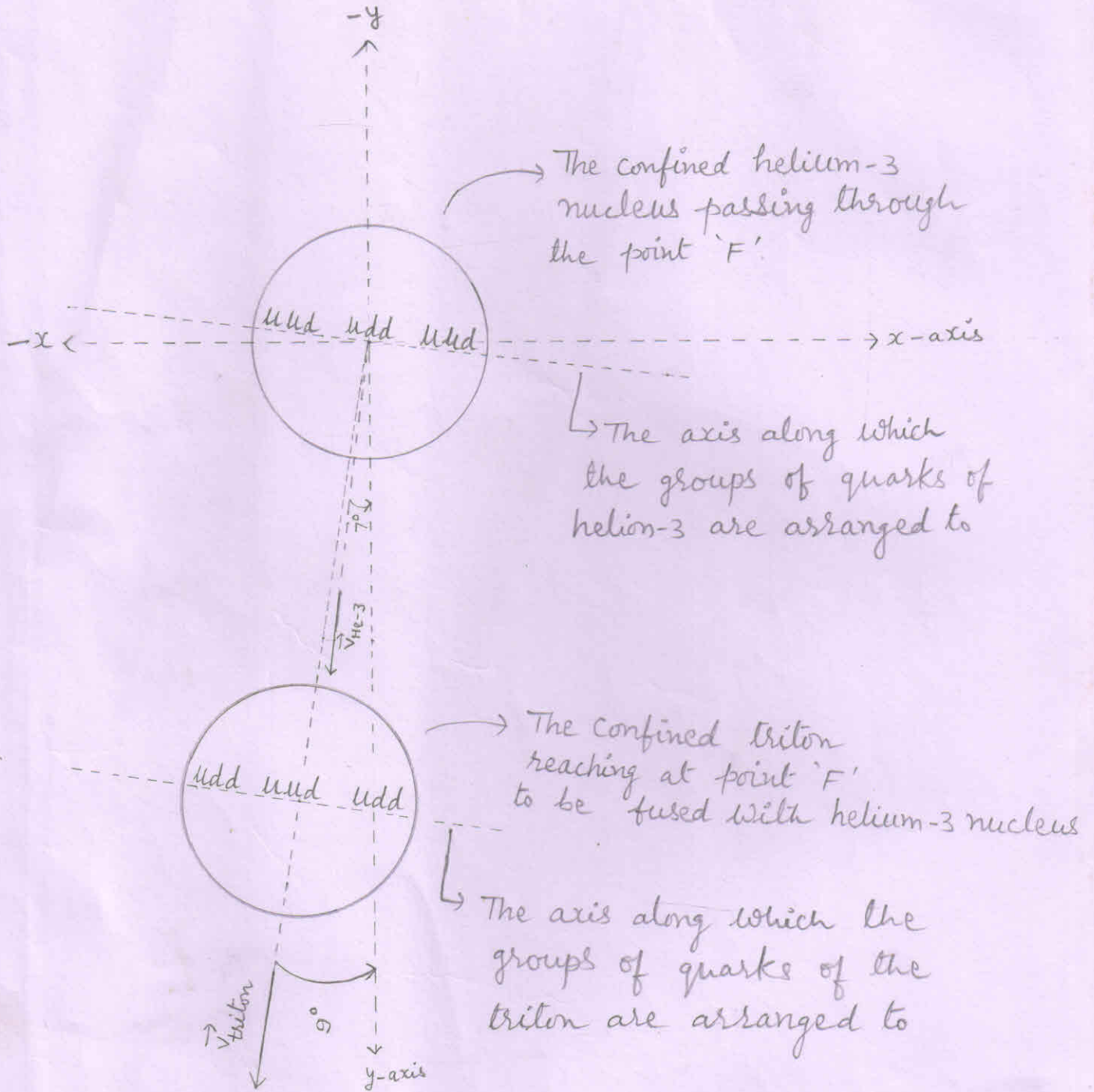


For fusion reaction (i) :  ${}^3_1\text{H} + {}^3_2\text{He} \rightarrow {}^5_3\text{Li} + {}^1_0\text{n}$

### 1. Interaction of nuclei :-

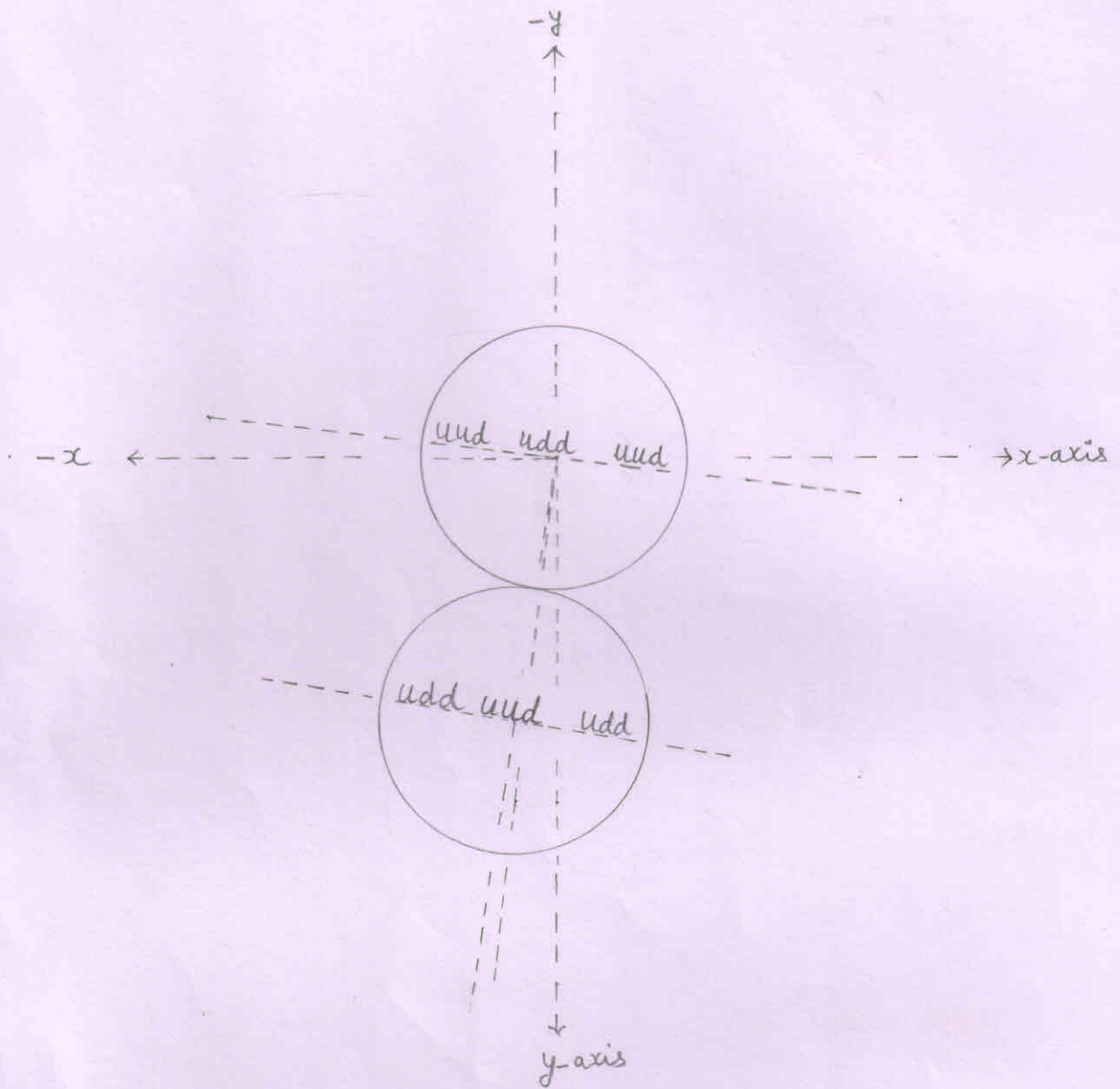
The confined triton reaches at point F and interacts [experiences a repulsive force due to confined helium-3 passing through the point 'F'] with the confined helium-3 at point 'F'. The confined triton overcomes the electrostatic repulsive force and - a like two solid spheres join - the confined triton dissimilarly joins with the confined helium-3 nucleus.



□ 1 (1)

Interaction of nuclei

# Interaction of nuclei



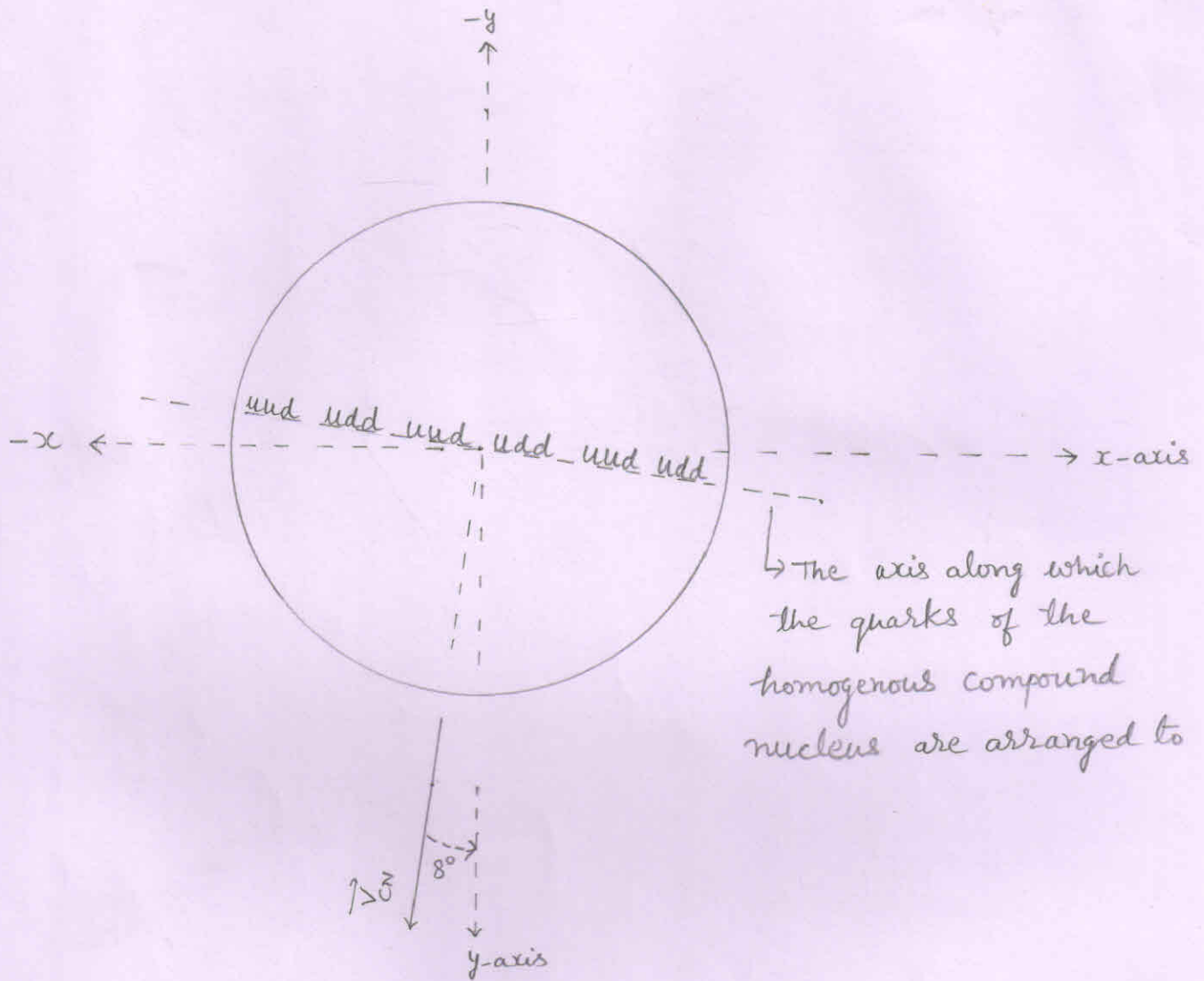
□ 1 (2)

The dissimilarly joined nuclei

2. Formation of the homogenous compound nucleus :-  
The constituents (quarks and gluons) of the dissimilarly joined nuclei (the triton and the helium-3) behave like a liquid and form the homogenous compound nucleus having similarly distributed groups of quarks with similarly distributed surrounding gluons.

