it gets rid of the region covered-up by the applied magnetic fields. So as the beryllium-9 nucleus gets rid of magnetic fields, it leaving its circular motion, starts its linear motion. So, in spite of completing its circle, it travels upward and strikes to the roof wall of the tokamak.

The beryllium-9 nucleus is not confined within into the tokamak.

Conclusion for the produced proton :-

The direction components $[\vec{F}_x, \vec{F}_y, \text{and } \vec{F}_z]$ of the resultant force (\vec{F}_r) that are acting on the proton are along **+x, -y and -z** axes respectively.

So by seeing the direction of the resultant force (\vec{F}_r) we come to know that the circular orbit to be followed by the proton lies in the plane made up of positive x-axis, negative y-axis and negative z-axis.

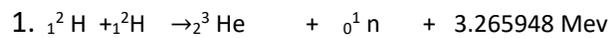
The resultant force (\vec{F}_r) tends the proton to undergo to a circular orbit of radius 5.9402 m.

It starts its circular motion from point $P_1(0,0,0)$ and tries to reach at point $P_2(9.2013 \text{ m}, -5.3117 \text{ m}, -5.3141 \text{ m})$. In trying to complete its circle, due to lack of space, it strikes to the base wall of the tokamak.

Hence the proton is not confined.

The power produced :

To calculate the heat energy produced we will consider the main fusion reactions only. To calculate the heat energy we will consider the released energy (E) of the each particle that has produced due to fusion reactions .



$$E_{\text{produced}} = 2 \text{}^2_1\text{H} \rightarrow \text{}^3_2\text{He} + \text{}^3_1\text{H} + \text{}^1_1\text{H} + \text{}^1_0\text{n} + 7.297178 \text{ Mev}$$

Conclusion : 4 deuterons fuse to produce onehelium-3 nuclei ,one triton, one proton and one neutron and 7.297178 Mev energy.

Total input energy :

Each deuteron is injected with 153.6Kev or with 0.1536 Mev energy.

So, the total input energy that is carried by the 6×10^{19} injected deuterons is –

$$\begin{aligned} E_{\text{input}} &= 0.1536 \times 1.6 \times 10^{13} \text{ J} \times 6 \times 10^{19} \text{ per second} \\ E_{\text{input}} &= 1.474 \times 10^5 \text{ W} \\ &= 0.1474 \text{ MW} \end{aligned}$$

Net yield energy :

$$\text{Net yield} = E_{\text{produced}} - E_{\text{input}}$$

$$\text{Net yield} = 1.7513 \text{ MW} - 0.1474 \text{ Mev}$$

$$\text{Net yield} = 1.6039 \text{ MW}$$

VBM fusion reactor and the power produced

The 4 deuterons fuse to yield 7.297178 MeV or the 4 deuterons fuse to yield $7.297178 \times 1.6 \times 10^{-13}$ J.

Then if the 6×10^{18} deuterons fuse per second then the power produced is –

$$P = 7.297178 \times 1.6 \times 10^{-13} \times 6 \times 10^{19} \text{ J}$$

4s

$$P = 17.5132272 \times 10^5 \text{ J/s}$$

$$P = 1.751322 \times 10^6 \text{ J/s}$$

$$P = 1.751322 \text{ MW}$$

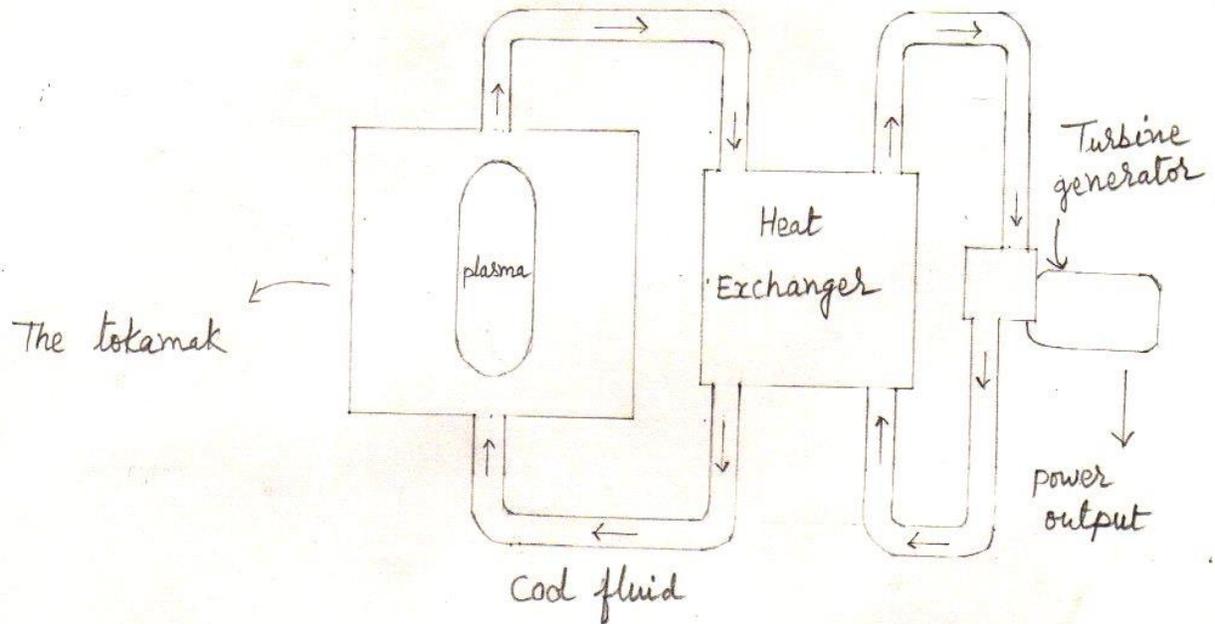
VBM fusion reactor and the Lawson criterion

For a deuterium – deuterium fusion reaction the,

$$n_e T_e \geq 10^{22} \text{ s/m}^3$$

As in VBM fusion reactor, there the identical bunches of deuterons are being injected, there the injected bunches during their linear path from particle accelerator to the point "F" follow one another and similarly the later injected bunch also follows the earlier injected bunch in their circular path and again pass through the point "F" one by one where they (deuterons) will have to meet (fuse) with the injected deuterons reaching at point "F". So, the VBM Fusion Reactor always achieves the Lawson criterion.

Mode of output



The heat is transferred by a water – cooling loop from the tokamak to a heat exchanger to make steam. The steam will drive electrical turbines to produce electricity . The steam will be condensed back into water to absorb more heat from tokamak.