Thus within the homogenous compound nucleus - each group of quarks is surrounded by gluons in equal proportion. So, within the homogenous compound nucleus there are 6 groups of quarks surrounded by the gluons.

# The homogenous compound nucleus



2

## The homogenous compound nucleus

⇒ The triton dissimilarly joined with the helium-3 nucleus and then their constituents form a homogenous compound nucleus. or the helium-3 nucleus dissimilarly joined with the triton and then their constituents form the homogenous compound nucleus.

In both these above conditions, the number of groups of quarks that compose the homogenous compound nucleus remains same but the arrangement of groups of quarks on their own axis of the homogenous compound nucleus [that they compose] differs. That is why the compound nucleus splits into three ways - 1. Lithium-5 +  $\Delta m$  + neutron

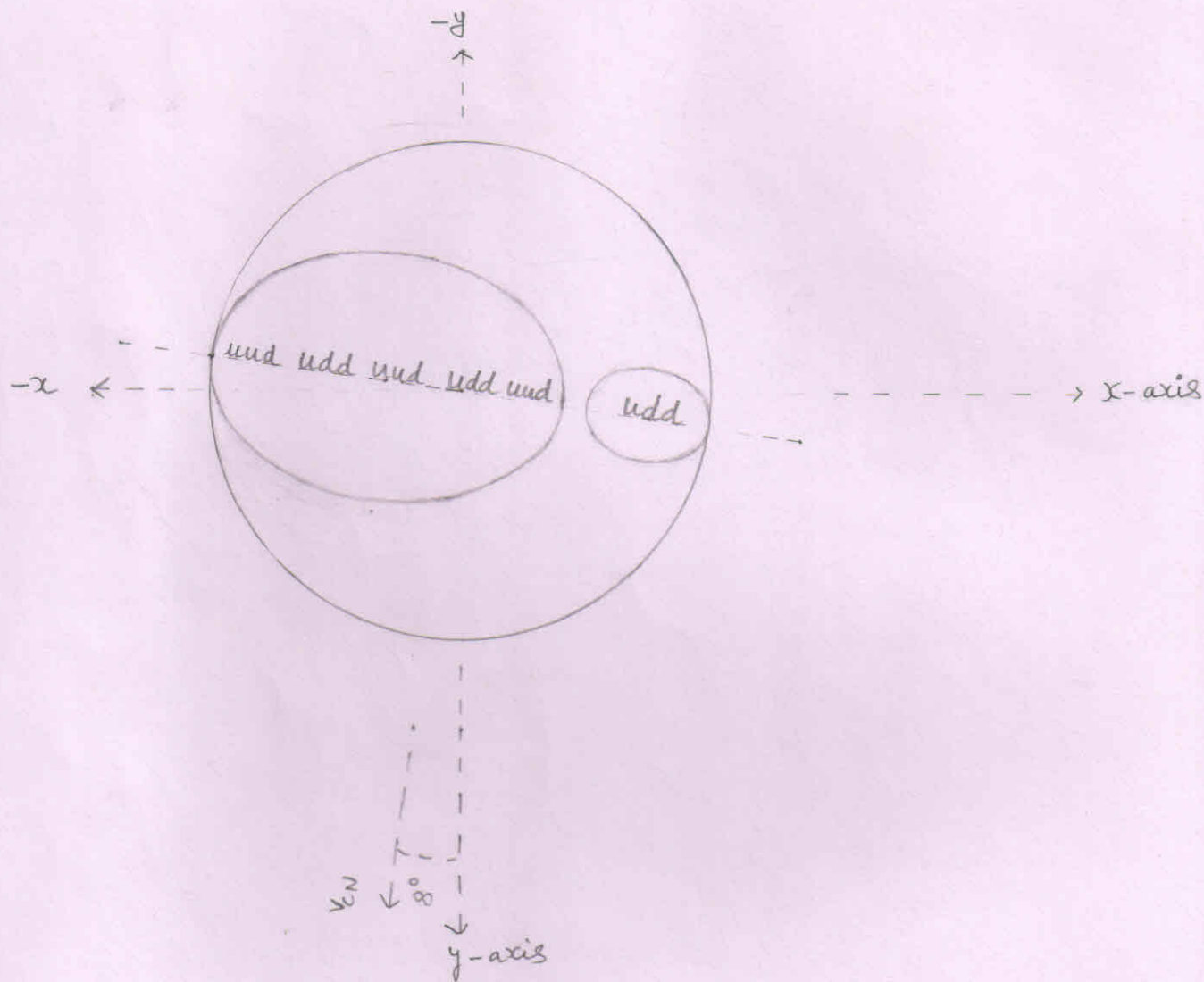
3. Formation of lobes within into the homogenous compound nucleus or the transformation of the homogenous compound nucleus into the heterogenous compound nucleus :-

The central group of quarks with its surrounding gluons to become a stable and the next higher nucleus (the lithium-5) than the reactant one (the helium-3) includes the other four (nearly located) groups of quarks with their surrounding gluons and rearrange to form the 'A' lobe of the heterogenous compound nucleus.

While the remaining group of quarks to become a stable nucleus (the neutron) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe 'A'] and rearrange to form the 'B' lobe of the heterogenous compound nucleus.

Thus, due to formation of two dissimilar lobes within into the homogenous compound nucleus, the homogenous compound nucleus transforms into the heterogenous compound nucleus.

### 3 Formation of lobes



#### Formation of lobes

⇒ Within into the homogenous compound nucleus, the greater nucleus is the lithium-5 and the smaller nucleus is the neutron and the remaining space represents the remaining gluons.

⇒ Within into the homogenous compound nucleus, the greater nucleus is the lobe 'A' while the smaller nucleus is the lobe 'B'

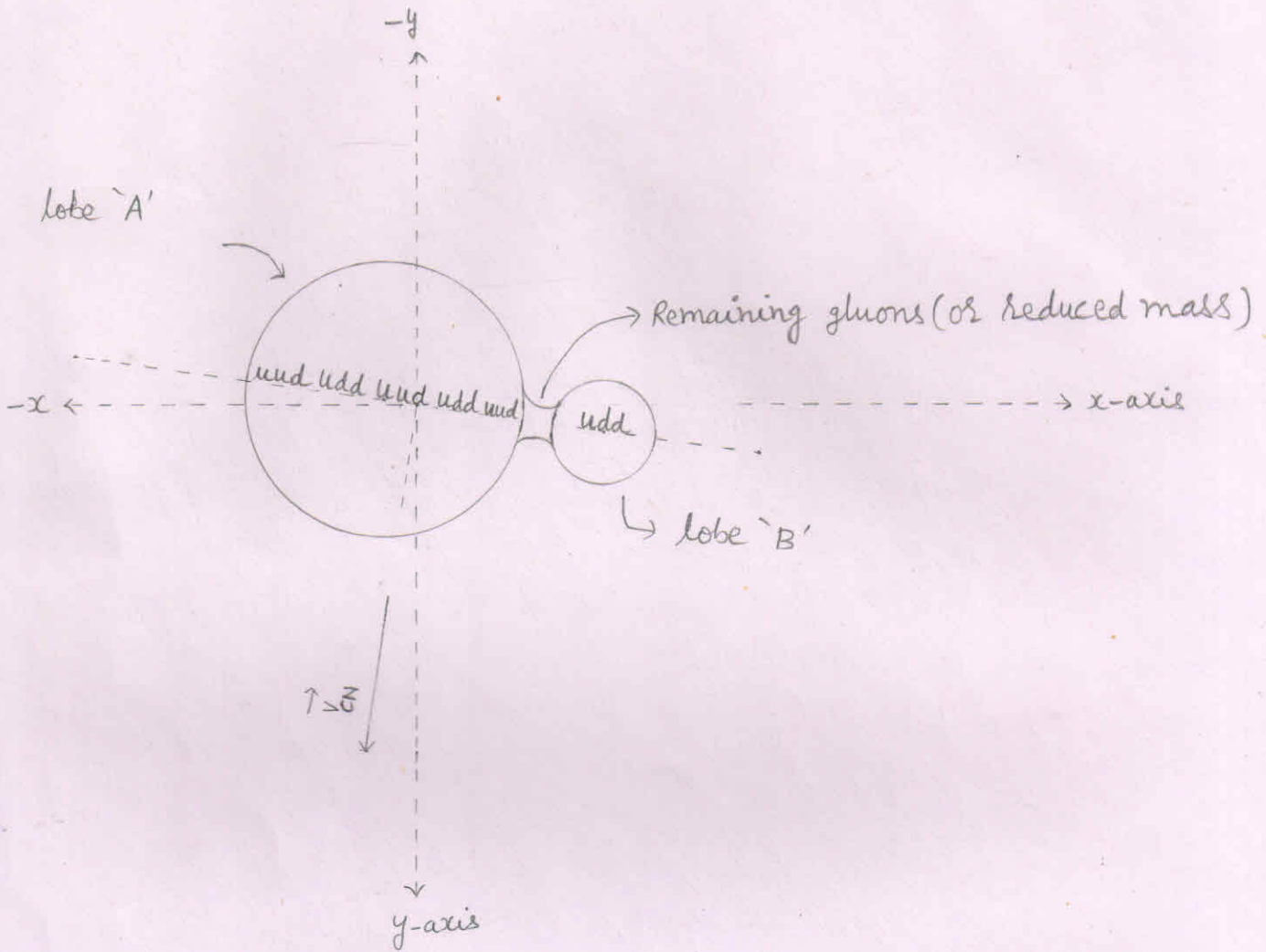
#### 4. Final Stage of the heterogenous compound nucleus:-

The process of formation of lobes creates voids between the lobes. So, the remaining gluons [ or the mass that is not involved in the formation of any lobe ] rearrange to fill the void(s) between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogenous compound nucleus.

Thus, the reduced mass (or the remaining gluons) keeps both the dissimilar lobes - of the heterogenous compound nucleus - joined together.

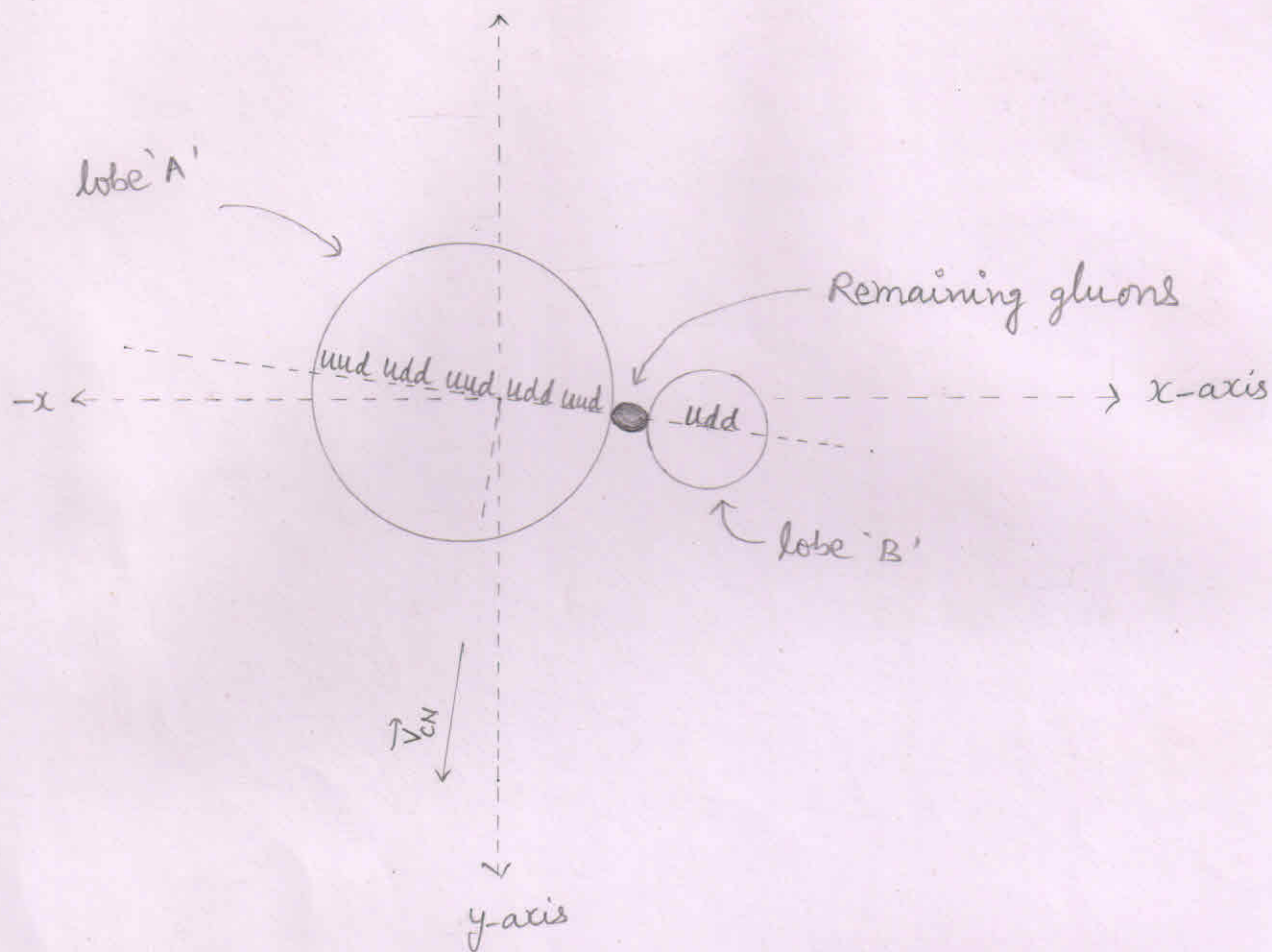
So, finally, the heterogenous compound nucleus becomes like an abnormal digit eight or becomes like a dumb-bell.





4(1)

Final stage of the heterogenous compound nucleus



4(2)

Final stage of the heteronuclear compound nucleus

Minimum kinetic energy ( $E_m$ ) required by the triton for  ${}^3_1\text{T} - {}^3_2\text{He}$  fusion is -

$$E_m = \frac{2k^2 z_1^2 z_2^2 q^4 m}{h^2}$$

$$z_1 = 1 \text{ and } z_2 = 2$$

$$m = m_t = 5.0072 \times 10^{-27} \text{ kg}$$

$$\Rightarrow E_m = \frac{2 \times (9 \times 10^9)^2 \times 1^2 \times 2^2 \times (1.6 \times 10^{-19})^4 \times 5.0072 \times 10^{-27}}{(6.62 \times 10^{-34})^2} \text{ J}$$

$$\Rightarrow E_m = \frac{21264 \cdot 2404761 \times 10^{18} \times 10^{-76} \times 10^{-27}}{43 \cdot 8244 \times 10^{-68}} \text{ J}$$

$$\Rightarrow E_m = 485 \cdot 2146 \times 10^{-17} \text{ J}$$

$$\Rightarrow E_m = 303 \cdot 2591 \times 10^2 \text{ eV}$$

$$= 30 \cdot 32591 \times 10^3 \text{ eV}$$

$$= 0.0303 \text{ MeV}$$

## Formation of Compound nucleus

1. As the confined triton reaches at point 'F', it fuses with the confined helium-3 [passing through the point 'F'] to form the compound nucleus.
  2. Just before fusion, to overcome the electrostatic repulsive force, the triton loses energy equal to 0.0303 MeV.
- S So, just before fusion, the kinetic energy of the triton is -

$$E_b = [1.1583 \text{ MeV}] - [0.0303 \text{ MeV}]$$
$$= 1.128 \text{ MeV}$$

3. Momentum of the triton (just before fusion)

$$P_b = \left[ 2 m_t E_b \right]^{\frac{1}{2}}$$

$$E_b = 1.128 \times 1.6 \times 10^{-13} \text{ J}$$

$$\Rightarrow P_b = \left[ 2 \times 5.0072 \times 10^{-27} \times 1.128 \times 1.6 \times 10^{-13} \right]^{\frac{1}{2}} \text{ kg m/s}$$

$$\Rightarrow P_b = \left[ 18.07398912 \times 10^{-40} \right]^{\frac{1}{2}} \text{ kg m/s}$$

$$\Rightarrow P_b = 4.2513 \times 10^{-20} \text{ kg m/s}$$

Components of the momentum of the triton just before fusion :-

If  $\alpha$ ,  $\beta$  and  $\gamma$  are the angles made by the triton with respect to positive x, y and z axes respectively. Then

$$1. \vec{P}_x = \frac{P}{b} \cos \alpha$$

$$P = 4.2513 \times 10^{-20} \text{ Kg m/s}$$

$$\cos \alpha = \cos 99^\circ \approx -0.1556$$

$$\Rightarrow \vec{P}_x = 4.2513 \times 10^{-20} \times (-0.1556) \text{ Kg m/s}$$
$$= -0.6615 \times 10^{-20} \text{ Kg m/s}$$

$$2. \vec{P}_y = \frac{P}{b} \cos \beta$$

$$\cos \beta = \cos 9^\circ \approx 0.9879$$

$$\Rightarrow \vec{P}_y = 4.2513 \times 10^{-20} \times 0.9879 \text{ Kg m/s}$$
$$= 4.1998 \times 10^{-20} \text{ Kg m/s}$$

$$3. \vec{P}_z = \frac{P}{b} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\Rightarrow \vec{P}_z = 4.2513 \times 10^{-20} \times 0 \text{ Kg m/s}$$
$$= 0 \text{ Kg m/s}$$

Components of momentum of the compound nucleus :-

1. X-Component of momentum of compound nucleus =

$$\left[ \begin{array}{l} \text{X-Component of momentum} \\ \text{of the Confined Triton} \\ \text{just before fusion} \\ \text{at point F} \end{array} \right] + \left[ \begin{array}{l} \text{X-Component of} \\ \text{the momentum} \\ \text{of the Confined Helium-3} \\ \text{at point F} \end{array} \right]$$

$$\begin{aligned} \vec{P}_x &= [-0.6615 \times 10^{-20}] + [-0.4710 \times 10^{-20}] \text{ Kg m/s} \\ &= -1.1325 \times 10^{-20} \text{ Kg m/s} \end{aligned}$$

2. Y-Component of momentum of compound nucleus =

$$\left[ \begin{array}{l} \text{Y-Component of momentum} \\ \text{of the Confined Triton} \\ \text{just before fusion} \\ \text{at point F} \end{array} \right] + \left[ \begin{array}{l} \text{Y-Component of} \\ \text{the momentum of} \\ \text{the Confined Helium-3} \\ \text{at point F} \end{array} \right]$$

$$\begin{aligned} \vec{P}_y &= [4.1998 \times 10^{-20}] + [3.9094 \times 10^{-20}] \text{ Kg m/s} \\ &= 8.1092 \times 10^{-20} \text{ Kg m/s} \end{aligned}$$

3. z-Component of momentum of Compound nucleus =

$$\left[ \begin{array}{l} \text{z-Component of momentum} \\ \text{of the Confined triton} \\ \text{just before fusion} \\ \text{at point F} \end{array} \right] + \left[ \begin{array}{l} \text{z-Component of} \\ \text{the momentum of} \\ \text{the Confined Helium-3} \\ \text{at point F} \end{array} \right]$$

$$\Rightarrow \vec{P}_z = [0] + [0] \quad \text{kgm/s}$$
$$= 0 \quad \text{kgm/s}$$

4. Mass of the Compound nucleus (M) :

$$M = m_t + m_{\text{He-3}}$$
$$= (5.0072 \times 10^{-27}) + (5.00629 \times 10^{-27}) \quad \text{kg}$$
$$= 10.01349 \times 10^{-27} \quad \text{kg}$$

Components of the velocity of the Compound nucleus:  $\rightarrow$

1. X-Component of the velocity of the Compound nucleus: -

$$\Rightarrow \vec{V}_x = \frac{V \cos \alpha}{CN} = \frac{\vec{P}_x}{M} = \frac{P_{CN} \cos \alpha}{M}$$

$$\Rightarrow \vec{V}_x = \frac{V \cos \alpha}{CN} = \frac{-1.1325 \times 10^{-20} \text{ kg m/s}}{10.01349 \times 10^{-27} \text{ kg}}$$

$$\Rightarrow \vec{V}_x = \frac{V \cos \alpha}{CN} = -0.1130 \times 10^7 \text{ m/s}$$

2. Y-Component of the velocity of the Compound nucleus: -

$$\Rightarrow \vec{V}_y = \frac{V \cos \beta}{CN} = \frac{\vec{P}_y}{M} = \frac{P_{CN} \cos \beta}{M}$$

$$\Rightarrow \vec{V}_y = \frac{V \cos \beta}{CN} = \frac{8.1092 \times 10^{-20} \text{ kg m/s}}{10.01349 \times 10^{-27} \text{ kg}}$$

$$\Rightarrow \vec{V}_y = \frac{V \cos \beta}{CN} = 0.8098 \times 10^7 \text{ m/s}$$

3. Z-Component of the velocity of the Compound nucleus -

$$\Rightarrow \vec{V}_z = \frac{V \cos \gamma}{CN} = \frac{\vec{P}_z}{M} = \frac{P_{CN} \cos \gamma}{M}$$

$$\Rightarrow \vec{V}_z = \frac{V \cos \gamma}{CN} = 0 \text{ kg m/s} = 0 \text{ m/s}$$



Velocity of the Compound nucleus ( $\vec{V}_{CN}$ ) :-

$$V_{CN}^2 = V_x^2 + V_y^2 + V_z^2$$

$$\vec{V}_x = V_{CN} \cos \alpha = -0.1130 \times 10^7 \text{ m/s}$$

$$\vec{V}_y = V_{CN} \cos \beta = 0.8098 \times 10^7 \text{ m/s}$$

$$\vec{V}_z = V_{CN} \cos \gamma = 0 \text{ m/s}$$

$$\Rightarrow V_{CN}^2 = (0.1130 \times 10^7)^2 + (0.8098 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$= (0.012769 \times 10^{14}) + (0.65577604 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$V_{CN}^2 = 0.66854504 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$\Rightarrow V_{CN} = 0.8176 \times 10^7 \text{ m/s}$$

Angle made by the velocity of the Compound nucleus ( $\vec{V}_{CN}$ ):-

$\Rightarrow$  If  $\alpha$ ,  $\beta$  and  $\gamma$  are the angles made by the velocity of the Compound nucleus with respect to the  $x$ ,  $y$  and  $z$  axes respectively. Then

$$1. \cos \alpha = \frac{V_{CN} \cos \alpha}{V_{CN}}$$

$$V_{CN} \cos \alpha = -0.1130 \times 10^7 \text{ m/s}$$
$$V_{CN} = 0.8176 \times 10^7 \text{ m/s}$$

$$\cos \alpha = \frac{-0.1130 \times 10^7 \text{ m/s}}{0.8176 \times 10^7 \text{ m/s}} = -0.1382$$

$$\alpha \approx 98^\circ$$

$$2. \cos \beta = \frac{V_{CN} \cos \beta}{V_{CN}}$$

$$V_{CN} \cos \beta = 0.8098 \times 10^7 \text{ m/s}$$

$$\Rightarrow \cos \beta = \frac{0.8098 \times 10^7 \text{ m/s}}{0.8176 \times 10^7 \text{ m/s}} = 0.9904$$

$$\beta \approx 8^\circ$$

$$3. \cos \gamma = \frac{V_{CN} \cos \gamma}{V_{CN}}$$

$$V_{CN} \cos \gamma = 0 \text{ m/s}$$

$$\Rightarrow \cos \gamma = \frac{0 \text{ m/s}}{0.8176 \times 10^7 \text{ m/s}} = 0$$

## The splitting of the heterogenous compound nucleus:-

⇒ The heterogenous compound nucleus, due to its instability, splits according to the lines parallel to the direction of the velocity of the compound nucleus ( $\vec{v}_{CN}$ ) into three particles - the lithium-5, the neutron and the reduced mass ( $\Delta m$ ).

out of them, the two particles (the lithium-5 and the neutron) are stable while the third one (reduced mass) is unstable.

⇒ According to the law of inertia, each particle that has separated from the compound nucleus has an inherited velocity ( $\vec{v}_{inh}$ ) equal to the velocity of the compound nucleus ( $\vec{v}_{CN}$ ).

⇒ So, for conservation of momentum

$$M\vec{v}_{CN} = (m_{Li-5} + \Delta m + m_n) \vec{v}_{CN}$$

Where,

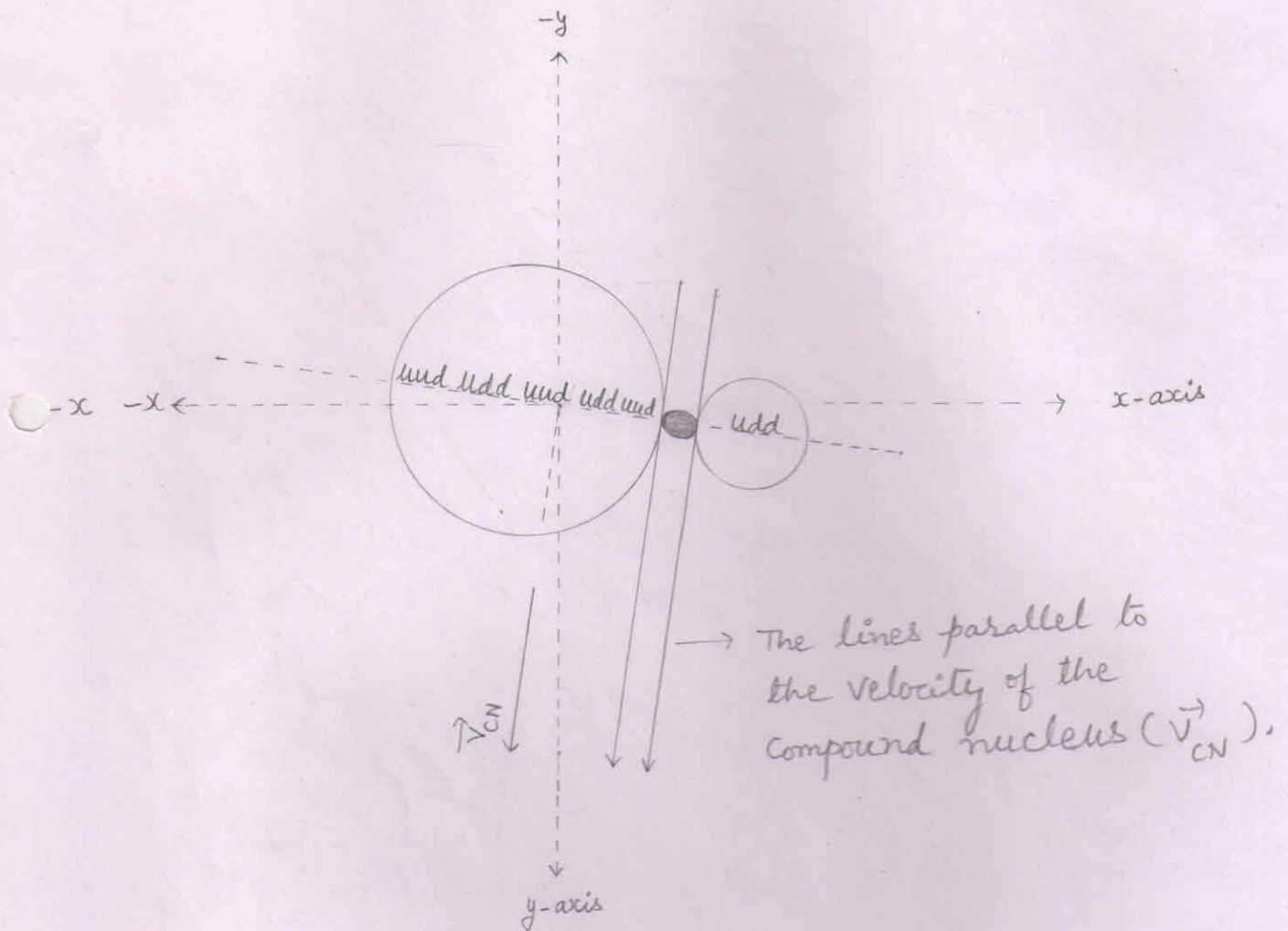
$M$  = mass of the compound nucleus

$\vec{v}_{CN}$  = velocity of the compound nucleus

$m_{Li-5}$  = mass of the lithium-5

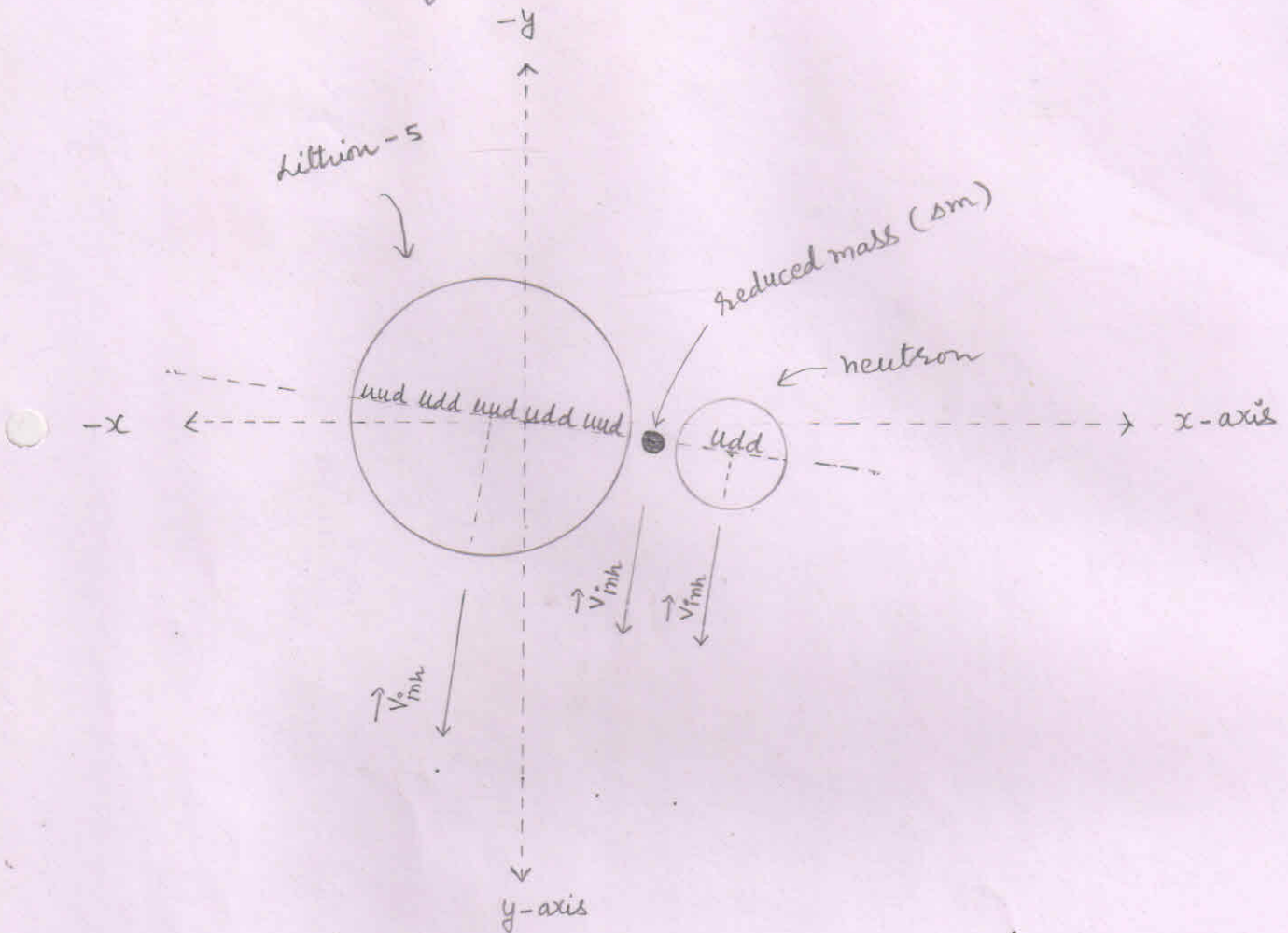
$\Delta m$  = reduced mass

$m_n$  = mass of the neutron



The Splitting of the heterogeneous compound nucleus

# The splitting of the heterogenous compound nucleus



⇒ The heterogenous compound nucleus splits into three particles - Lithium-5, reduced mass and the neutron.

## Inherited velocity of the particles

⇒ Each particle that has separated from the compound nucleus has an inherited velocity ( $\vec{V}_{inh}$ ) & equal to the velocity of the compound nucleus ( $\vec{V}_{CN}$ ).

1. Inherited velocity of the lithium-5.

$$V_{inh} = V_{CN} = 0.8176 \times 10^7 \text{ m/s}$$

⇒ Components of the inherited velocity ( $\vec{V}_{inh}$ ) of the lithium-5.

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = -0.1130 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.8098 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

2. Inherited velocity of the neutron

$$V_{inh} = V_{CN} = 0.8176 \times 10^7 \text{ m/s}$$

⇒ Components of inherited velocity ( $\vec{V}_{inh}$ ) of the neutron :-

$$1. \vec{V}_x = V_{inh} \cos \alpha = V_{CN} \cos \alpha = -0.1130 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inh} \cos \beta = V_{CN} \cos \beta = 0.8098 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inh} \cos \gamma = V_{CN} \cos \gamma = 0 \text{ m/s}$$

3. Inherited velocity of the reduced mass ( $\Delta m$ ) :-

## Propellation of the particles.

### 1. Reduced mass

$$\begin{aligned}\Delta m &= [m_t + m_{\text{He-3}}] - [m_{\text{Li-5}} + m_n] \\ &= [3.0155 + 3.0149] - [5.0109 + 1.0086] \text{ amu} \\ &= [6.0304] - [6.0195] \text{ amu} \\ &= 0.0109 \text{ amu} \\ &= 0.0109 \times 1.6605 \times 10^{-27} \text{ kg} \\ &= 0.01809945 \times 10^{-27} \text{ kg}\end{aligned}$$

### 2. Inherited kinetic energy of the reduced mass :

$$E_{\text{inh}} = \frac{1}{2} \Delta m v_{\text{inh}}^2 = \frac{1}{2} \Delta m v_{\text{CN}}^2$$

$$v_{\text{CN}}^2 = 0.66854504 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$\begin{aligned}\Rightarrow E_{\text{inh}} &= \frac{1}{2} \times 0.01809945 \times 10^{-27} \times 0.66854504 \times 10^{14} \text{ J} \\ &= 0.00605014876 \times 10^{-13} \text{ J} \\ &= 0.0037 \text{ MeV}\end{aligned}$$

### 3. Released energy ( $E_R$ ) :

$$\begin{aligned}E_R &= \Delta m c^2 \\ &= 0.0109 \times 931 \text{ MeV} \\ &= 10.1479 \text{ MeV}\end{aligned}$$

4. Total energy ( $E_T$ ) :

$$E_T = E_{inh} + E_R$$

$$= [0.0037] + [10.1479] \text{ MeV}$$

$$= 10.1516 \text{ MeV}$$



Increased kinetic energy of the neutron

$$E_{inc} = \frac{m_{Li-5}}{m_{Li-5} + m_n} \times E_T$$

$$= \frac{5.0109}{5.0109 + 1.0086} \times 10.1516 \text{ Mev}$$

$$= 0.83244455519 \times 10.1516 \text{ Mev}$$

$$\Rightarrow E_{inc} = 8.4506 \text{ Mev}$$

Increased kinetic energy of the lithium-5 [ ${}^5_3\text{Li}$ ]

$$E_{inc} = [E_T - \text{Increased kinetic energy of the neutron}]$$

$$= [10.1516 - 8.4506] \text{ Mev}$$

$$= 1.701 \text{ Mev}$$

Increased velocity of the neutron

$$\begin{aligned}v_{inc} &= \sqrt{\frac{2E_{inc}}{m_n}} \\&= \left[ \frac{2 \times 8.4506 \times 1.6 \times 10^{-13}}{1.6749 \times 10^{-27}} \right]^{\frac{1}{2}} \text{ m/s} \\&= \left[ \frac{27.04192 \times 10^{14}}{1.6749} \right]^{\frac{1}{2}} \text{ m/s} \\&= \left[ 16.1453937548 \times 10^{14} \right]^{\frac{1}{2}} \text{ m/s} \\&= 4.0181 \times 10^7 \text{ m/s}\end{aligned}$$

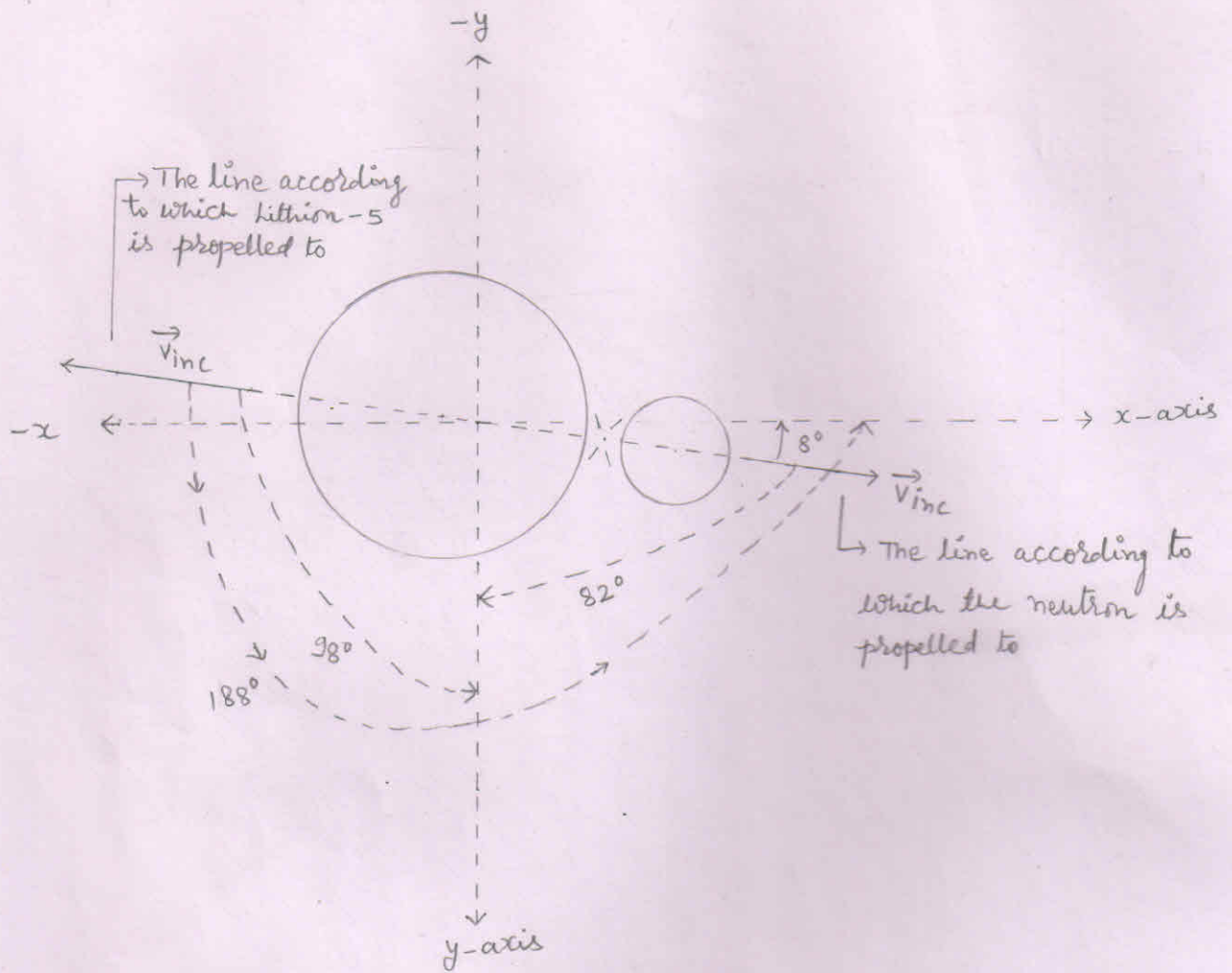
Increased velocity ( $v_{inc}$ ) of the lithium-5

$$\begin{aligned}v_{inc} &= \sqrt{\frac{2E_{inc}}{m_{Li-5}}} \\&= \left[ \frac{2 \times 1.701 \times 1.6 \times 10^{-13}}{8.3205 \times 10^{-27}} \right]^{\frac{1}{2}} \text{ m/s} \\&= \left[ \frac{5.4432 \times 10^{14}}{8.3205} \right]^{\frac{1}{2}} \text{ m/s} \\&= \left[ 0.65419145484 \times 10^{14} \right]^{\frac{1}{2}} \text{ m/s} \\&= 0.8088 \times 10^7 \text{ m/s}\end{aligned}$$

## Angle of propellation

1. As the reduced mass converts into energy, the total energy ( $E_T$ ) propell both the particles with equal and opposite momentum according to a ray (line) perpendicular to the direction (line) of the velocity of the compound nucleus ( $\vec{v}_{CN}$ ).
2. We know that when there a fusion process occurs, then we find the lighter nucleus in the forward direction [or in the direction of ion beam or in the direction of the velocity of the compound nucleus ( $\vec{v}_{CN}$ )].
3. At point 'F', as  $\vec{v}_{CN}$  make  $98^\circ$  angle with x-axis,  $8^\circ$  angle with y-axis and  $90^\circ$  angle with z-axis.
4. So, the neutron is propelled making  $8^\circ$  angle with x-axis,  $82^\circ$  angle with y-axis and  $90^\circ$  angle with z-axis.
5. While the lithium-5 is propelled making  $188^\circ$  angle with x-axis,  $98^\circ$  angle with y-axis and  $90^\circ$  angle with z-axis.

# Propellation of the particles



Components of the increased velocity ( $\vec{V}_{inc}$ ) of the particles

I. For neutron

$$1. \vec{V}_x = V_{inc} \cos \alpha$$

$$V_{inc} = 4.0181 \times 10^7 \text{ m/s}$$
$$\cos \alpha = \cos(8) = 0.99$$

$$\Rightarrow \vec{V}_x = 4.0181 \times 10^7 \times 0.99 \text{ m/s}$$
$$= 3.9779 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inc} \cos \beta$$

$$\cos \beta = \cos(82) = 0.13$$

$$\Rightarrow \vec{V}_y = 4.0181 \times 10^7 \times 0.13 \text{ m/s}$$
$$= 0.5223 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\Rightarrow \vec{V}_z = 4.0181 \times 10^7 \times 0 \text{ m/s} = 0 \text{ m/s}$$

II. For lithium -5

$$1. \vec{V}_{xc} = V_{inc} \cos \alpha$$

$$V_{inc} = 0.8088 \times 10^7 \text{ m/s}$$
$$\cos \alpha = \cos(188) = -\cos(8) = -0.99$$

$$\Rightarrow \vec{V}_x = 0.8088 \times 10^7 \times (-0.99) \text{ m/s}$$
$$= -0.8007 \times 10^7 \text{ m/s}$$

$$2. \vec{V}_y = V_{inc} \cos \beta$$

$$\cos \beta = \cos(98) = -\cos(82) = -0.13$$

$$\Rightarrow \vec{V}_y = 0.8088 \times 10^7 \times (-0.13) \text{ m/s}$$
$$= -0.1051 \times 10^7 \text{ m/s}$$

$$3. \vec{V}_z = V_{inc} \cos \gamma$$

$$\cos \gamma = \cos 90^\circ = 0$$

$$\Rightarrow \vec{V}_z = 0.8088 \times 10^7 \times 0 \text{ m/s} = 0 \text{ m/s}$$

# Components of the final velocity ( $\vec{v}_f$ ) of the particles

## I. For neutron

| According to | Inherited velocity ( $\vec{v}_{inh}$ ) | Increased velocity ( $\vec{v}_{inc}$ ) | Final velocity ( $\vec{v}_f$ )<br>$\vec{v}_f = \vec{v}_{inh} + \vec{v}_{inc}$ |
|--------------|----------------------------------------|----------------------------------------|-------------------------------------------------------------------------------|
| x-axis       | $\vec{v}_x = -0.1130 \times 10^7$ m/s  | $\vec{v}_x = 3.9779 \times 10^7$ m/s   | $\vec{v}_x = 3.8649 \times 10^7$ m/s                                          |
| y-axis       | $\vec{v}_y = 0.8098 \times 10^7$ m/s   | $\vec{v}_y = 0.5223 \times 10^7$ m/s   | $\vec{v}_y = 1.3321 \times 10^7$ m/s                                          |
| z-axis       | $\vec{v}_z = 0$ m/s                    | $\vec{v}_z = 0$ m/s                    | $\vec{v}_z = 0$ m/s                                                           |

## II. For lithium-5

| According to | Inherited velocity ( $\vec{v}_{inh}$ ) | Increased velocity ( $\vec{v}_{inc}$ ) | Final velocity ( $\vec{v}_f$ )<br>$\vec{v}_f = \vec{v}_{inh} + \vec{v}_{inc}$ |
|--------------|----------------------------------------|----------------------------------------|-------------------------------------------------------------------------------|
| x-axis       | $\vec{v}_x = -0.1130 \times 10^7$ m/s  | $\vec{v}_x = -0.8007 \times 10^7$ m/s  | $\vec{v}_x = -0.9137 \times 10^7$ m/s                                         |
| y-axis       | $\vec{v}_y = 0.8098 \times 10^7$ m/s   | $\vec{v}_y = -0.1051 \times 10^7$ m/s  | $\vec{v}_y = 0.7047 \times 10^7$ m/s                                          |
| z-axis       | $\vec{v}_z = 0$ m/s                    | $\vec{v}_z = 0$ m/s                    | $\vec{v}_z = 0$ m/s                                                           |

Final velocity ( $v_f$ ) of the neutron

$$v_f^2 = v_x^2 + v_y^2 + v_z^2$$

$$\begin{aligned}v_x &= 3.8649 \times 10^7 \text{ m/s} \\v_y &= 1.3321 \times 10^7 \text{ m/s} \\v_z &= 0 \text{ m/s}\end{aligned}$$

$$\Rightarrow v_f^2 = (3.8649 \times 10^7)^2 + (1.3321 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f^2 = (14.93745201 \times 10^{14}) + (1.77449041 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f^2 = 16.71194242 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f = 4.0880 \times 10^7 \text{ m/s}$$

Final kinetic energy of the neutron

$$E = \frac{1}{2} m_n v_f^2$$

$$v_f^2 = 16.71194242 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$\Rightarrow E = \frac{1}{2} \times 1.6749 \times 10^{-27} \times 16.71194242 \times 10^{14} \text{ J}$$

$$= 13.9954161796 \times 10^{-13} \text{ J}$$

$$= 8.7471 \text{ Mev}$$

Angles that make the final velocity ( $\vec{v}_f$ ) of the neutron with axes at point F.

1. With x-axis

$$\cos \alpha = \frac{\vec{v}_x}{v_f}$$

$$\vec{v}_x = 3.8649 \times 10^7 \text{ m/s}$$
$$v_f = 4.0880 \times 10^7 \text{ m/s}$$

$$\Rightarrow \cos \alpha = \frac{3.8649 \times 10^7 \text{ m/s}}{4.0880 \times 10^7 \text{ m/s}} = 0.9454$$

$$\Rightarrow \alpha \approx 19^\circ$$

2. With y-axis

$$\cos \beta = \frac{\vec{v}_y}{v_f}$$

$$\vec{v}_y = 1.3321 \times 10^7 \text{ m/s}$$

$$\Rightarrow \cos \beta = \frac{1.3321 \times 10^7 \text{ m/s}}{4.0880 \times 10^7 \text{ m/s}} = 0.3258$$

$$\Rightarrow \beta \approx 71^\circ$$

3. With z-axis

$$\cos \gamma = \frac{\vec{v}_z}{v_f}$$

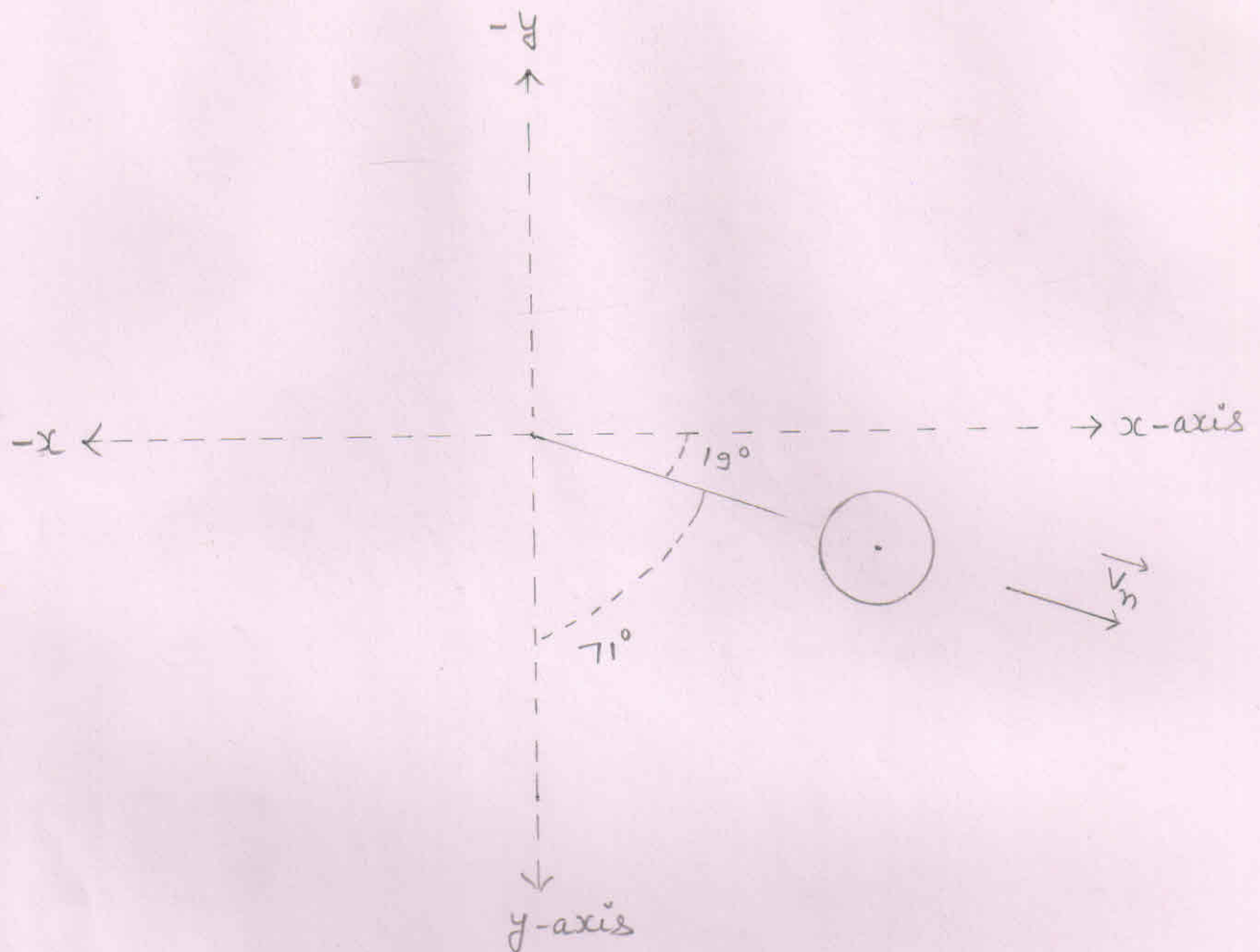
$$\vec{v}_z = 0 \text{ m/s}$$

$$\Rightarrow \cos \gamma = \frac{0 \text{ m/s}}{4.0880 \times 10^7 \text{ m/s}} = 0$$

$$\Rightarrow \gamma = 90^\circ$$



The angles that make the final velocity ( $\vec{v}_f$ ) of the neutron :-



Final velocity of the lithium-5

$$v_f^2 = v_x^2 + v_y^2 + v_z^2$$

$$v_x = 0.9137 \times 10^7 \text{ m/s}$$

$$v_y = 0.7047 \times 10^7 \text{ m/s}$$

$$v_z = 0 \text{ m/s}$$

$$\Rightarrow v_f^2 = (0.9137 \times 10^7)^2 + (0.7047 \times 10^7)^2 + (0)^2 \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f^2 = (0.83484769 \times 10^{14}) + (0.49660209 \times 10^{14}) + 0 \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f^2 = 1.33144978 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f = 1.1538 \times 10^7 \text{ m/s}$$

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$$\Rightarrow v_f^2 = 1.33144978 \times 10^{14} \text{ m}^2/\text{s}^2$$

$$\Rightarrow v_f = 1.1538 \times 10^7 \text{ m/s}$$

Angles that make the final velocity ( $\vec{v}_f$ ) of the lithium-5 with axes at F point F.

1. With x-axis

$$\cos \alpha = \frac{\vec{v}_x}{v_f}$$

$$\vec{v}_x = -0.9137 \times 10^7 \text{ m/s}$$
$$v_f = 1.1538 \times 10^7 \text{ m/s}$$

$$\Rightarrow \cos \alpha = \frac{-0.9137 \times 10^7 \text{ m/s}}{1.1538 \times 10^7 \text{ m/s}} = -0.7919$$

$$\Rightarrow \alpha \approx 142.3$$

$$[\because \cos(142.3) = -\cos(37.7) = -0.7912]$$

2. With y-axis

$$\cos \beta = \frac{\vec{v}_y}{v_f}$$

$$\vec{v}_y = 0.7047 \times 10^7 \text{ m/s}$$

$$\Rightarrow \cos \beta = \frac{0.7047 \times 10^7 \text{ m/s}}{1.1538 \times 10^7 \text{ m/s}} = 0.6107$$

$$\Rightarrow \beta \approx 52.3$$

$$[\because \cos(52.3) = 0.6115]$$

3. With z-axis

$$\cos \gamma = \frac{\vec{v}_z}{v_f}$$

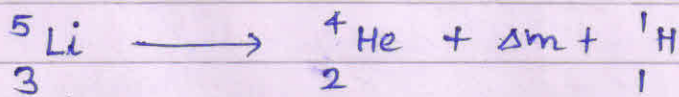
$$\vec{v}_z = 0 \text{ m/s}$$

$$\Rightarrow \cos \gamma = \frac{0 \text{ m/s}}{1.1538 \times 10^7 \text{ m/s}} = 0$$

$$\Rightarrow \gamma = 90^\circ$$



For the fusion reaction :-



⇒ The lithium-5 is an unstable homogenous nucleus. So, the lithium-5 again behave as a homogenous compound nucleus.

So, for stability, the groups of quarks that compose the lithium-5 again rearrange with the surrounding gluons and form the lobes 'A' and 'B' within into the homogenous compound nucleus [the lithium-5] and thus turns the lithium-5 into a heterogenous compound nucleus.

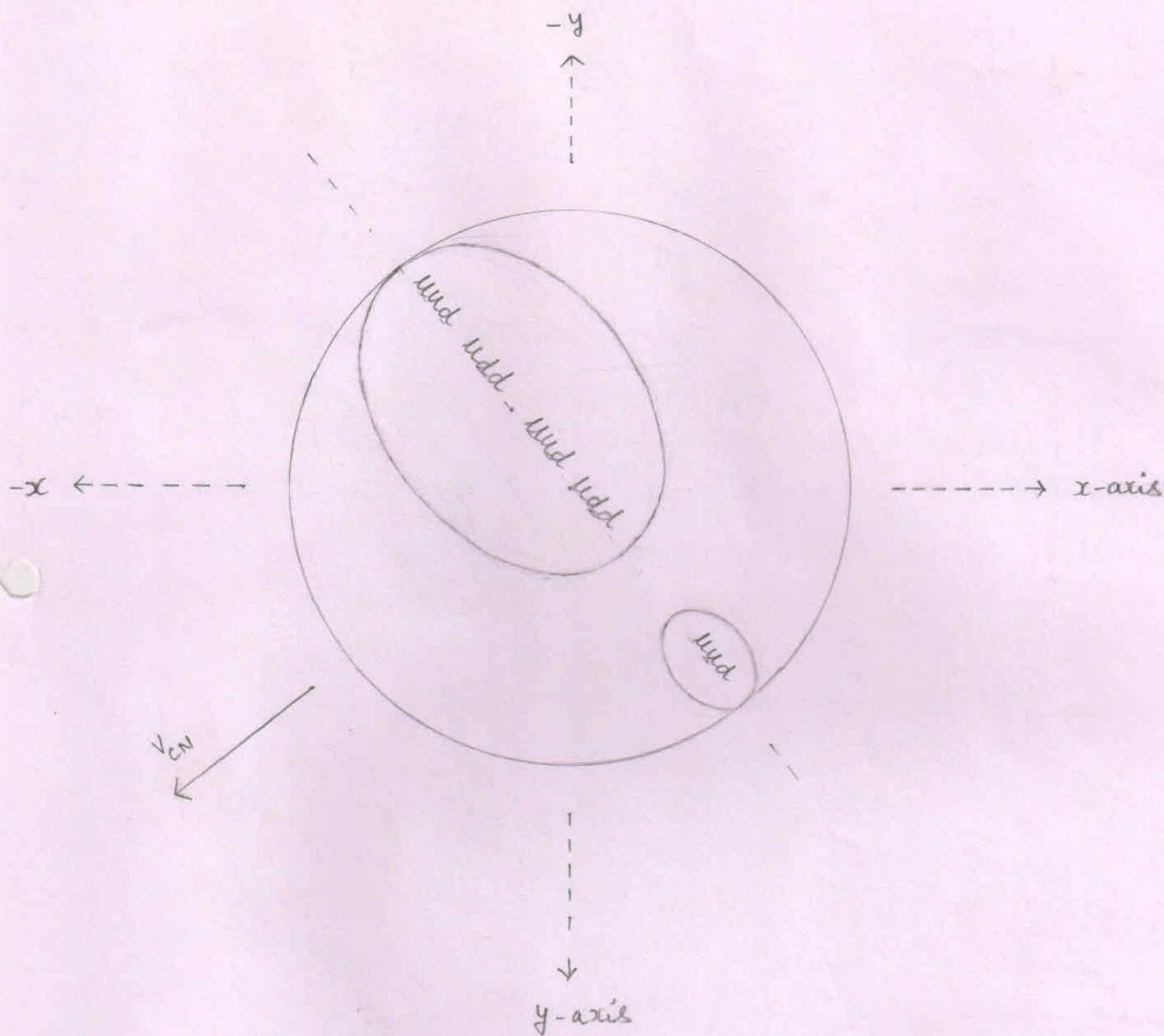
Formation of lobes within into the homogenous compound nucleus or the transformation of the homogenous compound nucleus into the heterogenous compound nucleus :-

The central group of quarks with its surrounding gluons to become a stable and the just lower nucleus (the helion-4) than the homogenous nucleus (the lithion-5) includes the other three (nearby located) groups of quarks with their surrounding gluons and rearrange to form the 'A' lobe of the heterogenous compound nucleus.

While the remaining group of quarks to become a stable nucleus (the proton) includes its surrounding gluons or mass [out of the available mass (or gluons) that is not included in the formation of the lobe 'A'] and rearrange to form the 'B' lobe of the heterogenous compound nucleus.

Thus, due to formation of two dissimilar lobes within into the homogenous compound nucleus, the homogenous compound nucleus transforms into the heterogenous compound nucleus.

### 3] Formation of lobes



⇒ Within into the homogenous compound nucleus, the greater nucleus is the helium-4 nucleus and the smaller nucleus is the proton while the remaining space represents the remaining gluons.

⇒ Within into the homogenous compound nucleus, the greater nucleus is the lobe 'A' while the smaller nucleus is the lobe 'B'



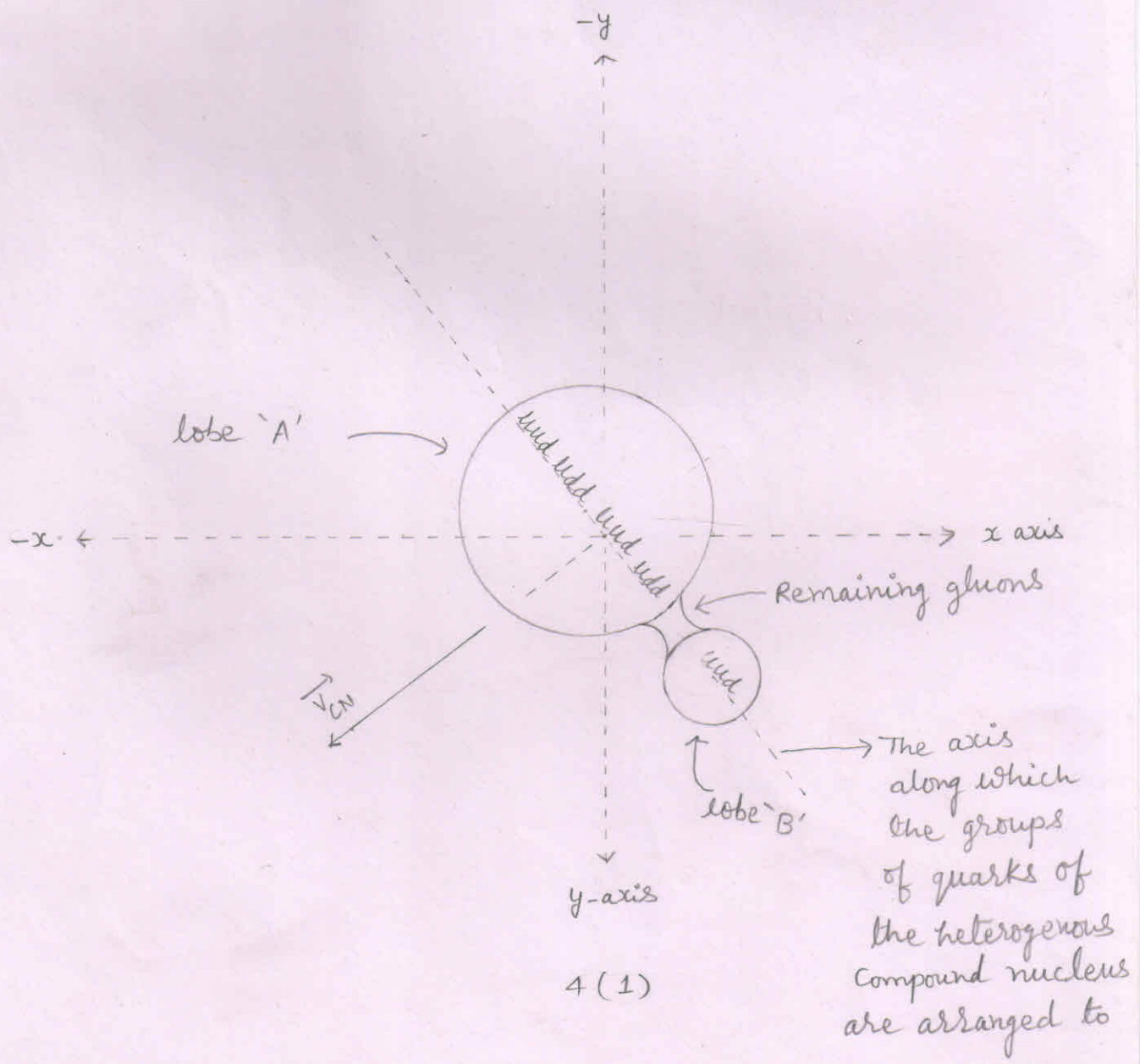
4. Final Stage of the heterogenous compound nucleus:-

The process of formation of lobes creates voids between the lobes. So, the remaining gluons [ or the mass that is not involved in the formation of any lobe ] rearrange to fill the void(s) between the lobes and thus the remaining gluons form a node between the two dissimilar lobes of the heterogenous compound nucleus.

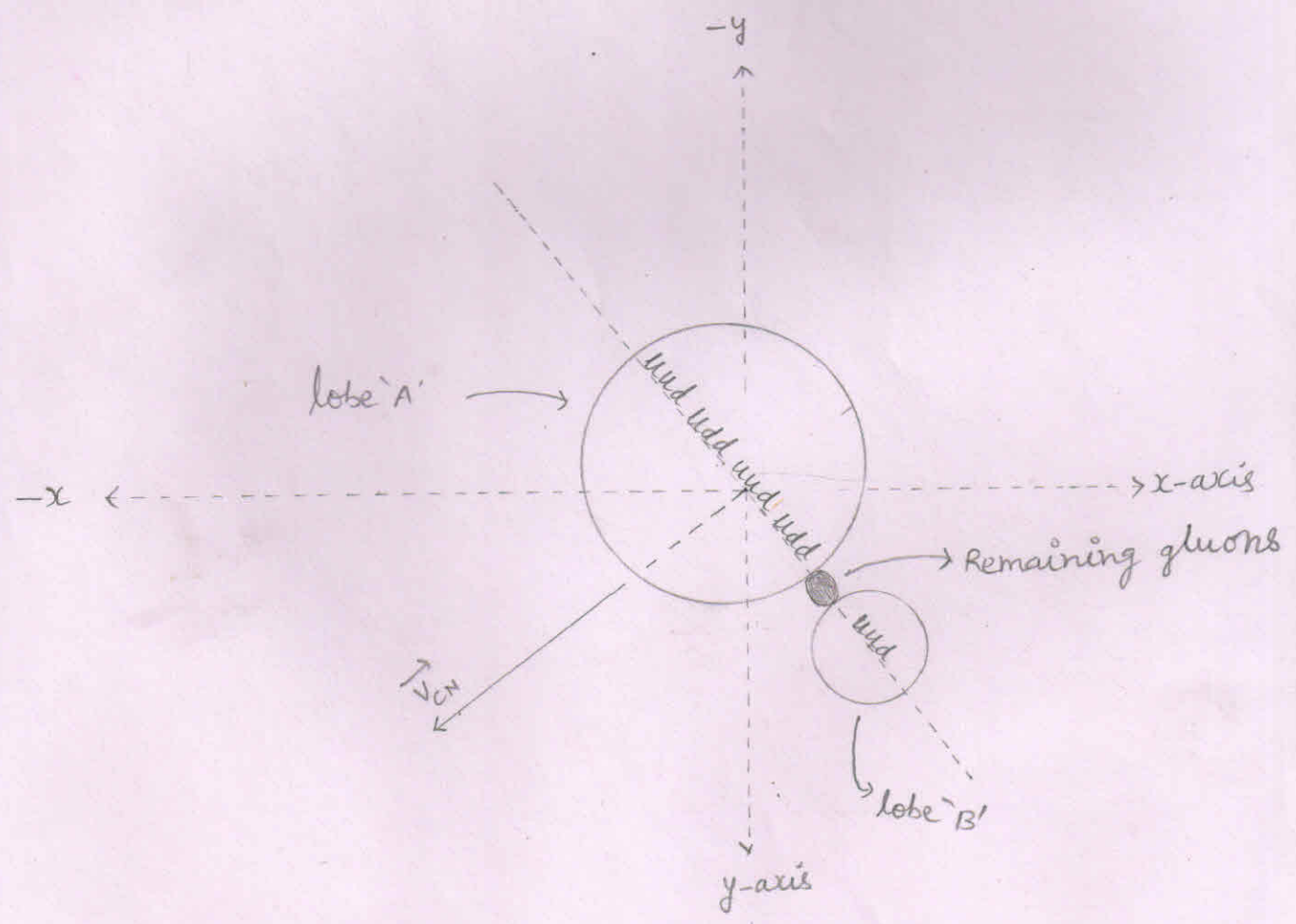
Thus, the reduced mass (or the remaining gluons) keeps both the dissimilar lobes - of the heterogenous compound nucleus - joined them together.

So, finally, the heterogenous compound nucleus becomes like an abnormal digit eight or becomes like a dumb-bell.

Final stage of the heterogenous compound nucleus



Final stage of the heterogenous compound nucleus



4 (2)

## The Splitting of the heterogeneous Compound nucleus :-

⇒ The heterogeneous compound nucleus, due to its instability, splits according to the lines parallel to the direction of the velocity of the compound nucleus ( $\vec{V}_{CN}$ ) into three particles - the helium-4 nucleus, the proton and the reduced mass ( $\Delta m$ ).

out of them, the two particles (the helium-4 and the proton) are stable while the third one (reduced mass) is unstable.

⇒ According to the law of inertia, each particle that has separated from the compound nucleus, has an inherited velocity ( $\vec{v}_{inh}$ ) equal to the velocity of the compound nucleus ( $\vec{V}_{CN}$ ).

⇒ So, for conservation of momentum

$$M\vec{V}_{CN} = (m_{he-4} + \Delta m + m_p) \vec{V}_{CN}$$

where,

$M$  = Mass of the compound nucleus

$\vec{V}_{CN}$  = velocity of the compound nucleus

$M$  = Mass of the compound nucleus that is equal to the mass of the lithium-5.

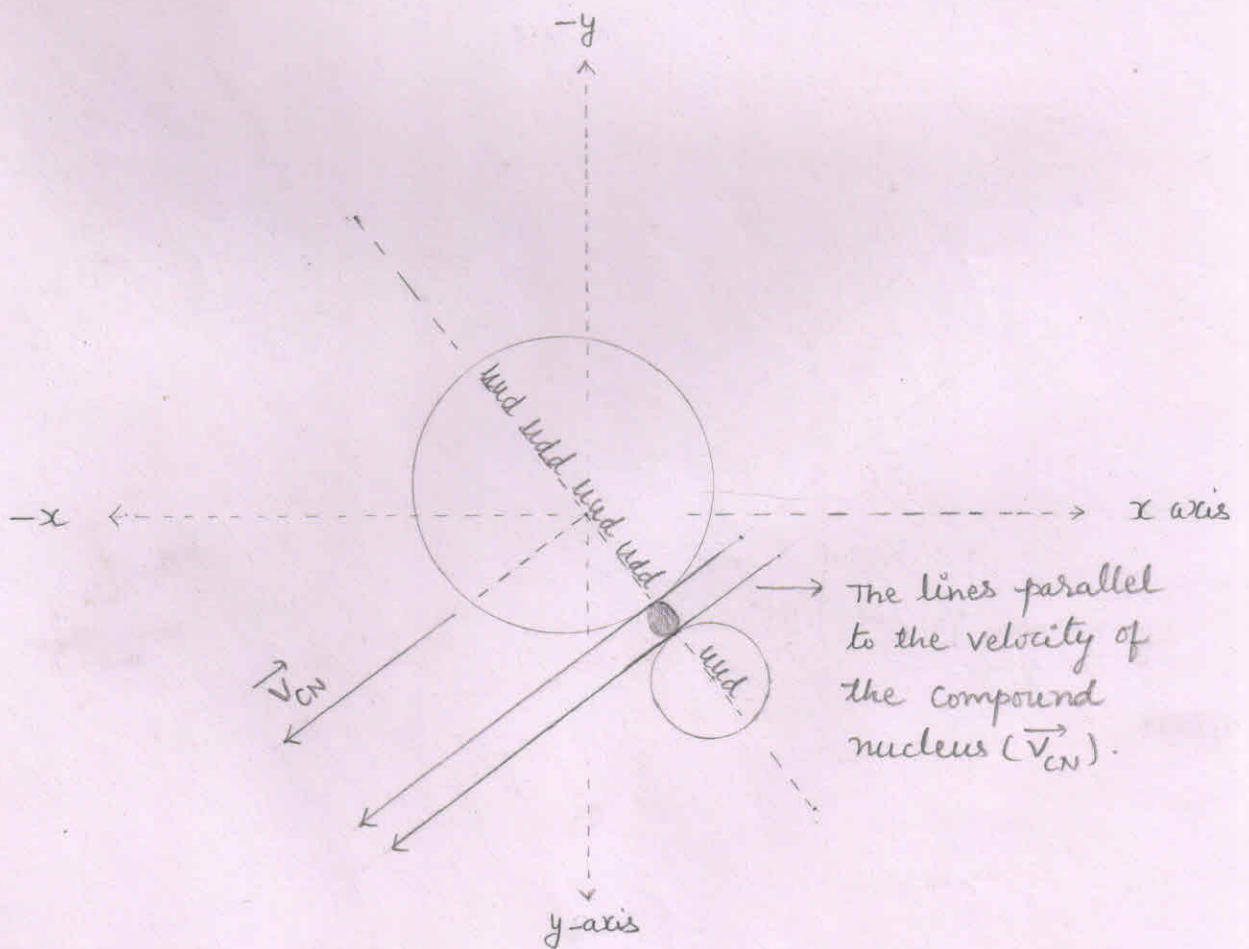
$\vec{V}_{CN}$  = velocity of the compound nucleus.

$m_{he-4}$  = mass of the helium-4 nucleus

$\Delta m$  = reduced mass

$m_p$  = mass of the proton

The splitting of the heterogeneous compound nucleus



The splitting of the heterogenous compound nucleus :-

The heterogenous compound nucleus splits into three particles - the helium-4 nucleus, the reduced mass ( $\Delta m$ ) and the proton

